The development of design guidance for bridges in New Zealand for liquefaction and lateral spreading effects

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A Murashev, D Kirkcaldie and C Keepa, Opus International Consultants, Wellington
M Cubrinovski, University of Canterbury, Christchurch
R Orense, University of Auckland, Auckland

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Executive summary

Introduction

This report is a result of a NZ Transport Agency (Transport Agency) research project towards the development of guidelines for the design of bridges on sites prone to liquefaction and lateral spreading in New Zealand. The purpose of the report is to identify a clear set of available procedures for analysis and design that are based on observed seismic behaviour of bridges (reviewed case studies) and on the most recent research findings.

Liquefaction-related design issues

Design of bridges for liquefaction and lateral spreading effects is a complex technical problem and a large number of issues associated with the design process should be considered. Key considerations include geotechnical investigations, evaluation of liquefaction and lateral spreading, ground improvement, analysis of the effects of liquefaction and lateral spreading on the bridge structure, structural design issues and post-construction monitoring issues.

Preliminary considerations

The preliminary considerations for the design of bridges on sites which are susceptible to liquefaction and lateral spreading include compliance with the structure performance requirements and standards, liquefaction effects on structures, lateral spreading effects on structures and geotechnical pile capacity following liquefaction.

Geotechnical investigations

In order to understand the full extent of the liquefiable deposits and the level of liquefaction susceptibility, site-specific geotechnical investigations need to be undertaken. A preliminary geotechnical appraisal is carried out initially to establish the site topography, stratigraphy and location of groundwater table.

If the preliminary geotechnical appraisal indicates the presence of liquefiable materials, site-specific geotechnical investigations may be required. A programme of geotechnical investigation should be developed to obtain sufficient information for the assessment of liquefaction potential of the site soils and for seismic analysis.

All of the information collected during the preliminary geotechnical appraisal and the geotechnical investigations should be interpreted and reported. The geotechnical investigation report should outline the methodology used in the interpretation of the collected information.

Evaluation of liquefaction and lateral spreading

The seismic demand of the bridge site should be evaluated using the NZ Transport Agency’s Bridge manual (3rd edition) where the peak ground acceleration to be applied is unweighted and derived for the relevant return period.

Alternatively, the Geotechnical earthquake engineering practice: module 1 – guideline for the identification, assessment and mitigation of liquefaction hazards prepared by the New Zealand Geotechnical Society can be used for this purpose.
Methods of ground improvement

Ground improvement methods can be categorised into densification, solidification, drainage, reinforcement and replacement of liquefiable soils as well as increase of in-situ stresses by either surcharging the soils or lowering the groundwater table. The report summarises the most common liquefaction countermeasures and gives brief descriptions of the principles behind the improvement mechanism associated with each category of the ground improvement methods along with some references detailing the design of ground treatment schemes and methods to evaluate the effectiveness of soil improvement.

Methods of analysis

Phases of response

When evaluating the effects of liquefaction and lateral spreading on the performance of the bridge pile foundations using equivalent static analyses, it is necessary to conduct separate analyses for different phases of the response. The following analyses corresponding to different phases of the response should be carried out:

- Cyclic analysis without liquefaction, in which inertial loads that would occur in the absence of liquefaction are considered.
- Cyclic liquefaction analysis, estimating the potential and consequences of liquefaction, and considering simultaneous kinematic loads (due to cyclic ground displacements) and structural inertial loads while accounting for stiffness and strength degradation due to excess pore water pressures.
- Lateral spreading analysis, estimating the potential for liquefaction and consequences of lateral spreading including large stiffness and strength degradation and kinematic loads due to large displacements associated with lateral spreading. Inertial loads may be considered in this analysis, but such loads are of secondary importance in the spreading phase, and can be ignored in many cases.

Classification of design methods

Methods of analysis for bridges and piles in liquefied soils range from simplified methods using an equivalent static analysis approach to a rigorous time history analysis based on the effective stress principle. These analysis methods can be classified into three different categories:

1. Pseudo-static analysis (PSA) or equivalent static analysis.
2. Direct dynamic time history analysis: a) effective stress analysis (ESA) considering effects of excess pore pressures and liquefaction through detailed constitutive modelling, and b) total stress analysis (TSA), dynamic analysis using total stresses or equivalent stresses (either ignoring excess pore pressures or considering them in a simplified manner). In the direct method of analysis (ESA and TSA), the response of the soil-pile-pier-abutment-deck system can be considered over the entire period of time from the initiation of shaking to the final stage of post-earthquake equilibrium and residual deformation of the bridge in a single analysis.
3. Substructure analysis methods which use some features of PSA, ESA or TSA but are essentially hybrid approaches tailored to address specific aspects in the performance assessment. For example, the well-known Newmark-type analysis (which is a simplified, user-defined time history analysis) would be a typical representative of this group of methods. The substructure method uses a set of separate but related analyses to assess the performance of a bridge subsystem.
Executive summary

The effect of liquefaction and lateral spreading can be evaluated by considering a single member (e.g., a single pile), a subsystem of the bridge (pile group, pier piles or piled abutment), or the whole bridge. Each of these models is acceptable in the evaluation of the bridge performance provided that proper boundary conditions and modelling assumptions are used, and that there is a clear understanding of the analysis objectives and limitations. The cyclic response should be considered both in the transverse and longitudinal directions, whereas the lateral spreading response is commonly considered in the longitudinal direction of the bridge.

**Pseudo-static analysis**

Based on our review of available PSA methods, the following design methods would be appropriate for New Zealand conditions and are described in the report:

- Cubrinovski method
- Pacific Earthquake Engineering Research Center (PEER) method

**Time history analysis**

A non-linear time history analysis allows investigation of the dynamic response of the bridge while accounting for the complex soil-pile-pier-abutment-deck interaction or response of the bridge system in liquefying and laterally spreading soils. A sound numerical analysis that is well calibrated and executed provides the most realistic simulation of the actual bridge behaviour.

**Substructure analysis**

A design procedure proposed in a 2003 report by the Multidisciplinary Center for Earthquake Engineering Research is considered to be appropriate for the substructure analysis and is described in the research report.

**Structural mitigation approaches**

Two main approaches for mitigation of liquefaction induced lateral spreading are described:

1. Minimising the effect of lateral spreading on the most vulnerable part of the structure and utilisation of the superstructure to support the abutments and piers
2. Resisting lateral spread loads at the abutments.

Soil structure interaction should be considered in the design of foundations under the effect of lateral spreading loads.

**Conclusions and recommendations**

Available design procedures based on observed seismic behaviour of bridges and on the most recent research findings have been summarised and design methods appropriate for New Zealand conditions have been identified. Additional work will be required to summarise the findings in a form of a technical memorandum which can be later incorporated into NZ Transport Agency’s *Bridge manual* and disseminated to the wider New Zealand engineering community.
Abstract

This report presents a summary of the outcomes from a research project commissioned by the NZ Transport Agency to develop design guidance for bridges in New Zealand for liquefaction and lateral spreading effects. The study involved review of relevant case studies and available design methods. The report summarises available design procedures that are based on observed seismic behaviour of bridges and on the most recent research findings, and identifies design methods appropriate for New Zealand conditions. The report also considers issues associated with liquefaction and lateral spreading and their effect on bridge structures and summarises requirements for geotechnical investigations, evaluation techniques for liquefaction and lateral spreading, methods of ground improvements, methods of liquefaction analysis, structural mitigation solutions, construction and monitoring issues. The report also identifies areas where supporting information is not available and further research work is required. Additional work is recommended to summarise the findings in a form of a technical memorandum which can be later incorporated into the NZ Transport Agency’s Bridge manual and disseminated to the wider New Zealand engineering community. This report is intended for engineers who are familiar with geotechnical and structural design practice for static and seismic loading of bridges.
1 Introduction

New Zealand’s state highway network has a vital role as the strategic road network for the country, enabling people to get to and from work quickly and efficiently, providing a convenient and robust route for freight and connecting communities. Also, New Zealand state highways serve as primary lifelines following natural disasters. The seismic performance of bridges has a substantial effect on post-earthquake response and recovery efforts and on the quality of life of affected communities.

Bridges and highway structures located at sites with shallow groundwater tables or close to bodies of water can be susceptible to earthquake damage. Liquefaction of saturated sand-like materials (sands, sandy gravels, non-plastic silts) and cyclic softening or cyclic failure of clay-like materials (plastic silts and clays) and lateral spreading can result in significant damage to bridges and highway structures.

Earthquake damage to bridge abutment slopes on sites prone to liquefaction and lateral spreading may include ground failures, excessive lateral displacements and settlements. A large number of recorded cases of damage to bridge foundations due to the lateral displacements and settlements associated with liquefaction have been reported worldwide. There are also recent examples of earthquake damage to bridge structures caused by liquefaction and lateral spreading in Christchurch as a result of the 2010 Darfield and 2011 Christchurch earthquakes.

Soil deformation caused by liquefaction and lateral spreading can result in damage to bridge abutments, pier foundations and structural elements of bridges. Damage to bridges associated with liquefaction and lateral spreading has been well documented. Information on causes and effects of liquefaction and lateral spreading as well as some case studies are included in appendix A. A detailed report on the performance of highway structures during the Darfield and Christchurch earthquakes of 4 September 2010 and 22 February 2011 has been prepared by Wood et al (2012).

A conservative design approach quite often results in the need for costly ground improvement to fully mitigate against liquefaction, cyclic softening and lateral spreading at bridge sites. Regular review and improvement of design methods for bridges located on sites prone to liquefaction and lateral spreading is critical for the development of cost-effective bridge designs.

This report is a result of a NZ Transport Agency (Transport Agency) research project towards the development of design guidelines for the design of bridges on sites prone to liquefaction and lateral spreading in New Zealand. The research project included a review of seismic behaviour of bridges on sites prone to liquefaction and lateral spreading in New Zealand and overseas, review of available design methods for bridges against liquefaction and lateral spreading effects as well as detailed consideration of the bridge design framework in New Zealand.

The purpose of this report is to identify a clear set of available procedures for analysis and design based on observed seismic behaviour of bridges (reviewed case studies) as well as on the most recent research findings. The report summarises these methods and provides references to supporting materials (where such references are available) and identifies design methods appropriate for New Zealand conditions. A clear set of design guidelines and design examples will be developed as part of a proposed extension of the project. The guidelines will then be incorporated into the Bridge manual (NZ Transport Agency 2013a).

The report also considers a large number of issues associated with liquefaction and lateral spreading and their effect on bridge structures, and summarises requirements for geotechnical investigations, evaluation techniques for liquefaction and lateral spreading, methods of ground improvements, methods of liquefaction analysis, structural mitigation solutions, construction and monitoring issues. It was not possible to address all design issues in detail within the scope of this research project, therefore the
report also identifies areas where supporting information is not available and further research work is required. Design of bridges for liquefaction and lateral spreading effects is a complex technical problem and a large number of issues associated with the design process require further research and refinement. Additional work will be required to summarise the findings in a form of a technical memorandum which can be later incorporated into the Transport Agency’s (2013a) *Bridge manual* and disseminated to the wider New Zealand engineering community.

This report promotes close interaction between structural and geotechnical engineers through the design process and is intended for engineers who are familiar with geotechnical and structural design practice for static and seismic loading of bridges.
2 Preliminary considerations

2.1 Liquefaction-related design issues

The key considerations and issues that are important for the design of bridges on sites prone to liquefaction and lateral spreading include those relating to:

- **geotechnical investigations:**
  - scoping and staging of geotechnical investigations to obtain necessary information for analysis of liquefaction and lateral spreading
  - geotechnical investigation techniques for field and laboratory testing
  - determination of site subsoil class
  - development of a reliable ground model

- **the evaluation of liquefaction and lateral spreading:**
  - determination of seismic demand (global seismic hazard analysis or site-specific seismic studies)
  - liquefaction triggering (seismic demand and liquefaction resistance)
  - liquefaction-induced ground displacements (transient and settlement)
  - permanent ground displacements due to spreading
  - evolution of liquefaction and associated loads with time
  - influence of embankments on liquefaction and stability of embankments on liquefied soil
  - characteristics, uncertainties and outstanding issues in the state-of-the-practice methods for evaluation of triggering of liquefaction, settlement and lateral spreading
  - some issues of practical concern (liquefaction of low plasticity silts, probabilistic vs deterministic liquefaction evaluation, effect of groundwater conditions and artesian water heads, liquefaction at depth and maximum depth of liquefaction, cyclic mobility, partial liquefaction and limited shear strain)
  - additional geotechnical investigations to refine analysis of liquefaction and lateral spreading (if the need for such refinement can be justified)
  - assessment of reduced bearing/pull out capacity of the foundation piles and of the effect of negative skin friction

- **ground improvement:**
  - available methods of ground improvement
  - cost of ground improvement work
  - reliability and resilience of adopted ground improvement methods (including factors affecting choice of ground improvement techniques)
  - effectiveness of ground improvement in mitigating liquefaction and/or its effects
  - level of design and construction documentation and quality assurance (QA) required for ground improvement
• detailed analysis of the effect of liquefaction and lateral spreading on the bridge structure:
  – methods of analysis (framework and selection of appropriate method)
  – determination of model parameters (range of values)
  – boundary conditions and pile-group effects
  – key uncertainties (sensitivity analysis)
  – soil-foundation-abutment-structure interaction
  – performance criteria (displacements, plastic deformation in piles and piers, need for post-earthquake repair or replacement of the bridge)
  – design, modelling, analysis and interpretation of effects of ground improvement

• structural design:
  – interaction between structural and geotechnical designers
  – definition of acceptable damage states and design for adopted damage states
  – structural detailing of bridges to reduce damage and increase reparability

• construction:
  – confirmation of ground conditions and design assumptions
  – control of ground improvement quality

• post-construction monitoring:
  – equipment to monitor post-earthquake performance of bridges (eg inclinometers in piles and/or ShapeAccelArray™ which consists of a chain of sensor elements (segments) joined together in such a manner that they can move in relation to each other in all directions except for twisting, each segment contains a multi-axial MEMSchip accelerometer which makes the segment act as an extremely accurate inclinometer)
  – post-earthquake inspections and assessment

The quality of the developed design solution, the seismic behaviour of bridges and the ability of the bridge and geotechnical engineers to assess the post-earthquake condition of the bridge are highly dependent on whether all of these issues have been adequately addressed.

2.2 Structure performance requirements

The NZ Transport Agency (2013a) Bridge manual 3rd edition sets out the structure performance requirements in section 5.1.2 as follows:

*The primary objective of seismic design shall be to ensure that the structure can safely perform its function of maintaining communications after a seismic event. The extent to which this is possible will depend on the severity of the event, and thus by implication on its return period.*

*For design purposes, the structures shall be categorised according to their importance, and assigned a risk factor related to the seismic return period. This will then result in an equivalent design earthquake hazard and consequent loading as defined in 5.2.*
If the behaviour at this design intensity meets the criteria of (a), it is expected that with appropriate detailing, behaviour at other intensities as in (b) and (c) will also be satisfactory, and no further specific analytical check is required except where there is the possibility of loss of ground strength or failure that could bring about structure collapse. However, performance expectations outlined below warrant philosophic consideration in design and detailing, and discussion in the structure options report and structure design statement.

The seismic performance criteria requirements are as follows [reproduced below as table 2.1]:

(a) After exposure to a seismic event of design severity, the structure shall be useable by emergency traffic, although damage may have occurred, and some temporary repairs may be required to enable use. Permanent repair to cater for at least one subsequent seismic event of design severity should be feasible.

(b) After an event with a return period significantly less than the design value, damage should be minor, and there should be no disruption to traffic.

(c) After an event with a return period significantly greater than the design value, the structure should not collapse, although damage may be extensive. It should be useable by emergency traffic after temporary repairs and should be capable of permanent repair, although a lower level of loading may be acceptable.

Table 2.1  Seismic performance requirements (from the NZ Transport Agency Bridge manual 3rd edition)

<table>
<thead>
<tr>
<th>Earthquake severity</th>
<th>Minor earthquake as (b) Return period factor = R_u/4</th>
<th>Design level earthquake as (a) return period factor = R_u (ULS event)</th>
<th>Major earthquake as (c) Return period factor = 1.5 R_u</th>
</tr>
</thead>
<tbody>
<tr>
<td>Post-earthquake function - immediate</td>
<td>No disruption to traffic</td>
<td>Useable by emergency traffic</td>
<td>Useable by emergency traffic after temporary repair</td>
</tr>
<tr>
<td>Post-earthquake function - reinstatement</td>
<td>Minimal reinstatement necessary to cater for all design-level actions</td>
<td>Feasible to reinstate to cater for all design-level actions, including repeat design-level earthquake</td>
<td>Capable of permanent repair, but possibly with reduced load capacity</td>
</tr>
<tr>
<td>Acceptable damage</td>
<td>Damage minor</td>
<td>Damage possible; temporary repair may be required</td>
<td>Damage may be extensive; collapse prevented</td>
</tr>
</tbody>
</table>

The design of any structure located in an area which is susceptible to earthquake induced liquefaction, or which is over an active fault with a recurrence interval of 2000 years or less, shall recognise the large movements which may result from settlement, rotation or translation of substructures. To the extent practical and economic, and taking into consideration possible social consequences, measures shall be incorporated to mitigate against these effects.

2.3 Liquefaction effects on structures

2.3.1 Ground settlement

Effects on the structure include the following:
• overall settlement, and differential settlement between supports and across the width of the structure, racking the structure
• down-drag loading induced on the foundation piles
• effect on services carried on the bridge.

Loss of stiffness and strength of soil have the following consequences:
• reduction in bearing and pull out capacity of deep foundations (piles)
• reduction in stiffness and strength of soil resisting lateral movement of deep foundations (piles)
• effect on overall stiffness of the bridge structure.

2.3.2 Ground lateral spreading

The behaviour of laterally spreading ground can be described as follows:
• Lateral spreading arises as a result of loss of strength in the ground giving rise to failure through higher ground and down into underlying liquefied material as the higher ground seeks to reduce its potential energy by settling and spreading. The ground surface seeks to level itself and flow will be towards areas of lower ground surface level or open face of the channel (waterway). Spreading displacements can be driven either by inertial loads during the strong ground shaking or by post-liquefaction gravity-imposed loads.
• The depth of lateral soil spreading is to be determined by the depth of the river channel and location of critical layers governing the spreading.
• Stronger material as usually exists in bridge approach embankments can 'raft' on top of liquefied underlying material.

The following effects on the structure should be considered:
• The effect of lateral spreading on the foundations (and the other way around) depends on whether soil moves past the foundation (typically the case when there is no (significant) raft/crust on top of the liquefied layer) or a significant movement of the foundation occurs (typically when a raft/crust of non-liquefiable material exists on top of the liquefiable layer). The assessment requires a comparison between the passive soil forces imposed by the soil on the foundation system versus ultimate structural resistance.
• Lateral loading will be applied to structure elements that the spreading soil comes in contact with. This lateral loading on a single pile can be as high as 4.5x the rankine passive pressure. For individually widely spaced piles, where soil arching between piles comes into play, the effective width is the width of the pile group.
• Lateral spreading loads should be assessed using the material properties appropriate to the state of the soil materials. Reduced properties should be adopted for laterally spreading liquefied material. Note that pile group effect in the liquefied layers may not be as significant as in the non-liquefied soils.
• Damage to piles has occurred particularly at the boundaries in soil layers at which significant changes in stiffness occur.
• The pinning effect (resistance to lateral movement) of the foundation system should be taken into account.
2.3.3 Effects of liquefaction on the vertical response of piles

Pile response to lateral spreading and inertia often dominate the design of bridge piles in areas susceptible to liquefaction. However, vertical aspects of the pile response must also be considered in design. These aspects include:

- temporary reduction in pile geotechnical capacity
- reduced structural capacity of the pile
- settlement of the pile head.

2.3.3.1 Geotechnical pile capacity following liquefaction

The generation of excess pore water pressure in liquefied layers and the associated reduction in soil strength will reduce the geotechnical capacity of piles. As excess pore pressures dissipate in the hours to weeks following the initiation of liquefaction, the near pre-earthquake pile capacity of piles will return. Piles and pile groups should be designed so they have sufficient geotechnical capacity to satisfy the post-earthquake performance requirements given in the Bridge manual. When calculating post-liquefaction pile capacity, no capacity from shaft friction should be assumed for sections of the shaft in liquefiable soils. Piles can form preferential pathways for dissipation of excess pore pressures from liquefied layers. Shaft friction may also be reduced in non-liquefied layers following a strong earthquake due to gapping between the soil and piles from plastic deformation of the crust with back and forward movement during shaking. Therefore consideration should be given to reducing shaft friction for sections of pile in non-liquefiable layers for design.

Liquefaction of layers near the tip of piles and pile groups (both above and below) can severely reduce their end bearing capacity. The migration and redistribution of pore pressures throughout the soil profile (as excess porewater pressures dissipate from liquefied layers) can also reduce the strength of a dense bearing stratum. Furthermore, research has shown that excess porewater pressures can be generated in non-liquefiable dense bearing layers during strong earthquake shaking, reducing their capacity to support piles (Madabhushi et al 2010).

The ultimate geotechnical end bearing capacity of individual piles following initiation of liquefaction can be calculated using conventional methods with reduced strengths for liquefied soils near the tip and, where relevant, reduced strength of the bearing layer itself. Madabhushi et al (2010) provide guidelines for accounting for pore pressure increases in dense bearing strata and designing piles against bearing failure at sites with liquefiable soils.

2.3.3.2 Pile settlement

Three mechanisms that can cause post-liquefaction vertical subsidence of pile heads are:

1. Transfer of axial load from the pile shaft to its base when soil surrounding the shaft liquefies
2. Down-drag with reconsolidation of liquefied layers as excess pore pressures dissipate and the downward friction of non-liquefied layers excavated above the liquefied layers. Subsidence results from compression of the pile and shear deformation of soil around the lower part of the pile as the load on the base increases
3. Post-liquefaction reconsolidation of liquefied layers below the pile bearing layer.

Settlements due to load transfer during reconsolidation of liquefied sand can be estimated using the method by Boulanger et al (2003) which is essentially a modification of the neutral plane solution originally developed by Fellenius (1972).
2.3.3.3 Structural pile capacity following liquefaction

Piles in liquefiable soil can be susceptible to buckling from reduced lateral support of the pile and lateral displacement of the pile head (p-delta effects). Madabhushi et al (2010) and Bhattacharya (2006) provide guidelines for calculating the potential for buckling of piles in liquefiable ground.

This report mostly deals with lateral response of piles affected by liquefaction and lateral spreading. While the vertical response of piles affected by liquefaction is important and should be considered in the design process, detailed consideration of this issue and development of detailed recommendations on this design aspect was beyond the scope of this research.
3 Geotechnical investigations

Geotechnical investigations for the assessment of liquefaction potential of soils and their seismic behaviour are generally carried out in several stages:

1. Preliminary geotechnical appraisal of the site ground conditions
2. Geotechnical investigations
3. Evaluation of liquefaction potential and potential consequences of liquefaction.

3.1 Preliminary geotechnical appraisal

A preliminary geotechnical appraisal involves establishing the topography, stratigraphy and location of the ground water table at the project site. This preliminary geotechnical work should address the following questions (California Geological Survey 2008):

- Are potentially liquefiable soils present?
- What is the grain size and grading of soils?
- Are they saturated and/or likely to become saturated at some future date?
- Are they of sufficient thickness and/or lateral extent to pose potential risk of damaging ground deformations (including lateral spreading)? (Liquefaction hazards are commonly considered in the top 20m, but on a slope near a free face or where deep foundations go beyond that depth, liquefaction potential should be considered at greater depths.)
- Does the geometry of liquefiable soil zones within the foundation soils pose significant risks that require further investigation? (Thick deposits of liquefiable soils generally require further investigation. Additionally, relatively thin seams of liquefiable soils, if laterally continuous over sufficient area, can represent potentially hazardous planes of weakness and sliding, and may thus pose a hazard with respect to lateral spreading and related ground displacements.)

Important considerations for the stage of the preliminary geotechnical appraisal include the following (Dickenson et al 2002):

- soil nature, soil fabric and structure (the nature of soil and the method of deposition and compaction have a significant influence on liquefaction resistance)
- depth to ground water table and saturation of soils
- density of soils (it is the most important factor governing the liquefaction resistance of a cohesionless soil)
- geologic age (or time under a sustained overburden) can significantly increase the liquefaction resistance of soils overtime
- prior cyclic load history (prior seismic excitation may or may not increase liquefaction resistance; more recent seismic excitation causing full or nearly full liquefaction does not increase and may actually reduce liquefaction resistance of soils)
- over consolidation (this can increase liquefaction resistance)
drainage characteristics (the ability to rapidly dissipate excess pore pressures, which is a function of the permeability of the soil and the drainage boundary conditions imposed by the surrounding soils, affects the liquefaction resistance)

effective confining stress (resistance to cyclic pore pressure generation and/or liquefaction increases with increased effective confining stress).

presence of non-liquefied crust (the crust reduces liquefaction manifestation and ground distortion near the surface)

grain size and particle grading.

Sands and sandy soils that are loose to medium dense or even dense can be potentially liquefiable. Sandy soils with fines content greater than 50% and a plasticity index (PI) of greater than 12% are generally considered to be non-liquefiable. The influence of fine-grained soil on the liquefaction resistance of predominantly sandy soils is a topic that has received considerable attention over the past decade. Examination of fine-grained soil behaviour during strong earthquakes and the results of laboratory tests reveal that uniformly graded loose sandy soils and even silty soils that contain over 30% non-plastic to low plasticity fines may be highly liquefiable (Dickenson et al 2002).

Gravelly soils and rock fills can also have a potential for liquefaction. A large number of case studies confirm that gravelly soils can liquefy. Most coarse, gravelly soils are relatively free draining. However, if the voids are filled with finer particles, or the surrounded soils have low permeability, then drainage may be insufficient and liquefaction may occur. When gravel layers are of considerable thickness and lateral extent, pore pressures may not be able to dissipate and this may also result in liquefaction. Case studies have shown that most liquefied gravelly soils are mixtures of sands, gravels and fines.

A more detailed discussion on liquefaction potential of soils is included in chapter 4 of this report.

In assessing the potential presence of liquefiable soil types, investigations should extend to a depth below which liquefiable soils cannot be reasonably expected to occur. Field evidence, as observed in Kobe and Loma Prieta earthquakes, has shown that liquefaction may occur to depths of up to 20m. In Japan liquefaction below 20m depth is not considered. It is important to consider the maximum possible depth of liquefaction, and effect of liquefaction at depth while deciding the required depth of geotechnical testing.

Liquefaction resistance can be roughly correlated with geologic age, depositional environment and prior seismic history. Generally, geologically young natural sandy formations are most susceptible to liquefaction. Such deposits can be found in offshore, coastal or floodplain areas when deposits are formed by the soil particles settling through water and coming to rest in a very loose state (Dickenson et al 2002). This means that the latest Holocene deposits, typically related to the natural drainage network, are most susceptible to liquefaction. Deposits older than late Pleistocene are assumed to be not susceptible to liquefaction, based on their performance during earthquakes. In various regions of New Zealand liquefaction hazard maps have been developed by local authorities based on local general geology data complemented by recent borehole and cone penetration test (CPT) information and can be used for preliminary geotechnical appraisal purposes.

Soils exhibiting high liquefaction susceptibility can be produced by hydraulic filling methods, where a cohesionless material is placed by dumping through water or as part of a pumped slurry (this is a very common method for construction of reclamation fills and embankments).

In order to be susceptible to liquefaction, soil should be saturated. If it can be demonstrated that soils present at a site are currently unsaturated, have not recently been saturated, and/or cannot reasonably be expected to become saturated for a significant length of time during the design life of a structure founded
on these materials, then such soils may be considered to pose no liquefaction hazard (Dickenson et al 2002). Preliminary site evaluations should identify the possibility of high groundwater tables. Layers of liquefiable soils that are very loose over sufficient area can represent hazardous planes of weakness and sliding. Where lateral containment is provided to eliminate potential for sliding on liquefied layers, the thin liquefiable zones at depth may be considered to pose no significant risk.

If a preliminary geotechnical appraisal evaluation can clearly demonstrate the absence of a liquefaction hazard at a project site, then no geotechnical investigations to identify potential for liquefaction may be required.

If the preliminary geotechnical appraisal indicates the presence of potentially liquefiable soils, then the potential of these soils for liquefaction (or significant loss of strength due to cyclic loading) should be evaluated and geotechnical investigations should be carried out. If the preliminary geotechnical appraisal does not eliminate the possibility of liquefaction at a project site, then geotechnical investigations are required.

It should be noted that investigations to assess liquefaction potential of soils normally form part of overall geotechnical investigations for a project. Therefore investigations for liquefaction should be scoped and carried out as part of the overall geotechnical investigations for a project.

3.2 Geotechnical site investigations

The geotechnical site investigation should identify and characterise the subsurface conditions and all geological hazards (including liquefaction and lateral spreading hazards) that may affect the seismic analysis and design of the proposed structures. The goal of the site characterisation for seismic design is to develop the subsurface profile and obtain soil property information needed for liquefaction assessment and for seismic analyses. Both the geotechnical designer and the structural designer should be involved in scoping geotechnical investigations, as seismic design is a combined effort between the geotechnical and structural disciplines.

While scoping geotechnical investigations, in accordance with Oregon State Department of Transportation (2012) Geotechnical design manual, volume 1, the geotechnical designer should:

• identify potential geologic hazards, areas of concern (eg deep, soft soils or liquefiable soils) and potential variability of local geology
• develop good understanding of possible structural forms of the required bridge and approximate level of structural loads
• carry out preliminary consideration of ground conditions, possible forms of the bridge foundations and of the required maximum depth of boreholes and CPTs
• identify engineering analyses to be performed (eg ground response analysis, liquefaction susceptibility, susceptibility to cyclic mobility, lateral spreading/slope stability assessments, seismic-induced settlement/down drag, dynamic earth pressures)
• identify engineering soil/rock properties required for these analyses
• determine methods to obtain the required design parameters and assess the validity of such methods for the soil and rock material types
• develop an integrated investigation programme for in-situ testing, soil sampling and laboratory testing. This should include the number of samples needed and appropriate locations and sampling techniques to obtain them, as well as appropriate test methods.
The following test techniques should be considered depending on site conditions (Oregon State Department of Transportation 2012):

- boreholes and cone penetration tests with associated testing, as described below
- standard penetration tests (SPTs) in boreholes – SPT test data is used for the assessment of liquefaction potential of soils
- SPT hammer energy: this value (usually termed hammer efficiency) should be noted on the boring logs or in the geotechnical report. The hammer efficiency should be obtained from the hammer manufacturer, preferably through field testing of the hammer system used to conduct the test. This is needed to determine the hammer energy correction factor for liquefaction analysis
- grading tests (including wet sieving) on soil samples to determine the liquefaction potential
- laboratory testing including Atterberg limit tests, specific gravity, organic content, water content, unit weight and shear box tests
- shear wave velocity measurements to determine subsoil class, develop a shear wave velocity profile for the soil layers and to assess low strain shear modulus values to use in analyses such as dynamic soil response
- seismic piezocone penetrometer to determining soil site class, develop a shear wave velocity profile and obtain low strain shear modulus values to use in a ground response analysis
- piezocone penetrometer test for liquefaction analysis. Pore pressure measurements and other parameters can be obtained for use in foundation design and modelling. This test is also useful in establishing the pre-construction subsurface soil conditions prior to conducting ground improvement techniques and the post-construction condition after ground improvement
- depth to bedrock should be established. If a ground response analysis is to be performed the depth to bedrock must be known
- pressure meter tests can be useful for development of p-y curves. Testing is typically performed in soft clays, organic soils, very soft or decomposed rock and for unusual soil or rock materials. The shear modulus, G, for shallow foundation modelling and design can also be obtained
- static or cyclic plate load tests
- static or cyclic screw plate load tests
- in-situ testing of seismic behaviour of soils by subjecting the soils to cyclic loading using a large scale in-situ cyclic loading test where cyclic loading is generated by a truck-based vibration machine (TRex or similar)
- dilatometer tests
- field trials using explosives to confirm liquefaction potential of soil
- at a later stage of the design process, the need for ground improvement field trials (to prove effectiveness of proposed method of ground improvement) should be considered.

Geotechnical reports that address liquefaction and lateral spreading hazards at bridge sites should include the following information (California Geological Survey 2008):

- if methods other than the SPT and CPT are used, a description of equipment and testing procedures
- borehole logs showing detailed soil and rock description in accordance with NZGS (2005) *Guideline for the field classification and description of soil and rock for engineering purposes* and SPT N-values if SPTs are performed (SPTs should be carried out using calibrated hammers so that the hammer energy ratio or hammer efficiency is known)
- CPT logs showing plots of cone resistance and sleeve friction values if CPTs are performed (CPT equipment should be in current calibration and electrical cones checked for zeroing error at the end of each CPT profile)
- explanation of the basis of the methods used to convert raw SPT, CPT or non-standard test data to corrected values
- tabulation and/or plots of corrected values used for analyses
- explanation of methods used to develop estimates of the cyclic stress ratios used to represent the anticipated field earthquake excitation
- explanation of the basis for evaluation of the cyclic stress ratio necessary to cause liquefaction at the number of equivalent uniform loading cycles considered representative of the design earthquake
- factors of safety against liquefaction at various depths and/or within various potentially liquefiable soil units
- description of assessment methods used and conclusions regarding the potential for liquefaction and lateral spreading and likely deformation and its likely impact on the proposed project
- preliminary discussion of proposed mitigation measures necessary to reduce potential damage caused by liquefaction to an acceptable level of risk; detailed recommendations should be developed as a part of the detailed design process
- criteria for SPT-based, CPT-based, or other types of acceptance testing that will be used to demonstrate satisfactory quality of ground improvement, if applicable.
4 Evaluation of liquefaction and lateral spreading

4.1 Introduction

Past large-scale earthquakes have demonstrated that bridges and ancillary components (abutments, approach fills, embankments and pile foundations) located at sites of shallow groundwater and/or adjacent to bodies of water are highly susceptible to liquefaction-induced damage. In order to prevent and/or minimise such damage, there is a need to evaluate the liquefaction potential at the site, and to predict the associated ground deformations in order to evaluate how they affect the bridge structures.

The evaluation of soil liquefaction and its effects involve several steps, from determining the seismic demand at the site to evaluating liquefaction susceptibility, liquefaction triggering and liquefaction-induced deformations. These steps may involve either simplified or detailed analysis procedures. This section provides guidelines on how these steps are conducted.

4.2 Determination of seismic demand

Evaluation of liquefaction potential of sandy deposits is usually performed for a certain specified level of shaking, typically described by a design ground motion, which can be characterised by design ground motion parameters. For geotechnical earthquake engineering, the amplitude (the largest value of acceleration recorded during the earthquake, represented by peak ground acceleration (PGA) and duration of shaking (which can be related to earthquake magnitude) are the key input parameters to most common design procedures, with no direct consideration of the frequency (represented by the response spectrum). These input parameters can be evaluated for a target site using code-based approaches or by site-specific seismic hazard/response analysis.

It is recommended that determination of the seismic demand at bridge sites follow recommendations of the Bridge manual, where the PGA to be applied shall be ‘unweighted’ and derived for the relevant return period. Similarly, the earthquake magnitude is also derived for the relevant return period.

An alternative method is that recommended by the Geotechnical earthquake engineering practice: module 1 – guideline for the identification, assessment and mitigation of liquefaction hazards (NZGS 2010) where two methods of defining the seismic demand are described. These are based on the provisions of design standards (ie NZS 1170.5: 2004) and on site-specific analyses (seismic hazard analysis and ground response analysis).

4.3 Evaluation of liquefaction

Evaluation of liquefaction generally involves the following steps:

1. Liquefaction susceptibility:
   a. Are the soils at the site liquefiable or not?

2. Triggering of liquefaction:
   a. Is the ground motion of the adopted ‘design earthquake’ strong enough to trigger liquefaction at the site?
3 Consequences of liquefaction:
   a If liquefaction does occur, what will be the extent and magnitude of resulting ground deformation?

4 Effects of liquefaction on structures:
   a What will be the effect of liquefaction on the seismic performance of structures?

5 Mitigation of liquefaction and its consequences:
   a Determine an acceptable level of performance and if liquefaction-induced ground displacements are intolerable or the structure’s performance is below an acceptable level, then what countermeasures should be used against soil liquefaction?

This section focuses on liquefaction susceptibility and methods of analysis for assessment of liquefaction triggering. Evaluation of magnitude of ground deformation is discussed in section 4.4, while mitigation measures are addressed in chapters 5 and 7.

4.3.1 Liquefaction susceptibility

It is well known that sites consisting of loose cohesionless sediments (gravels, sands and very low-plasticity silts) and with sufficiently high water table for these sediments are susceptible to liquefaction. Thus, knowing the geology of the site in question and the nature and properties of the soils are a key component in determining whether the soils in that location are liquefiable or not. Several methods are available to evaluate liquefaction susceptibility of sites and these should be adopted as initial screening tools when assessing possible extent of liquefaction at specific sites.

4.3.1.1 Historical criteria

Liquefaction case histories are often used to identify specific sites, or more general site conditions, which may be susceptible to liquefaction in future earthquakes. Youd (1991) pointed out some case histories where susceptibility maps were developed based on historical evidence of liquefaction occurrence. Moreover, post-earthquake field investigations have shown that liquefaction occurrence has been confined within a zone of certain distance from the seismic source. Based on case histories, several investigators have plotted the maximum extent of liquefied sites as a function of the magnitude of the earthquake (eg Youd and Perkins 1978; Ambraseys 1988). Hence, if the seismic activity at the target site is known, the maximum extent of liquefaction susceptible area can be directly estimated.

4.3.1.2 Geological and geomorphological criteria

Correlations between past liquefaction occurrences and geological and geomorphological criteria can also be used to identify sites susceptible to liquefaction. The depositional environment, hydrological environment and age of soil deposit all contribute to its liquefaction susceptibility (Yould and Hoose 1977). Based on the study by Youd and Perkins (1978), sediments most susceptible to liquefaction are fills and alluvial, fluvial, marine, deltaic and wind-blown deposits. In addition, recently deposited sediments are most susceptible to liquefaction, becoming more resistant when they become older.

4.3.1.3 Compositional criteria

Compositional characteristics associated with high volume change potential, such as particle size, shape and gradation, tend to be associated with high liquefaction susceptibility (Kramer 1996). Uniformly graded soils have higher volume change potential therefore, tend to build up pore pressure more readily than well-graded soils. Based on this concept and on field evidence, the Japanese Ministry of Transport (MTJ 1999) has proposed a zone expressed in terms of grain size distribution separating potentially liquefiable
soils from fine-grained soils which are not vulnerable to liquefaction. Subsequent studies however suggest that even finer soils than those proposed possessed a high degree of potential to liquefaction if the fines are non-plastic. Moreover, well-graded reclaimed fills containing 30%-60% gravels, well beyond the zones proposed, liquefied following the 1995 Kobe (Japan) earthquake. The NZGS guidelines (NZGS 2010) stated that based on current knowledge, grading criteria alone are not a reliable indicator of liquefaction susceptibility.

In the NCEER Workshop recommendations (Youd et al 2001), there is no specific mention of the liquefaction potential of silts and clay and the so-called Chinese criteria ‘might be applied’ to verify the soil type and whether the soil is liquefiable or not. However, the use of these criteria has been discouraged in US practice (Boulanger and Idriss 2004a) and assessment of liquefaction susceptibility of fine-grained soils have been proposed based on recent studies (eg Bray et al 2004; Boulanger and Idriss 2006; Anderson et al 2007). The NZGS (2010) guideline for the identification, assessment and mitigation of liquefaction hazards gives more information on this issue.

4.3.2 Liquefaction triggering

Several approaches and methods have been proposed for assessing the potential for liquefaction triggering. The most widely used method has been the stress-based approach that compares the earthquake-induced cyclic stresses with the cyclic resistance of the soil. A simplified procedure based on the empirical method originally proposed by Seed and Idriss (1971) is recommended for assessing the potential for liquefaction triggering.

In general, the evaluation of liquefaction potential requires the following:

- estimation of the maximum or equivalent cyclic shear stress likely to be induced in the soil deposit during an earthquake (seismic demand)
- quantitative assessment of liquefaction resistance, or cyclic resistance ratio (CRR) (seismic capacity).

4.3.2.1 Seismic demand

The simplified procedure developed by Seed and Idriss (1971) provides an easy approach to estimate earthquake-induced cyclic shear stresses without the need for a site response analysis. The cyclic shear stress ratio (CSR) is as follows:

\[ CSR = \frac{\tau_{\text{ave}}}{\sigma'_{v0}} = 0.65 \frac{a_{\text{max}}}{g} \frac{\sigma_{v0}}{\sigma'_{v0}} \cdot r_{d} \]  

(Equation 4.1)

Where

- \( \tau_{\text{ave}} \) = equivalent uniform or average cyclic shear stress
- \( \sigma'_{v0} \) = effective overburden stress
- \( \sigma_{v0} \) = total overburden stress
- \( a_{\text{max}} \) = peak horizontal ground acceleration generated by the earthquake
- \( g \) = acceleration due to gravity
- \( r_{d} \) = stress reduction factor which takes into account the flexibility of the soil column.

This equation has remained largely unchanged from its original form. The stress reduction factor, initially presented graphically by Seed and Idriss (1971) as a function of depth, has been subsequently refined by various researchers to incorporate the effects of other parameters such as earthquake magnitude, acceleration and soil shear wave velocity. Typical forms of \( r_{d} \) equations are presented by Liao and Whitman...
Evaluation of liquefaction and lateral spreading


4.3.2.2 Resistance to liquefaction

The dynamic stress the soil can withstand before liquefying is defined in terms of the CRR. The recommended method of characterising the liquefaction resistance is based on in situ tests because of the disturbance inherent in the sampling and laboratory testing of cohesionless soils. In the simplified procedure, the CRR of the in-situ soil is primarily based on empirical correlations to the SPT, CPT or shear wave velocity ($V_s$) measurements. These empirical correlations have been developed from case history databases of liquefied and non-liquefied soils documented in previous earthquakes.

SPT-based liquefaction triggering procedures use SPT blow count ($N$) as the basis of computing CRR. Typical SPT-based CRR relationships were developed by various researchers, such as Youd et al (2001), Cetin et al (2004) and Idriss and Boulanger (2008). In recent years, however, the CPT has become more common as an in situ test for liquefaction evaluation, especially as the database of case histories grows and its simplicity, repeatability and accuracy, not to mention that it provides a continuous record. CPT-based CRR correlations have been proposed by Robertson and Wride (1998), Moss et al (2006) and Idriss and Boulanger (2008). When the economics of a project permit, the combination of SPTs and CPTs may offer a very reliable way to evaluate the liquefaction susceptibility. $V_s$ can also be used to evaluate the liquefaction potential of soils. Essentially, the procedure is similar to other penetration-based approaches, and the boundary curves separating liquefaction and non-liquefaction obtained by various researchers are presented in Youd et al (2001). Note that although liquefaction potential evaluation is typically conducted deterministically, there are also probabilistic methods available. For example, the methods by Cetin et al (2004), Moss et al (2006) and Kayen et al (2013) also assess liquefaction occurrence probabilistically by considering relevant uncertainties such as: measurement/estimation errors, model imperfection, statistical uncertainty, and those arising from inherent variables. A probability of liquefaction (PL) of 15% is generally adopted when using these methods for deterministic liquefaction evaluation.

These empirical charts are expressed in terms of $CRR_{7.5, 1\text{ atm}}$ (ie the cyclic resistance ratio of the soil adjusted to 1 atmosphere of effective overburden pressure for $M_w=7.5$ earthquake). Note that the various relationships use different factors to account for earthquake magnitude and overburden stresses. It is common for CRR relationships to be normalised for this base case, and then site-specific adjustments are made via magnitude scaling factors (MSF) and overburden correction factors ($K_\sigma$) to account for the earthquake magnitude under consideration and the overburden stresses at the depth of interest. The site adjusted CRR is obtained from $CRR_{7.5, 1\text{ atm}}$ according to the following equation:

$$CRR_{M, \sigma, \text{cr}} = CRR_{7.5, 1\text{ atm}} \cdot MSF \cdot K_\sigma$$

(Equation 4.2)

The adjustment for magnitude is necessary because of the strong correlation between CRR and the number of loading cycles the earthquake imparts to the soil. The most commonly used expressions for MSF as a function of magnitude have been proposed by Youd et al (2001), Cetin et al (2004) and Idriss and Boulanger (2008).

The overburden correction factor ($K_\sigma$) is used to extrapolate liquefaction triggering relationships to high overburden pressures. Typical expressions of $K_\sigma$ were proposed by Seed and Harder (1990), Hynes and Olsen (1999) and Boulanger and Idriss (2004b).

It should be mentioned that the various liquefaction triggering procedures cannot be compared solely on CRR plots. For example, even if the CRR relationships appear to be very similar, one would not necessarily obtain the same CRR value for a given raw penetration data ($N$-value or tip resistance) because the factors
used to correct the raw data to the penetration index (e.g., normalised clean sand N-value, \(N_{(1)}\) or normalised clean sand tip resistance, \(q_{u,cs}\)) can vary significantly between relationships. Thus, in the same way as the \(r_a\)-values discussed above, each CRR relationship should only be used within its recommended procedure.

### 4.3.2.3 Factor of safety

Liquefaction susceptibility is usually expressed in terms of a factor of safety against its occurrence, i.e.

\[
F_L = \frac{CRR}{CSR}
\]  
(Equation 4.3)

If \(F_L < 1.0\), the shear stress induced by the earthquake exceeds the liquefaction resistance of the soil and therefore, liquefaction is likely to occur. Otherwise, when \(F_L \geq 1.0\), liquefaction will not be likely to occur. Note that this boundary is well understood to be not a distinct line and that engineering judgement needs to be applied to evaluate the liquefaction susceptibility of soils with \(F_L\) near unity.

### 4.4 Liquefaction-induced ground deformations

The significant reduction in stiffness and strength of liquefied soils may result in the development of large shear strains in the ground during and following intense ground shaking. The maximum cyclic shear strains can easily reach several percent in liquefying soils in level ground, resulting in large lateral displacements or ground oscillations. These large cyclic lateral movements are important to consider because they may generate significant kinematic loads on buried structures and deep foundations. Moreover, in the presence of driving stresses or unconstrained boundaries (such as free-face near river banks), the liquefied soil can undergo permanent lateral ground deformations as large as several metres in some cases.

Following the liquefaction process, the soil deposit undergoes a very complex process involving dissipation of excess pore water pressure, sedimentation, solidification and re-consolidation of the liquefied soil resulting in settlement of the ground. These liquefaction-induced settlements occur during and after the earthquake shaking and can be significant even for free-field level-ground sites.

#### 4.4.1 Ground settlements

Several methods have been developed for estimating the magnitude of earthquake-induced settlements in sandy soils. One of the most widely adopted methods is that developed by Ishihara and Yoshimine (1992), who produced a design chart relating volumetric strain (\(\varepsilon_v\)) in sandy soils to soil density (\(D\)) and the factor of safety against liquefaction (\(F_L\)). It should be noted that because this procedure was developed for clean sands, a correction is required for silty sands and silts. The method has been extended by Zhang et al. (2002) for use with CPT data.

Another procedure for estimation of soil densification and related settlements was developed by Tokimatsu and Seed (1987), where the volumetric strains \(\varepsilon_v\) induced by earthquake shaking are expressed as function of the corrected SPT N-value \((N_{(1)}\) and cyclic shear stress ratio caused by the earthquake. The chart was developed for clean sands and for magnitude 7.5 earthquakes, and therefore correction factors are required for soils with more than 5% fines content, and for earthquakes of magnitude other than 7.5.
4.4.2 Cyclic ground displacements

The empirical procedure proposed by Tokimatsu and Asaka (1998) can be used for a preliminary assessment of cyclic ground displacements in liquefied soils. Similar to the chart developed by Tokimatsu and Seed (1987) for estimating volumetric strain, this procedure is based on an empirical chart correlating the maximum cyclic shear strain $\gamma_{cyc}$ in liquefied soil with the SPT N-value $(N)_{60}$ and cyclic shear stress ratio caused by the earthquake.

4.4.3 Permanent ground displacement due to spreading

Prediction of lateral ground displacements is a difficult geotechnical problem. Even though the prediction of whether a site will liquefy or not can be done with a reasonable degree of confidence, there is no generally accepted method for evaluating lateral displacements. Current methods can generally be classified into four categories.

4.4.3.1 Empirical approaches

The most widely adopted methods for estimating lateral spread displacement are empirically based procedures developed using extensive databases from case studies where measured displacements are correlated with site-specific topographic, geotechnical, and ground motion data. These include the empirical equations formulated by Bartlett and Youd (1995) and Youd et al (2002) using a multiple linear regression (MLR) analysis to take into account a great number of variables in a predictive equation for horizontal displacements. Other available procedures include the empirical equations proposed by Bardet et al (2002) and the EPOLLs model of Rauch and Martin (2000). Note that the predicted response from MLR models may be strongly nonlinear outside the range of the data used to derive the regression coefficients, and caution is warranted when extrapolating beyond the intended range of parameters.

4.4.3.2 Semi-empirical approaches

These procedures involve estimating the permanent (or residual) shear strains that are expected within the liquefied zones and integrating those strains over depth to estimate the potential lateral displacement at the ground surface. The residual shear strains are estimated using charts developed from laboratory tests and the computed ground displacement is then sometimes empirically modified to take into account case history observations (eg Tokimatsu and Asaka 1998; Shamoto et al 1998; Zhang et al 2004).

4.4.3.3 Analytical methods

The empirical and semi-empirical methods are developed to evaluate lateral displacements at free-field sites and these conditions severely limit their application for bridge sites with embankments and site-specific configurations. In these cases, these approaches can be used only as approximate indicators of lateral spread hazard, and supplementary analysis procedures are required. A common method of analysis is through rigid body mechanics, such as the sliding-block method proposed by Newmark (1965). In this method, the soil is assumed to behave as a rigid, perfectly plastic material and the yield acceleration is calculated using simple limit equilibrium stability analysis. The movement of the slope (earth structure) is then calculated either by integrating a given acceleration time history over the range of accelerations exceeding the yield level or by using approximate equations developed from analyses based on a suite of earthquake records. Additional information is given by Jibson (2007) and Olson and Johnson (2008).

4.4.3.4 Advanced numerical modelling

For applications involving preliminary screening of liquefaction hazards at bridge sites, a high degree of accuracy is not required. Therefore the empirical and semi-empirical methods are adequate and can be conservatively applied. If lateral spreading hazards are indicated, then more sophisticated analyses may be warranted. Advanced numerical modelling procedures, which make use of non-linear effective stress
Constitutive models and are implemented through finite element or finite difference methods provide useful tools in estimating lateral spreading displacements. Key advantages of these procedures are: 1) complex geometries and soil profiles can be evaluated; 2) sensitivity studies can be made to determine the influence of various parameters on the magnitude of lateral deformation; and 3) dynamic soil behaviour is more realistically reproduced. On the other hand, disadvantages of these techniques include: 1) the engineering time required to construct the numerical model can be extensive; 2) substantial geotechnical data is required which may not be available for many projects; and 3) very few of the available models have been validated with well documented case studies and the level of uncertainty in the analysis is often unknown.

These methods are discussed further in appendix A.4.3. The choice of the method(s) to be used for a particular site depends on the information available and the level of details required for the project. For most projects, however, the semi-empirical approach of estimating permanent strains from SPT/CPT data and expressing them as lateral displacement index (LDI) has been the preferred approach. A benefit of the integration of strain method is that an estimate of the soil displacement profile is obtained over the depth of the foundation, which can in turn be used as an analysis input. However, care must be taken when implementing this method because it does not account for two- or three-dimensional effects and therefore, the results for individual borings can be misleading on their own.

Many liquefaction assessment studies have been conducted in Christchurch making use of the Canterbury Geotechnical Database. For example, Lees et al (2013) used the three CPT-based methods mentioned above (Robertson and Wride 1998; Idriss and Boulanger 2008; Moss et al 2006) to estimate the liquefaction potential index (LPI) at 1400 sites and compared them with the observed damage. They showed that the three CPT-based methods adequately assessed liquefaction triggering in Christchurch and the LPIs calculated were effective estimates of the damage observed at the ground surface. Based on their study, the factor of safety obtained from the Moss et al (2006) method showed the best correlation.
5 Methods of ground improvement

5.1 Introduction

To reduce the risk of damage to bridges due to soil liquefaction, remediation methods through ground improvement and/or structural enhancement shall be employed. In this report, only ground improvement techniques are addressed. Ground improvement, whose goal is to limit soil deformations to acceptable levels, is being used increasingly for remediating liquefiable soils due to the wide variety of available methods.

5.2 Types of ground improvement

Ground improvement methods are generally based on one or more of the following principles: 1) densification; 2) solidification; 3) drainage; 4) reinforcement and containment and 5) soil replacement. Table 5.1 summarises the most common liquefaction countermeasures. Brief descriptions of the principles behind the improvement mechanism associated with each category are provided below, along with some references detailing the design of ground treatment schemes and methods to evaluate the effectiveness of soil improvement. Further details concerning the specific treatment methods can be found in references on ground improvement (eg Cooke and Mitchell 1999; Andrus and Chung 1995; Xanthakos et al 1994; Hausmann 1990; JGS 1998; PHRI 1997; Schaefer 1997).

5.2.1 Densification methods

Densification or compaction methods involve re-arranging the soil particles into tighter configuration, resulting in increased density. This increases the shear strength and liquefaction resistance of the soil, and encourages a dilative instead of a contractive dynamic soil response. Densifying sandy soil with vibration and/or impact has been used extensively, making it the most popular liquefaction countermeasure.

Vibro-compaction methods such as sand compaction piles, have been used to increase the density of granular soils. Several case studies of Japanese earthquakes have shown the effectiveness of the method in treating liquefiable soils (eg Yasuda et al 1996; Harada et al 2012).

The use of vibro-replacement methods such as stone columns for densification, drainage and strengthening, are popular in the US. The design of stone column applications for liquefaction mitigation has been described by Baez and Martin (1992), Baez (1995) and Boulanger et al (1998).

Dynamic compaction (or heavy tamping) involves repetitively dropping a large weight onto the ground causing the soil grains to form a denser arrangement. The drop height, weight and spacing vary, depending on ground and groundwater conditions. Lukas (1986; 1995) has provided the most widely quoted and referenced documents on dynamic compaction.
Table 5.1 Liquefaction countermeasure techniques

<table>
<thead>
<tr>
<th>Method</th>
<th>Principle</th>
<th>Most suitable soil conditions/types</th>
<th>Maximum effective treatment depth</th>
<th>Relative costs</th>
</tr>
</thead>
</table>
| 1  Vibrotary probe         | Densification by vibration; liquefaction-induced settlement and settlement in dry soil under overburden to produce a higher density. | Saturated or dry clean sand; sand.                | • 20m routinely (ineffective above 3m–4m depth  
• >30m sometimes  
• 40m. | Moderate         |
| a  terraprobe             |                                                                          |                                                   |                                   |                |
| b  vibrorods              |                                                                          |                                                   |                                   |                |
| c  vibrowing              |                                                                          |                                                   |                                   |                |
| 2  Vibro-compaction       | Densification by vibration and compaction of backfill material of sand or gravel. | Cohesionless soils with less than 20% fines.       | >20m                              | Low to moderate|
| a  vibrofloat             |                                                                          |                                                   |                                   |                |
| b  vibro-composer system  |                                                                          |                                                   |                                   |                |
| 3  Compaction piles       | Densification by displacement of pile volume and by vibration during driving, increase in lateral effective earth pressure. | Loose sandy soil; partly saturated clayey soil; loess. | >20m                              | Moderate to high|
| 4  Heavy tamping (dynamic compaction) | Repeated application of high-intensity impacts at surface. | Cohesionless soils best, other types can also be improved. | 10m (possibly deeper) | Low            |
| 5  Displacement (compaction grout) | Highly viscous grout acts as radial hydraulic jack when pumped in under high pressure. | All soils.                                          | Unlimited                        | Low to moderate|
| 6  Surcharge or buttress   | The weight of a surcharge/ buttress increases the liquefaction resistance by increasing the effective confining pressures in the foundation. | Can be placed on any soil surface.                 | Dependent on size of surcharge/ buttress | Moderate if vertical drains are used|
| 7  Drains                  | Relief of excess pore water pressure to prevent liquefaction (wick drains have comparable permeability to sand drains). Primarily gravel drains; sand/wick may supplement gravel drain or relieve existing excess pore water pressure. Permanent dewatering with pumps. | Sand, silt, clay.                              | Gravel and sand >30m; depth limited by vibratory equipment; wick >45m | Moderate to high|
| a  gravel                 |                                                                          |                                                   |                                   |                |
| b  sand                   |                                                                          |                                                   |                                   |                |
| c  wick                   |                                                                          |                                                   |                                   |                |
| d  wells (for permanent dewatering) |                                                                 |                                                   |                                   |                |
| 8  Particulate grouting   | Penetration grouting – fill soil pores with soil, cement, and/or clay.   | Medium to coarse sand and gravel.                 | Unlimited                        | Lowest of grout methods|
| 9  Chemical grouting       | Solutions of two or more chemicals react in soil pores to form a gel or a solid precipitate. | Medium silts and coarser.                        | Unlimited                        | High           |
| 10 Pressure injected lime | Penetration grouting – fill soil pores with lime.                        | Medium to coarse sand and gravel.                | Unlimited                        | Low            |
5 Methods of ground improvement

<table>
<thead>
<tr>
<th>Method</th>
<th>Principle</th>
<th>Most suitable soil conditions/types</th>
<th>Maximum effective treatment depth</th>
<th>Relative costs</th>
</tr>
</thead>
<tbody>
<tr>
<td>11 Electrokinetic injection</td>
<td>Stabilising chemical moved into and fills soil pores by electro-osmosis or colloids in to pores by electrophoresis.</td>
<td>Saturated sands, silts, silty clays.</td>
<td>Unknown</td>
<td>Expensive</td>
</tr>
<tr>
<td>12 Jet grouting</td>
<td>High-speed jets at depth excavate, inject and mix a stabiliser with soil to form columns or panels.</td>
<td>Sands, silts, clays.</td>
<td>Unknown</td>
<td>High</td>
</tr>
<tr>
<td>13 Mix-in-place piles and walls</td>
<td>Lime, cement or asphalt introduced through rotating auger or special in-place mixer.</td>
<td>Sands, silts, clays, all soft or loose inorganic soils.</td>
<td>&gt;20m (60m obtained in Japan)</td>
<td>High</td>
</tr>
<tr>
<td>14 Vibro-replacement stone and sand columns</td>
<td>Hole jetted into fine-grained soil and backfilled with densely compacted gravel or sand hole formed in cohesionless soils by vibro-techniques and compaction of backfilled gravel or sand. For grouted columns, voids filled with a grout.</td>
<td>Sands, silts, clays.</td>
<td>&gt;30m (limited by vibratory equipment)</td>
<td>Moderate</td>
</tr>
<tr>
<td>15 Root piles, soil nailing</td>
<td>Small-diameter inclusions used to carry tension, shear and compression.</td>
<td>All soils</td>
<td>Unknown</td>
<td>Moderate to high</td>
</tr>
<tr>
<td>16 Blasting</td>
<td>Shock waves and vibrations cause limited liquefaction, displacement, remoulding and settlement to higher density.</td>
<td>Saturated clean sand; partly saturated sands and silts after flooding.</td>
<td>&gt;40m</td>
<td>Low</td>
</tr>
</tbody>
</table>

In *compaction grouting*, cement-sand grout is injected into the soil under high pressure. The grout bulb displaces the surrounding soil outwards, thereby increasing soil density. Recent case studies on liquefaction applications of compaction grouting have been described by Orense (2008) and Russell et al. (2008). Moreover, a consensus guide has been published by ASCE (2010).

### 5.2.2 Solidification method

Increase in liquefaction resistance can also be obtained through a more stable skeleton of soil particles. This can be achieved by solidification methods, which involve filling the voids with cementitious materials resulting in the soil particles being bound together.

Typical methods include deep mixing and pre-mixing. The *deep mixing method* achieves liquefaction remediation by mixing a stabilising material such as cement in sandy soil and solidifying the soil. Such a method is applicable even for foundation ground beneath an existing structure. The *pre-mixing method*, on the other hand, involves adding stabilising material to the soil in advance and placing the treated soil at the site. This is recommended for constructing new reclaimed land. References on the application of these methods include Francis and Gorski (1998), Bruce (2000) and CDIT (2002).

*Chemical grouting* is a technique that transforms granular soils into sandstone-like masses, by permeation with a low viscosity grout. Typically, a sleeve port pipe is first grouted into a predrilled hole. The grout is
injected under pressure through the ports located along the length of the pipe. The grout permeates the soil and solidifies it into a sandstone-like mass. The grouted soil has increased strength and stiffness, and reduced permeability.

5.2.3 Drainage

Excess pore water pressure generated by cyclic loading can be reduced and/or dissipated by installing a permeable drain within the deposit. The gravel drain and plastic drain methods are representative examples. In the installation of gravel drains, casing with an auger inside is drilled into the ground down to the specified depth. Crushed stone is then discharged into the casing and the gravel drain is formed by lifting the casing pipe. A plastic drain, on the other hand, consists of a plastic perforated pipe drainage skeleton wrapped in geofabric to prevent clogging from soil particles. These can be easily installed; however, close spacing is usually required due to the limited capacity of each drain.

5.2.4 Reinforcement

When saturated sand deposits are sheared during seismic loading, excess pore water pressure is generated. To prevent the occurrence of liquefaction, the soil should undergo smaller shear deformation during earthquake. This can be achieved by underground diaphragm walls. This method simply surrounds the liquefiable soil with continuous underground wall and thus it can be used for the soil at the bottom of existing structures where liquefaction remediation is difficult with other methods.

The presence of stone columns, CFA or timber piles and other stiff elements provide additional shear resistance against earthquake shaking. These reinforcements would take much of the earthquake load, thereby minimising the shear deformation of the soil.

5.2.5 Soil replacement

The remove and replace method is another liquefaction mitigation technique. This involves the removal of the in situ liquefiable material, and replacement with a non-liquefiable material such as clay, gravel or dense sand. However, this method is only feasible when relatively small volumes of liquefiable material are involved at shallow depths.

5.2.6 Increasing in situ stress

In situ effective stresses within the soil mass can be increased, resulting in an increase in shear resistance. Pre-loading involves over-consolidating the soil with a surcharge embankment. This method is applicable to soils with large fines content and can also be applied below existing structures since the soil can be over-consolidated by lowering the ground water table. Lowering the groundwater table makes the soil above the water table unsaturated, resulting in increased effective stress for soils below the water table. For this method, it is always necessary to maintain the lower ground water level, and this may result in a high operating cost.

5.2.7 Applications of ground improvement in New Zealand

Various liquefaction countermeasure techniques have been implemented in New Zealand. Some of the methods include:

- partial replacement
- stone columns (vibro-displacement and vibro-replacement)
- vibro-compaction and vibro-roller
5 Methods of ground improvement

- compaction grouting
- reinforcement (CFA or timber piles)
- jet grouting
- deep soil mixing
- heavy tamping.

Some of these methods were tested following the 2010–2011 Christchurch earthquake sequence. (Wotherspoon et al (2014) summarised the main findings regarding the performance of these improved sites and noted that there were still liquefaction-related ground failure and/or intolerable settlements that occurred at some facilities due to the following reasons:

- ground shaking exceeding the design levels
- some sites contained liquefiable silty strata that were not effectively densified during treatment, resulting in liquefaction of the soil in-between the stone columns
- some ground improvement works (like stone columns) did not extend through the entire liquefiable layer, meaning that liquefaction occurred in the soil layers beneath the base of the treated zone.

Moreover, except for some of the sites within 10km away from the earthquake epicentres, most of the sites improved in Christchurch were subjected to very low PGAs and were not sufficiently tested.

5.3 Costs of ground improvement

The cost associated with each ground improvement method is affected by the size and location of the zone to be improved, the type of treated zone, degree of improvement required, local soil conditions, groundwater conditions, contractor and equipment availability and geographic location. Figure 5.1 indicates the approximate relative costs of improvement.

Figure 5.1 Relative cost of soil improvement based on Japanese experience (after JGS Kanto 2013).

Key: SCP = sand compaction pile; DM = deep mixing
5.4 Reliability and resilience

Ground improvement methods to mitigate liquefaction-induced ground deformations have been widely implemented over the past several decades, and case histories have indicated their performance. There is clear historical evidence from events as far back as the 1964 Niigata earthquake and most recently the devastating 2011 East Japan earthquake that improved sites suffer less ground deformation and subsidence than adjacent, unimproved areas (e.g., Yasuda et al. 1996; Hausler and Sitar 2001; Harada et al. 2012).

Recent large earthquakes significantly helped in extending the level of information available relative to the effectiveness of ground improvement. The available case histories clearly indicate that ground improvement leads to a significant reduction, if not elimination, of large ground displacements during seismic loading. However, some case histories show a set of circumstances in which ground improvement may not effectively eliminate ground deformation, such as the use of conventional densification methods in the presence of a severe lateral spreading hazard, or an inadequate remediation zone depth or lateral extent. For example, Hausler and Sitar (2001), compiled over 90 case histories on the performance of improved sites from 14 earthquakes in Japan, Taiwan, Turkey, and the US covering a wide range of improvement methods. The collected data indicated that improved sites generally performed well but about 10% of the surveyed sites required significant post-earthquake remediation, repair, or demolition. Table 5.2 indicates the number of acceptable and unacceptable sites in their database. Without additional consideration of soil type, construction procedures and treatment ratio, this statistic must be taken at face value.

Table 5.2 Performance of various ground improvement methods in the database (Hausler and Sitar 2001)

<table>
<thead>
<tr>
<th>Method</th>
<th>Performance (acceptable/unacceptable)</th>
<th>Average increase in N1.60</th>
</tr>
</thead>
<tbody>
<tr>
<td>Densification through vibration and compaction</td>
<td>26/5</td>
<td>77</td>
</tr>
<tr>
<td>Sand compaction piles</td>
<td>15/0</td>
<td>5</td>
</tr>
<tr>
<td>Deep dynamic compaction</td>
<td>11/6</td>
<td>13</td>
</tr>
<tr>
<td>Vibro-rod/vibro-floatation</td>
<td>7/1</td>
<td>8</td>
</tr>
<tr>
<td>Stone columns</td>
<td>5/0</td>
<td>5</td>
</tr>
<tr>
<td>Preloading</td>
<td>1/1</td>
<td>n/a</td>
</tr>
<tr>
<td>Compaction grouting</td>
<td>1/0</td>
<td>n/a</td>
</tr>
<tr>
<td>Timber displacement piles</td>
<td>1/0</td>
<td>n/a</td>
</tr>
<tr>
<td>Dissipation of excess pore water pressure</td>
<td>5/0</td>
<td>7</td>
</tr>
<tr>
<td>Gravel drains</td>
<td>5/0</td>
<td>9</td>
</tr>
<tr>
<td>Sand drains</td>
<td>2/0</td>
<td>n/a</td>
</tr>
<tr>
<td>Wick or paper drains</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Restraining effect through inclusions</td>
<td>4/1</td>
<td>n/a</td>
</tr>
<tr>
<td>Deep soil mixing</td>
<td>0/1</td>
<td>n/a</td>
</tr>
<tr>
<td>Diaphragm walls</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Stiffening through chemical or cement addition</td>
<td>5/0</td>
<td>n/a</td>
</tr>
<tr>
<td>Jet grouting</td>
<td>1/0</td>
<td>n/a</td>
</tr>
<tr>
<td>Chemical grouting</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
5.5 Generic design recommendations

5.5.1 Design guidelines

The design of soil mitigation strategies involves investigating the cost-benefit ratio, the seismic performance and the effect of the mitigation technique(s) on adjacent structures.

Some design guidelines for each of these remediation categories are briefly discussed below. More in-depth discussions on the design of soil mitigation strategies and procedures are available in the literature, such as PHRI (1997) and JGS (1998).

Densification or compaction methods are more suitable for use in saturated, cohesionless soils with a limited percentage of fines. They cause noise and vibration during installation, and also increase horizontal earth pressures against adjacent structures. This increase in pressure is the major disadvantage of using compaction methods in close proximity to retaining walls and pile foundations. The major advantage of compaction methods is the relatively low cost-benefit ratio. The necessary degree of compaction can be evaluated using penetration resistances that have been back-calculated from an acceptable factor of safety against liquefaction.

Drainage remediation methods are suitable for use in sands, silts or clays. One of the greatest advantages of drains is that they induce relatively small horizontal earth pressures during installation. Therefore, they are suitable for use adjacent to sensitive structures. In the design of drains, it is necessary to select a suitable drain material that has a coefficient of permeability substantially larger than the in situ soils.

Cementation techniques can be used with any type of soil. They are advantageous because the installation methods are relatively quiet and induce relatively small vibrations compared with compaction methods. The induced horizontal earth pressures are smaller than with compaction methods, and are larger than with drainage methods. Their disadvantage is the relatively high cost-benefit ratio compared with compaction and drainage methods.

The influence of ground treatment on existing structures is a primary design consideration. The construction methods may lead to increased horizontal earth pressures, which can result in deformations of embankments, walls and pile foundations. Mitigation methods also may induce excess pore pressures and vibration, which will affect sloping embankments and retaining structures. Therefore, a mitigation strategy design may include the combination of two or more improvement techniques in order to take advantage of robust treatment methods in free-field areas and less disturbing methods close to existing structures. In general, compaction techniques have the largest impact on adjacent structures, followed by controlled cementation techniques, and then drainage methods which generally are the least disruptive.

5.5.2 Design issues

Several factors influence the stability and deformation of improved ground zones and supported structures during and after an earthquake. These factors include size, location and type of treated zone (Mitchell et al 1998).

Generally, even when the soil undergoes liquefaction over a wide area, the area requiring soil improvement is limited to the area which controls the stability of the structure. For example, the portion of the subsoil which contributes to the stability of shallow spread foundations is that directly below and on the perimeter of the structure; the portion of the subsoil far away from the structure does not contribute to the stability of the shallow foundation.
Design guidance for bridges in New Zealand for liquefaction and lateral spreading effects

The region for soil improvement should be determined in both horizontal and vertical directions. For the vertical direction, it is usual practice to improve the ground to the deepest part of the liquefiable layer. If only the shallow portion is improved, the excess pore water pressure generated at the bottom of the unimproved soil if it liquefies may induce upward seepage towards the surface, resulting in potential instability in the upper improved zone. As for the lateral extent of treatment necessary, this is dependent on the type of remediation measure employed and the allowable deformation the structure can undergo. This can be investigated by performing detailed analysis, and if possible, supplemented by model tests. In many cases, the lateral extent of treatment beyond the edge of the structure is a distance equal to the depth of treatment beneath the structure.

6 Pore pressure migration

The difference in stiffness between a densified zone of material and the surrounding loose liquefiable material could result in seepage between these two materials during and after earthquakes. Larger excess pore water pressure is developed in the untreated material, resulting in propagation into the improved soil. Although the influence of pore pressure migration into a dense material is very complex, it may nevertheless lead to strength loss of the densified soil.

7 Ground motion amplification

Due to the increase in stiffness, improved ground may result in increase in ground motion, and this may be detrimental to the structure on top of it. Although little information is available regarding the influence of the size of improved ground and its stiffness on ground motions, engineers should consider a balance in design so the size and stiffness of the improved ground would result in acceptable deformations and accelerations of the structure during an earthquake.

8 Dynamic fluid pressure

During earthquake shaking, the movement of the improved ground zone within the liquefied soil may result in a dynamic component of fluid pressure to act on improved ground, in addition to the static fluid pressure. These forces must be considered for stability and deformation of structure supported in the improved zone.

9 Inertia force

Inertia forces acting on the improved soil mass should be included when evaluating the stability of an improved ground zone supporting a structure. Note however, that the phasing between inertia forces acting on the improved ground and supported structure may be different and this can have significant impact on the results of simplified stability and deformation analyses.

10 Influence of structure

The presence of structure built on top of an improved ground will alter the stress-state within the said zone and can affect the dynamic response and stress-strain behavior of the improved soil.

11 Forces exerted by laterally spreading soil

Liquefaction-induced lateral ground movements have been observed to occur at sites with slopes less than 1%. Therefore, the improved ground should be adequately designed to resist the forces induced by the laterally moving ground. There are two force components that should be considered: first, the load exerted by the moving liquefied ground itself; and second, the force exerted by the unliquefied surficial crust riding on top of the liquefied ground.
6 Methods of analysis

6.1 Introduction

This chapter discusses state-of-the-practice and state-of-the-art methods for the analysis of bridges (and their subsystems) in liquefying and lateral spreading soils. In particular, it covers the simplified pseudo-static method of analysis, advanced dynamic analysis, and the substructure method of analysis, with particular focus on their application to bridges in liquefying and laterally spreading soils.

6.1.1 Characteristics of liquefaction and lateral spreading

The key characteristics of earthquake-induced soil liquefaction and lateral spreading can be summarised as follows:

- Excess pore water pressures (EPWP) builds up very quickly during strong ground shaking. Hence, under strong earthquake excitation, the soils may liquefy within a relatively short period of time (within 5 to 20 seconds of strong shaking). The rate of EPWP build-up depends on the ground motion characteristics (the amplitude and duration of strong shaking or number of significant cycles), liquefaction potential of soils, and site characteristics including soil stratification, permeability of soils and drainage conditions.

- The stiffness and strength of the liquefying soil reduce dramatically over the 5 to 20 seconds of rapid EPWP build-up and change from their initial high stiffness and strength values to post-liquefaction residual values of very low stiffness and strength. These rapid and drastic changes in the stress-strain characteristics of liquefying soil are illustrated in figure 6.1 where the initial stress-strain curve (figure 6.1a), a slightly degraded stress-strain curve (figure 6.1b), and a post-liquefaction stress-strain curve (figure 6.1c) exhibiting nearly zero stiffness and strength (horizontal segments of the $\tau-\gamma$ curve) are shown together with the associated EPWP time history (figure 6.1d). Full liquefaction (or zero effective stress condition) occurs when the excess pore water pressure reaches the initial effective overburden stress $\sigma'_{vo}$.

- The stress-strain curves in figure 6.1 clearly indicate that cyclic (transient) ground displacements (readily obtained by integrating the shear strains over the depth of the deposit) gradually increase during the rapid EPWP build-up from stage a to stage c. The maximum cyclic ground displacements may occur during the pore pressure build up, at the onset of liquefaction or slightly after the occurrence of liquefaction.

- Lateral spreading of liquefied soils is generally associated with two ground configurations: a) sloping ground, and b) flat or sloping ground close to a free face (river banks, waterfront and backfills behind revetment structures). Lateral spreading has been observed even in very gentle slopes of a few degrees only.

- While lateral ground displacements associated with spreading may initiate during the pore pressure build-up, most of the large spreading displacements occur after the onset of liquefaction. Hence, majority of the gravity driven lateral spreading displacements occur post-liquefaction or after a substantial loss of strength and stiffness in the liquefied soils has occurred. Post-liquefaction stiffness and strength values could be much lower than the stiffness and strength of the soil corresponding to the cyclic phase of the response (ie during the shaking and pore water pressure build-up).

- Inertial loads due to strong shaking (vibration of the superstructure) are significant during the cyclic phase (development of EPWPs); however, these loads could largely diminish post-liquefaction due to
the reduced capacity of liquefied soils to transfer shear stresses. This effect of reduction in acceleration amplitudes (shear stresses) post-liquefaction could be particularly pronounced in very loose sandy soils, but it could be negligible or even reversed in dense soils exhibiting acceleration spikes due to cyclic mobility or temporary dilation during cyclic loading. As significant spreading is normally associated with loose soils, a post-liquefaction reduction in the inertial loads during the spreading appears to be a more realistic scenario. In the evaluation of effects of liquefaction and laterals spreading on bridges, it is important to adopt a consistent scenario with compatible values for the magnitude of ground displacements, soil stiffness and strength, and inertial loads. For example, very large ground displacements (indicating low stiffness and strength of soils) are incompatible with very high accelerations which are associated with relatively high (strain-hardening) stiffness and dilation during cyclic mobility.

- Soil liquefaction and lateral spreading are highly variable and non-uniform phenomena both in time and space involving large masses of soils, dynamic interaction of various layers throughout the depth of the deposit, intense pore water pressure redistribution and significant seepage forces in addition to the complex mechanism of pore pressure build up previously described. Also refer to section 5.2.2 in this report.

Figure 6.1  Schematic illustrations of changes in the shear stress – shear strain relationship of the soil at different stages of pore pressure development (Haskell et al 2012)

6.1.2 Design cases to consider

Clearly the stiffness and strength of liquefying soils, their stress-strain behaviour, and consequent ground accelerations (inertial loads) and ground displacements (kinematic loads) are very different during the cyclic phase (during the shaking and development of excess pore water pressures) and post-liquefaction. As illustrated in figure 6.2, the cyclic phase is characterised by a rapidly changing stiffness and strength of the soil due to the decreasing effective stresses, and simultaneous action of cyclic ground displacements and cyclic inertial loads on the pile foundation. Because of the very short duration (about several tens of seconds or less), this phase of the response is associated with undrained behaviour in sandy soils. The cyclic displacements in the liquefied soils would generally correspond to maximum shear strains in the range between 1% and 4%. In other words, a fully liquefied 10m thick deposit will generate peak-to-peak cyclic horizontal displacements at the ground surface of about ± 200mm to ± 800mm.
Methods of analysis

The post-liquefaction lateral spreading phase is associated with residual or post-liquefaction stiffness and strength of the liquefied soils and consequent large ground deformation. Gravity-driven spreading displacements may continue after the end of shaking or until equilibrium is re-established in the soil masses across the depth of the deposit and lateral spreading area. This post-liquefaction phase often results in fissuring and cracking of the ground, significant water flow and seepage action, loss of integrity of the crust due to sand boils and ejecta, dissipation of excess pore pressures, re-solidification and re-consolidation of the soil, and large permanent ground displacements. The inertial loads during spreading are generally much smaller than the corresponding loads during the cyclic phase.

When evaluating the effects of liquefaction and lateral spreading on the performance of the bridge (e.g., pile foundations) using equivalent static analyses, it is necessary to conduct separate analyses for different stages of the response. The following phases in the response need to be considered in the performance evaluation of pile foundations:

- Cyclic analysis without liquefaction, in which inertial loads that would occur in the absence of liquefaction are considered.
- Cyclic liquefaction analysis, estimating the potential and consequences of liquefaction, and considering simultaneous kinematic loads (due to cyclic ground displacements) and structural inertial loads while accounting for stiffness and strength degradation of the soils due to excess pore water pressures.
- Lateral spreading analysis, estimating the potential for liquefaction and consequences of lateral spreading including substantial stiffness and strength degradation, and kinematic loads due to large spreading displacements. Inertial loads may be considered in this analysis, but as discussed previously, such loads are of secondary importance in the spreading phase, and could be ignored in many cases.

For example, the design specifications for highway bridges in Japan (JRA 1996; Tamura 2013), the AIJ code for piled building foundations in Japan (AIJ 2001; Tokimatsu and Asaka 1998) and the Pacific Earthquake Engineering Research (PEER) recommended design practice (Ashford et al 2011) for pile foundations of bridges in laterally spreading soils consider separate equivalent static analyses for different phases of the response.
6.1.3 Local and global effects (models and analysis)

Effect of liquefaction and lateral spreading could be evaluated by considering a single member (e.g., a single pile), a subsystem of the bridge (pile group, pier piles or piled abutment, or the whole bridge (figure 6.3). Each of these models is acceptable in the evaluation of the bridge performance provided that proper boundary conditions and modelling assumptions are used, and that there is a clear understanding of the analysis objectives and limitations. The cyclic response should be considered both in the transverse and longitudinal directions, whereas the lateral spreading response is commonly considered in the longitudinal direction of the bridge.
6.1.4 Methods of analysis

Several methods are available for analysis of bridges and piles in liquefied soils, ranging from simplified methods using an equivalent static approach to a rigorous time history analysis based on the effective stress principle. These methods can be summarised into three general approaches:

1. Pseudo-static analysis (PSA) or equivalent static analysis.

2. Direct dynamic time history analysis including: a) effective stress analysis (ESA) considering effects of excess pore pressures and liquefaction through detailed constitutive modelling, and b) total stress analysis (TSA), dynamic analysis using total stresses or equivalent stresses and either ignoring excess pore pressures or considering them in a simplified manner. In the direct method of analysis (ESA and TSA), the response of the whole soil-pile-pier-abutment-deck system can be considered over the entire period of time from the initiation of shaking to the final stage of post-earthquake equilibrium and residual deformation of the bridge, in a single analysis. More complex dynamic analyses are typically used for more important structures and where details of dynamic soil-foundation-structure-interaction are required. ESA also provides the best currently available tool for evaluation of the effectiveness of mitigation measures against liquefaction.

3. Substructure analysis methods which use some features of PSA, ESA or TSA but are essentially hybrid approaches tailored to address specific aspects in the performance assessment. For example, the well-known Newmark-type analysis, a simplified user-defined time history analysis, would be a typical representative of this group of methods. The substructure method uses a set of separate but related analyses to assess the performance of a bridge subsystem.

While all these analysis methods are used to assess the seismic performance of the pile foundation and the bridge, these different methods focus on different members/subsystems and aspects of the problem and provide different and distinct contributions to the assessment of seismic performance (Cubrinovski and Bradley 2009). Table 6.1 summarises key features, advantages, shortcomings and modelling requirements of the methods.
Table 6.1 Methods for analysis of effects of liquefaction and lateral spreading on bridges

<table>
<thead>
<tr>
<th>Method</th>
<th>Key features</th>
<th>Advantages</th>
<th>Shortcomings</th>
<th>Model types, and key requirements</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pseudo-static analysis</td>
<td>• Static analysis&lt;br&gt;• Beam-spring model&lt;br&gt;• Decoupled kinematic and inertial loads&lt;br&gt;• Separate cyclic liquefaction and lateral spreading analyses&lt;br&gt;• Separate liquefaction triggering analysis</td>
<td>• Conventional data and engineering concepts&lt;br&gt;• Relatively simple to use&lt;br&gt;• Evaluates the response and damage to piles (for a range of ground conditions and loads – parametric study)</td>
<td>• Gross approximation of dynamic loads and behaviour&lt;br&gt;• Large uncertainties in soil spring parameters, kinematic and inertial loads&lt;br&gt;• Dynamic interaction/response is not considered&lt;br&gt;• Aims at maximum response only</td>
<td>Single pile&lt;br&gt;• Pile group&lt;br&gt;• Whole bridge&lt;br&gt;• Should address uncertainties through parametric analyses</td>
</tr>
<tr>
<td>Seismic effective stress analysis</td>
<td>• Dynamic (time history) analysis&lt;br&gt;• Finite element model including soil-pile-abutment-pier-superstructure&lt;br&gt;• Two phase soil (solid and fluid phases), effective stresses, pore pressures and fluid flow are considered</td>
<td>• Most realistic numerical simulation of liquefaction effects on the bridge response&lt;br&gt;• Best method to evaluate effectiveness of mitigation measures&lt;br&gt;• Accurate modelling of the stress-strain behaviour of soil and consequent ground deformation&lt;br&gt;• Provides direct feedback to the bridge designer for effects of liquefaction on the bridge (the designer can ‘see’ features that could not be anticipated)&lt;br&gt;• Response and damage to piles, subsystems&lt;br&gt;• Enhances communication of design between geotech and structural engineers</td>
<td>• Complex numerical procedure; difficult to use, and relatively expensive&lt;br&gt;• High demands on the user (requires in depth understanding of numerical procedures, constitutive model and liquefaction phenomena/effects&lt;br&gt;• It is not practical to conduct large number of time history analyses; consequently, uncertainties in the ground motion and numerical model cannot be addressed (in practical applications)</td>
<td>Pier, pier piles (transverse direction)&lt;br&gt;• Whole bridge (longitudinal direction)&lt;br&gt;• Understanding limitations of the model/ procedure&lt;br&gt;• Good constitutive model, and competent user</td>
</tr>
<tr>
<td>Total stress analysis</td>
<td>• Dynamic (time history) analysis&lt;br&gt;• Finite element model&lt;br&gt;• Single phase soil (solid)</td>
<td>• Dynamic interaction is considered&lt;br&gt;• Accurate modelling of the stress-strain behaviour of soil and ground deformation in absence of liquefaction&lt;br&gt;• Provides feedback to the bridge designer for</td>
<td>• Ignores (oversimplifies) effects of EPWP and key features of liquefaction&lt;br&gt;• Complex numerical procedure; difficult to use; relatively expensive</td>
<td>Pier, pier piles (transverse direction)&lt;br&gt;• Whole bridge (longitudinal direction)&lt;br&gt;• Understanding limitations of the model/ procedure&lt;br&gt;• Competent user</td>
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6 Methods of analysis

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| Substructure approach (eg Newmark-type analysis) | • Dynamic (time history) analysis  
• Three separate analyses: i) liquefaction triggering, ii) stability (critical or yield acceleration), iii) PSA | some aspects of dynamic response                                            | • High demands on user  
• Uncertainties in the ground motion and numerical model ignored            | • Abutment, abutment piles, embankment (longitudinal direction)  
• Understanding limitations of the models/procedures  
• Competent user |

### 6.2 Pseudo-static analysis (PSA)

The PSA approach is carried out based on nonlinear equivalent static analysis of a relatively simple beam-spring model is used for the soil-pile-bridge system. The approach is also referred to as the ‘beam on Winkler foundation’ (Boulanger et al 2007; Ashford et al 2011) or ‘static pushover analysis’ (Brandenburg et al 2007). Several methods for PSA of piles in liquefying soils are available (eg Tokimatsu and Asaka 1998; Cubrinovski and Ishihara 2004; Cubrinovski et al 2009b; Brandenburg et al 2007; Ashford et al 2011). These methods are similar in concept but differ in the modelling details and analysis procedures. All PSA methods are burdened by significant uncertainties arising from the fact that a highly complex dynamic soil-structure interaction problem involving liquefying soils is represented by a simplified model and an equivalent static analysis. Nevertheless, the approach has been proven to be very useful, and therefore is the backbone approach in many of the seismic codes for the design of piled foundations of bridges and buildings.

Two approaches are generally used for PSA of piles subjected to lateral spreading: a force-based approach and a displacement-based approach. These approaches differ in the way in which the lateral load on pile due to ground movement is considered in the analysis.

In the force-based approach, an equivalent static load representing the pressure from the laterally spreading or cyclically moving soil is applied to the pile, as an input load. For a typical three-layer configuration with a liquefied layer sandwiched between a non-liquefied surface crust and a non-liquefied base layer, the lateral earth pressures from the crust and liquefied layer are first estimated and then applied as lateral loads to the pile, pushing the pile in the direction of spreading (figure 6.4a).

One serious deficiency of the force-based approach is that it ignores the fact that the lateral load on the pile (magnitude of the mobilised lateral soil pressure on the pile) depends on the relative displacement between the soil and the pile; hence, the lateral load depends on the pile displacements. In other words, one cannot estimate the lateral load on the pile due to ground movement, if pile displacements along the length of the pile are not known.
The displacement-based approach offers a more rigorous modelling compatible with the mechanism of soil-pile interaction. As shown in figure 6.4b, in the displacement-based approach lateral ground displacements representing the free-field ground movement are applied at the free end of soil springs attached to the pile. In this case, the forces that develop in the soil springs are compatible with the relative displacement between the soil and the pile, and hence, the mobilised lateral soil pressure is fully compatible with the induced pile response. For this reason, the displacement-based approach is the preferred method for PSA. Figure 6.5 illustrates possible pile responses resulting in different relative displacements between the pile and free-field ground movements, ranging from stiff pile response in which the pile resists the ground movement to very flexible pile response in which the pile practically moves together with the ground.

The key requirements for the simplified PSA can be summarised as follows:

1. The adopted model and analysis method must capture the relevant deformation mechanism for piles in liquefying/spreading soils.
2. The analysis should permit estimating the inelastic response and damage to piles.
3. The method should allow for uncertainties associated with liquefaction and lateral spreading. It is important to conduct parametric study, identify the key parameters affecting the pile response and
assess the effects of the uncertainties on the pile response. Cubrinovski et al (2009b) and Ashford et al (2011) methods make this parametric evaluation a key requirement for PSA, whereas many other codes remain mute on this issue, or stipulate fixed factors, loads and resistances for practical reasons and easier application.

4 Separate analyses should be conducted for the cyclic phase and post liquefaction phase of the soil-pile interaction. This has been adopted in many of the codes (AIJ, JRA, PEER) and proposed PSA procedures (Tokimatsu and Asaka 1998; Cubrinovski et al 2009b; Ashford et al 2011; Tamura 2013).

5 In addition to the single-pile analysis, effects of pile groups, boundary conditions, and deck-pinning effects should be considered with appropriate models and analyses. The use of global bridge PSA can be very effective in the analysis of the soil-pile-abutment-superstructure system (Ashford et al 2011; Cubrinovski et al 2014).

Based on our review of available PSA methods, the following PSA methods would be appropriate for New Zealand conditions:

- Cubrinovski et al method (Cubrinovski et al 2009b)
- PEER method (Ashford et al 2011)

These two methods are described below. In addition we provide a brief description of two more PSA methods:

- AIJ method (Tokimatsu and Asaka 1998)
- JRA method (JRA 1996)

The Cubrinovski et al method is first presented in detail, and then the other methods are presented and discussed with reference to this method, pointing out their distinctive characteristics in the modelling and analysis procedures.

6.2.1 Cubrinovski et al method

This PSA method can be applied either to a single-pile, pile group or the whole bridge. For clarity, the single pile model is first used in the detailed description of the method and then additional requirements for pile group and whole bridge analyses are given.

6.2.1.1 Analysis procedure

The key steps in the simplified pseudo-static analysis procedure are listed below.

Step 1: Site and soil characterisation

Step 2: Determine earthquake load at the bridge site

Step 3: Liquefaction triggering analysis

Step 4: Formulate beam-spring model

Step 5: Estimate soil spring parameters

Step 6: Estimate pile M-φ parameters

Step 7: Estimate free-field ground displacements

Step 8: Estimate inertia loads

Step 9: Conduct PSA with best-estimate parameters
Step 10: Conduct parametric (sensitivity) study

Step 11: Estimate pile group effects

Step 12: Consider geometric non-linearity, soil-foundation-structure interaction (SFSI) and 3-D effects

A more detailed summary of the key steps is given at the end of this section.

6.2.1.2 Computational model

The typical beam-spring model representing the soil-pile system in the analysis is shown in figure 6.6. The model can easily incorporate a multi-layered deposit with liquefied layers of different thickness and location in the deposit, a crust of non-liquefiable soil at the ground surface, and deeper non-liquefiable layers including base layers at the tip of the pile. Parameters of the model are summarised in figure 6.6 for a typical configuration in which liquefied layers are sandwiched between a surface layer and a non-liquefiable base layer of non-liquefiable soils.

Soil properties

- Multi-layered deposit is considered including both liquefied and non-liquefied layers.
- A non-liquefiable layer at the ground surface (crust) is defined by the depth to the water table, presence of non-liquefiable soils (e.g., clayey soils with I<sub>c</sub> > 2.6 or stiff gravels) or a combination of both.
- Soil properties are determined using conventional field parameters such as SPT blow count or CPT resistance; effects of fines and plasticity of fines could be considered in the same way as in the simplified liquefaction triggering analysis.

Given that a key requirement of the analysis is to estimate the inelastic deformation and damage to the pile, the proposed model incorporates simple but non-linear load-deformation relationships for the soil and the pile. The soil is represented by bilinear (elastic-plastic) springs, the stiffness and strength of which can be degraded to account for effects of nonlinear behaviour and liquefaction.

Soil springs

- Bi-linear soil springs are used.
- Two parameters define the spring: stiffness and strength which is related to the ultimate pressure from the soil on the pile.
- Both stiffness and strength can be degraded due to effects of liquefaction or/and soil nonlinear load-deformation characteristics.
- Spring spacing should be preferably 0.1m and not larger than 0.2m.
The pile is modelled with a series of beam elements each having a tri-linear moment-curvature relationship. Bilinear, multi-linear or nonlinear $M-\phi$ relationships could be also used. Commonly available software and finite element programs can be employed for the beam-spring model and analysis.

**Beam elements (pile modelling)**
- The pile is modelled with a series of beam elements; the length of the beam elements should be equal to the spring spacing (i.e., preferably 0.1 m and not larger than 0.2 m).
- The load-deformation characteristics of each beam element are defined by a moment-curvature ($M-\phi$) relationship; the $M-\phi$ relationship may change throughout the length of the pile in accordance with changes in pile properties.
- The soil springs are attached to the nodal points of the beams.
- Translational and rotational fixity (boundary) conditions should be defined at the top and tip of the pile, with fixed rotation at the pile head (due to rigid connection of the piles with the cap), fixed translation at the tip of the pile, and free rotation at the tip of the pile are most commonly used boundary conditions.

**Pile properties**
- Tri-linear (or bilinear) moment-curvature ($M-\phi$) relationship for the pile is used.
- For a reinforced concrete (RC) pile, the tri-linear relationship indicates threshold levels of concrete cracking (C), yielding of reinforcement (Y) and ultimate state at concrete crushing (U).
- The $M-\phi$ relationship should be defined for the appropriate axial loads acting on the pile, pre-stress levels, pile geometry, reinforcement and concrete characteristics. Accurate $M-\phi$ relationships are critical for the evaluation of the pile response and damage.
In the model, two equivalent static loads can be applied to the pile: a lateral force at the pile head \( F \) representing the inertial load on the pile due to vibration of the superstructure, and a horizontal ground displacement \( U_G \) applied at the free end of the soil springs representing the kinematic load on the pile due to lateral ground movement (cyclic or spreading) in the free field. As indicated in figure 6.6, it is assumed that all of the ground surface displacement is accommodated within the liquefied layer, that the non-liquefied crust at the ground surface moves as a rigid body and undergoes the same ground displacement as the top of the liquefied layer, \( U_G \), and that the non-liquefying base layers are not moving.

### Ground displacement (kinematic loads)
- Liquefaction triggering analysis is carried out first to identify the layers that will liquefy for a given earthquake load, i.e., a certain level of PGA and Mw (refer to section 4.3.2).
- Free field displacements at the ground surface should be estimated separately for the transient (cyclic) phase and lateral spreading phase (refer to section 4.3.1).
- Once liquefied layers have been identified, liquefaction-induced lateral displacements can be estimated throughout the depth of the profile using simplified liquefaction or lateral spreading analysis; for example, free-field liquefaction-induced transient (cyclic) ground displacements in level ground free field can be estimated using the method of Tokimatsu and Asaka (1998). The methods of Zhang et al (2004) and Youd et al (2002) can be used to estimate free-field lateral spreading displacements. It should be noted that estimates of liquefaction and spreading-induced displacements are burdened by significant uncertainties, and these uncertainties should be accounted for by conducting parametric analyses of bridge structures using a range of different magnitudes of applied ground displacements (section 4.4).
- Ground displacement profile is then estimated based on the above calculations.
- The adopted ground displacements are applied at the free end of the soil springs to calculate the deformation of the pile due to ground displacements (kinematic loads).
- The crust moves as a rigid body on top of the underlying liquefied layer; the base non-liquefied layer does not move.
- The designers should also consider negative skin friction on the piles resulting from settlement of liquefied soil and non-liquefied crust, appropriate down-drag loads should be considered in the design if required.

### Vibration of the superstructure (inertial loads)
- An estimate for the dynamic response of the bridge is needed, in particular, what would be the peak horizontal acceleration response or spectral acceleration.
- A portion of this acceleration can be used to calculate the equivalent horizontal static force. This force can be applied at the top of the pile considering the total number of piles, and distribution of the total inertial load on the piers, abutments and their piles.
- A combined ground displacement (kinematic load) and inertial load should be applied for the transient (cyclic) phase of the response. Inertial loads may or may not be considered in the lateral spreading analysis, at the discretion of the engineer.
6 Methods of analysis

Analysis results

- Lateral displacement of the pile throughout its length at every nodal point.
- Bending moment (curvature) along the length of the pile at every nodal point.
- Distributed lateral load on pile along the length of the pile, at every nodal point.
- Damage to the pile is estimated from comparison between computed curvature and threshold $M-\phi$ levels (C, Y, U) along the pile length.

6.2.1.3 Model parameters

The key issue in the implementation of any PSA is how to select appropriate values for the soil stiffness, strength and lateral loads applied to the pile in the equivalent static analysis. In other words, what are the appropriate values for $\beta$, $P_{\text{max}}$, $U_g$ and $F$ in the model shown in figure 6.6. This section provides recommendations on determination of the beam-spring model parameters.

The first important distinction of the Cubrinovski et al method is the use of bilinear soil springs instead of nonlinear $p$-$y$ curves, typical for US practice. Bilinear rather than non-linear springs are used because the uncertainties associated with the stiffness and strength of liquefied soils are so large that they completely override the benefits of nonlinear spring modelling. To illustrate this point, we can consider the pressure-displacement ($p$-$\delta$) relationship for a soil spring of laterally spreading soil shown in figure 6.7. Here, $p$ is the pressure applied from the soil on the pile, and $\delta$ is the relative displacement between the soil and the pile ($\delta = U_g - U_p$), at a given depth $z$, where $U_g$ is the free-field ground displacement. The shaded area in the figure indicates the range of possible variation in the stiffness (degradation factor of 1/50 to 1/1000) and the strength (factor of 1/3 to 2) of the spring. The very large possible variation in the stiffness and strength of the spring clearly shows that the focus in the assessment should be on covering the uncertainty in stiffness and strength rather than on the shape of the curve between the initial slope and ultimate pressure level of the $p$-$\delta$ relationship. It is important to note that the use of non-linear $p$-$y$ curves in liquefaction PSA in the US is actually a by-product of the historical development of $p$-$y$ curves, which were first developed for non-liquefiable soils, and were then adopted for simplified liquefaction analyses. In fact, the shape of the conventional $p$-$y$ curves is not always compatible with the shape of the stress-strain curve of liquefying soils, such as those shown in figure 6.1 (Ashford et al 2011).

Bi-linear vs nonlinear soil spring

- There are significant uncertainties in the stiffness and strength of liquefied soils and, hence, soil spring properties.
- Rather than modelling the nonlinearity in detail, it is important to consider the large uncertainties in the stiffness and strength of liquefied soils and their effects on the pile response, thorough a systematic parametric study.
- The bi-linear model satisfies the requirements for parametric PSA.
In this method, the concept of stiffness and strength degradation has been adopted for the liquefied soils (or even non-liquefied soils), as illustrated conceptually in figure 6.8. Strictly speaking, soil behaviour suggests that the degradation factor should be different for the stiffness and strength, or in other words, the yield threshold ($\delta_u$) should not be the same for the non-degraded and degraded bilinear relationships. The basis for this reasoning is illustrated in figure 6.9 where experimental correlation between the threshold displacements required to fully mobilise the passive pressure ($\delta_u$) and the relative density of soil ($D_r$) is shown. The results show much larger $\delta_u$ values for loose soils (low $D_r$ values) as compared to dense soils. For example, $\delta_u = 2\%$ to $7\%$ of $H$ for $D_r = 85\%$ while $\delta_u = 12\%$ to $18\%$ of $H$ for $D_r = 40\%$. Here, $H$ is either the thickness of the crust (in pile experiments) or height of the wall (in wall experiments).

In the Cubrinovski et al method, the degradation of stiffness and strength has been derived based on experimental and case studies evidence resulting in different degradation factors for the stiffness and strength of liquefied soils. Note that some degradation can also be adopted for the non-liquefied soil springs to simulate effects of excess pore pressures or to achieve target relative displacements at the full mobilization of the passive pressure, as indicated by the test results in figure 6.9.

Figure 6.7  Illustration of wide range of variation in the $p$-$\delta$ relationship for a laterally spreading liquefied soil and associated uncertainties in stiffness and strength of the soil spring

In the Cubrinovski et al method, the degradation of stiffness and strength has been derived based on experimental and case studies evidence resulting in different degradation factors for the stiffness and strength of liquefied soils. Note that some degradation can also be adopted for the non-liquefied soil springs to simulate effects of excess pore pressures or to achieve target relative displacements at the full mobilization of the passive pressure, as indicated by the test results in figure 6.9.

Figure 6.8  Generalised bi-linear soil spring model (non-degraded vs degraded stiffness and strength)
6.2.1.4 Soil spring parameters

The bilinear elastic-plastic soil spring parameters are estimated as follows:

1. **Non-liquefied crust**

   The soil spring stiffness is given by:
   
   \[ K_C = k_C \cdot s \cdot D_0 \]  \hspace{1cm} (Equation 6.1)

   where \( K_C \) = spring stiffness, \( s \) = spring spacing, \( D_0 \) = pile diameter (width) in metres, and \( k_C \) = subgrade reaction coefficient given by:
   
   \[ K_C = 56 \cdot N \cdot (100D_0)^{-3/4} \]  \hspace{1cm} (MN/m³)  \hspace{1cm} (Equation 6.2)

   where \( N \) = SPT blow count. (uncorrected, as measured in the field, assumed to correspond to 60% energy efficiency, \( N_{60} \)).

   Other expressions for \( k_C \), based on soil moduli, can be also used. The spring stiffness can be degraded for the effects of nonlinearity (by a degradation factor of 0.3, 0.5 or similar) or based on a target \( \delta_u \) value from the correlation shown in figure 6.9.

   The yield force of the soil spring corresponding to the ultimate pressure from the soil on the pile is given by:
   
   \[ P_{C-max} = p_{c-max} \cdot s \cdot D_0 = \alpha_c \cdot P_p \cdot s \cdot D_0 \]  \hspace{1cm} (for non-cohesive soils)  \hspace{1cm} (Equation 6.3)

   \[ P_{C-max} = p_{c-max} \cdot s \cdot D_0 = 9 \cdot S_u \cdot s \cdot D_0 \]  \hspace{1cm} (for cohesive soils)  \hspace{1cm} (Equation 6.4)

   where \( p_{c-max} \) = yield strength of soil spring, \( P_p \) = Rankine passive pressure, \( s \) = spring spacing, \( D_0 \) = pile diameter (width), \( S_u \) = undrained strength, and \( \alpha_c \) = scaling factor accounting for the increased pressure on a single pile (due to 'wedge effect'), as compared to the Rankine pressure for an equivalent continuous wall (\( P_p \)).

   Cubrinovski et al (2009b) recommend use of:
   
   \[ \alpha_c = 4.5 \] as a reference value and \( \alpha_c = 3 \) lower-bound, and \( \alpha_c = 5 \) upper-bound values \hspace{1cm} (Equation 6.5)

   Note that \( \alpha_c = 1.0 \) is used for the springs connected to a pier or abutment (wall).

   The upper and lower bound values are based on the early work of Broms (1964); the reference value is based on benchmark experiments on piles in liquefying soils (Cubrinovski et al 2006).
2 Non-liquefied deeper soils

The soil spring parameters for deeper non-liquefied soils are determined using identical procedure as for the non-liquefied soils but with the following modifications:

\[ P_{B-max} = \alpha \cdot P_{p} \cdot s \cdot D_0 = 3 \cdot P_{p} \cdot s \cdot D_0 \] (for non-cohesive soils)  
(Equation 6.6)

Note: \( \alpha_c = 1.0 \) (instead of 3) could be also used, and is the preferred choice at larger depths; in some cases, this choice may affect both the displacement of the pile at the pile head and the peak bending moment at the soil interface at the base of the liquefied layer.

3 Liquefied soils

The soil spring parameters for liquefied soils are determined using similar procedure as for the non-liquefied soils but with the following modifications:

The spring stiffness is reduced by a degradation factor \( \beta_L \) and is given by:

\[ K_L = \beta_L \cdot k_L \cdot s \cdot D_0 \]  
(Equation 6.7)

in which \( K_L \) = spring stiffness, \( s \) = spring spacing, \( D_0 \) = pile diameter (width), \( k_L \) = subgrade reaction coefficient (Eq. 6.2) and \( \beta_L \) is defined as:

For cyclic loading:  
\[ \beta_L = 0.05 \] – reference value  
\[ \beta_L = 0.02 \] – lower bound value  
\[ \beta_L = 0.10 \] – upper bound value

For lateral spreading:  
\[ \beta_L = 0.01 \] – reference value  
\[ \beta_L = 0.001 \] – lower bound value  
\[ \beta_L = 0.02 \] – upper bound value  
(Equation 6.8)

The recommended ranges of values for \( \beta_L \) are based on back-calculations of case studies from the 1995 Kobe earthquake (Ishihara and Cubrinovski 1998a; Ishihara and Cubrinovski 1998b; Ishihara and Cubrinovski 2004) and benchmark liquefaction experiments on full-size piles (Cubrinovski et al 1999; Cubrinovski et al 2006).

The soil spring yield force is given by:

\[ P_{L-max} = \alpha_L \cdot S_r \cdot s \cdot D_0 \]  
(Equation 6.9)

In which \( P_{L-max} \) = yield strength of soil spring, \( s \) = spring spacing, \( D_0 \) = pile diameter (width), and \( S_r \) = residual strength of liquefied soil layer. \( \alpha_L = 1.0 \) is provisionally adopted as a lower bound and reference value; \( \alpha_L > 1.0 \) values could be also used in parametric evaluations.

\( S_r \) can be estimated using empirical correlations between \( S_r \) and SPT blow count \( N \) (Idriss and Boulanger 2008; Olson and Stark 2002; Seed and Harder 1990) or \( S_r \) and CPT resistance (Idriss and Boulanger 2008; Olson and Stark 2002), similar to those shown in figure 6.10. It is important to consider the uncertainty in the residual strength of liquefied soils in the analysis.
6.2.1.5 Pile moment-curvature parameters

Moment-curvature relationships should be determined for the particular diameter, cross-section dimensions and details, yield strength and threshold strains of materials, axial loads and pre-stress levels of the piles. The $M$-$\phi$ relationship(s) are critical input for the PSA, as they affect the pile response and consequent damage to the piles.

Pile properties

- Accurate determination of the moment-curvature relationship is critical in the assessment of the pile response and its damage.
- Use of simplified $M$-$\phi$ relationship such as tri-linear or bi-linear relationship identifying the threshold curvature levels (kink points in the relationship) is preferred for the PSA; For example, for a RC pile, concrete cracking (C), yielding of the reinforcement (Y) and concrete crushing or ultimate level (U) points can be defined to develop the $M$-$\phi$ for PSA (figure 6.11). It should be noted that the threshold points of the $M$-$\phi$ relationship are estimated based on the calculated strains in the steel and concrete, in a section analysis.
- The $M$-$\phi$ relationship should be defined for an appropriate range of axial loads acting on the pile, pre-stress levels, pile geometry, strength and threshold strain characteristics of pile materials.
- The $M$-$\phi$ relationship could be determined using conventional procedures for cross section analysis with simplified elastic-plastic load-deformation characteristics for concrete and steel. Commercial software is available for computing $M$-$\phi$ relationships.
6.2.1.6 Input ground displacements

Both magnitude and distribution of ground displacements have to be estimated for the cyclic liquefaction and lateral spreading analyses. A number of methods can be used to estimate the maximum free-field cyclic (transient) displacements in liquefied deposits. For example, SPT- and CPT-based liquefaction analysis methods may provide estimates for the maximum shear strain induced by liquefaction as a function of the seismic demand (cyclic stress ratio) and penetration resistance of soils. Ishihara and Yoshimine (1992), Tokimatsu and Asaka (1998) and Idriss and Boulanger (2008) provide such charts for evaluation of maximum shear strains. By integrating the shear strains throughout the depth of the deposit, ground displacement profile can be estimated assuming linear variation for the displacement in any given layer. While cosine distribution might be more appropriate, linear distribution is more practical and acceptable as the shape of the ground displacement profile has relatively small effect on the pile/foundation response compared with the absolute magnitude of the ground displacement.

Lateral spreading displacements can be estimated using the lateral displacement index or LDI method based on CPT (Zhang et al 2004) or empirical correlations based on regression analyses of case studies (eg Youd et al 2002). All methods currently in use for estimating lateral spreading displacements involve significant uncertainties, and some of those methods such as those based on regression analysis have little physical basis. Therefore, a range of ground displacements should be estimated and considered in the lateral spreading analyses.

**Ground displacement**

- Estimate maximum shear strains in liquefied soils using simplified methods based on SPT- or CPT-resistance.
- Determine the displacement profile by integrating shear strains throughout the depth of the deposit assuming linear distribution of displacements within a given layer.
- The estimated displacements are free-field ground movements unaffected by the presence of piles and bridge structure. Reduction of soil displacements due to pinning and strutting effects should then be considered for stiff and strong bridge structures with sufficient capacity to resist large lateral loads/movements. A number of case histories from the 2010-2011 Canterbury earthquakes suggest that pinning (strutting)-effects reduced the displacements of the foundation soils to 50% of the corresponding free-field ground displacements. (Note: ‘pinning’ refers to a resistance to ground movement provided by the superstructure. Pinning effects could be provided by global effects, eg from the strutting of the superstructure between the two abutments, or by structural members such as cantilevering of the piles above non-liquefied soils).
- It is assumed that the non-liquefiable crust layer on top of underlying liquefied layer moves as a rigid body, and hence displaces for the same amount as the top of the underlying liquefied soil; the base non-liquefiable layers do not move, though the method allows the designer to apply lateral ground displacement in any layer.
- For estimate of cyclic ground displacements refer to Idriss and Boulanger (2008), Tokimatsu and Asaka (1998) and Ishihara and Yoshimine (1992).
- Lateral spreading displacements can be estimated based on Zhang et al (2004) and Youd et al (2002). Evidence from the 2010-2011 Christchurch earthquakes can also be used to calibrate the estimates.
6.2.1.7 Input inertia load

In the model, two equivalent static loads can be applied to the pile: a lateral force \((F)\) representing the inertial load on the pile/bridge structure due to vibration of the superstructure, and a horizontal ground displacement \((U_g)\) representing the kinematic load on the pile due to lateral ground movement (cyclic or spreading) in the free field. The selection of appropriate equivalent static loads is probably the most difficult task in the PSA, because both input loads are, in effect, estimates of the seismic response of the ground and superstructure respectively.

One of the key issues in the PSA when evaluating the peak response of the pile during the cyclic phase is how to combine the kinematic loads due to cyclic ground displacements and the inertial loads due to vibration of the superstructure. The peak cyclic ground displacement and superstructure inertial force are transient conditions occurring momentarily during the course of strong shaking. They may or may not occur at the same instant. Currently there is no clear and simple strategy on how to combine these loads in the equivalent static analysis (PSA). Based on a series of large-scale shake table experiments, Tokimatsu et al (2005) suggested that the phasing of the kinematic and inertial demands varies, and depends primarily on the natural frequency of the superstructure and soil deposit. Based on numerical studies, Boulanger et al (2007) proposed a simplified expression (discussed in section 6.2.2) allowing for different combinations of kinematic and inertial loads on the pile while accounting for the period of the ground motion. As commonly acknowledged, for equivalent static approaches used for analysis of seismic problems, the kinematic-inertia load combination producing the critical (peak) pile response in liquefying soils cannot be predicted with any high degree of certainty.

Inertia load

- An estimate for the dynamic response of the bridge (spectral acceleration) is needed to calculate the maximum inertia force. A portion of this force can be used to determine the equivalent horizontal static force that will be applied in PSA.

- For the transient (cyclic) phase of the response, estimated cyclic ground displacements and estimated reduced inertia force are simultaneously applied to the pile (beam-spring model). Parametric variation in the inertia force should be considered to account for uncertainties in the combined kinematic and inertia loads.

- Provided that effects of inertia force have been carefully considered and evaluated in a cyclic PSA, inertia loads could be ignored in the lateral spreading analysis. A reduced inertia loads representative for post-liquefaction phase of the response can be adopted in the lateral spreading analysis, at discretion of the engineer.

6.2.1.8 Pile group effects

Pile group effects generally arise due to two independent mechanisms: a) obstruction of ground deformation/displacements, and consequent reduction in soil pressure on piles due to the presence of adjacent/surrounding piles in the group (foundation), and b) cross-interaction amongst piles due to the constraints imposed by a rigid pile cap or abutment that the piles are connected to.

When a large group of piles is subjected to cyclic ground displacements or lateral spreading displacements, the presence of the surrounding and adjacent piles influences the displacements of the foundation soils and the pressure (and ultimate load) on any given pile in the group. The well-known **shadowing effects** (obstruction of ground movement by the frontline adjacent pile) and **overlapping of wedges** (reduced pressure on the pile due to shared wedge-zone with adjacent piles in the row) affect the movement of the foundations soils and the imposed kinematic loads on any given pile. The shadowing and overlapping effects
depend on the spacing and the number of piles in the group. Figure 6.12 illustrates the reduction in the ultimate lateral soil pressure on a pile within a group compared with a single pile, as a function of the number of piles within the group. These data is for pile spacings of 2.5 to 3 pile diameters, and includes both active loading (pile pushed into the ground) and passive loading (ground pushed into the pile) (Cubrinovski et al 2006), though the trend is predominantly derived from active piles. These results from experiments in non-liquefied soils show reduction in the ultimate load on the pile with increasing number of piles in the group. Note however that pile spacing influences these reductions significantly, and that generally for spacing of six diameters or greater, pile group effects should be ignored.

Available experimental data on these effects for piles in liquefiable soils is limited and not conclusive. Because of the significant reduction in stiffness and strength of liquefied soils, the zone of soil affected by the presence of stiff piles is much smaller compared with non-liquefied soils. One can anticipate ‘flow’ of the liquefied soil around the pile without any substantial effect on the adjacent piles. Hence, it is prudent to ignore pile group effects in liquefied soils.

Figure 6.12  Pile-group effects on the ultimate lateral soil pressure displacements (Cubrinovski and Ishihara 2007)

Piles in a group are normally rigidly connected at the pile head and therefore, when subjected to lateral loads, all piles will share nearly identical horizontal displacements at the pile head. During lateral spreading of liquefied soils at river banks or waterfront area, each of the piles could be subjected to a different lateral load from the surrounding soils, depending upon its particular location within the group and the spatial distribution of the spreading displacements (figure 6.13). Consequently, both the interaction force at the pile head and the lateral soil pressure along the length of the pile will be different for each pile, thus leading to a development of distinct patterns of deformation and stresses along the length of individual piles in the group. These pile-group effects should be considered in the analysis using pile-group or whole bridge model.

Figure 6.13  Piles in a group subjected to varying lateral spreading displacements (Cubrinovski and Ishihara 2007)
Lateral spreading often exhibits a non-uniform spatial distribution of lateral ground displacements, which are commonly largest near the river banks (waterfront) and gradually decreasing with distance from the waterfront, therefore, as shown in the figure, the leading piles are subjected to much larger ground displacements than the trailing piles.

Pile group effects

1. Soil-pile interaction effects and pile cross-interaction effects should be considered.
2. Soil-pile interaction effects in liquefied soils are ignored.
3. Soil-pile interaction effects in non-liquefied soils depend on the spacing and number of piles in the group.
4. Significant reduction in lateral loads from the crust layer due to the pile-group effect is generally non-conservative and should be avoided. In other words, such reduction is prudent only when supported by a compelling case for the existence of pile group effects.
5. Cross-interaction effects should be considered with a pile-group or whole bridge model.

6.2.1.9 Global bridge analysis

A whole global bridge model for the Anzac Bridge is shown in figure 6.14. The model illustrates the benefits of the global bridge PSA. In principle, the soil and pile modelling for the whole bridge model is identical to the single-pile model. In the global bridge model, however, the variation in the subsurface conditions and lateral ground displacements can be considered along the bridge alignment, and their effects can be evaluated/quantified. The superstructure can be modelled as elastic or elastic-plastic, using linear or nonlinear (e.g., bi-linear) beam elements, and respective stiffness and strength of the structural members. Gaps between the deck and the abutment can be modelled as well as deck-pinning or deck-strutting effects. Depending on structural characteristics and geometry, abutments can be modelled either as rigid members or with their actual flexibility.

The global bridge analysis can provide more realistic simulation of the distribution of force and displacement demands throughout the bridge while considering the interaction between different components of the bridge, complex spatial distribution of subsurface conditions, foundation characteristics and ground movements along the bridge alignment. In addition to the details of the pile response as per single-pile analysis, deformation and stresses in structural members (e.g., deck, piers, abutment walls) and global displacement of the bridge (magnitude and direction) can be estimated while considering the interaction of the soil-pile-abutment-pier-superstructure system.

Global bridge analysis

- In the global bridge analysis, it is necessary to consider the response of the bridge and its components using a global bridge model.
- Liquefaction analysis and estimate of ground displacement profiles are required for each foundation (pile group). Lateral spreading displacements at the ground surface at the location of piers in the riverbed can be estimated by interpolating between the estimated spreading displacements at the river banks and assuming zero displacement at the neutral point in the central area of the riverbed.
- Simple but realistic models can be used for all principal components of the bridge including imposed displacement constraints by the deck or other structural members.
- Uncertainties in the estimates of ground displacements and soil spring properties should be assessed through parametric analyses.
In figure 6.14, blue solid lines show the deformed shape of the ANZAC Bridge computed in the analysis (A) where ground displacements have been applied only to the abutments and abutment piles. Red lines indicate the deformed shape of the bridge computed in the analysis (AP) where, in addition to the ground displacements applied to the abutments and abutment piles, ground displacements have been also applied to the pier piles. In the central part of the figure, bending moments are shown for the piers and pier piles for analysis A (solid blue lines), for analysis AP (red lines), for analysis 0.2AP (yellow lines) in which the magnitude of ground displacements applied to the pier piles has been reduced to 20% of those applied in the AP analysis (to account for uncertainties in the magnitude of ground displacements), and AP, $\alpha_{nl-0.5}$ analysis (green lines) where the strength of the non-liquefied layers along the pier piles was reduced to 50% of that used in the AP analysis (to account for potential increase in the excess pore pressures in these layers). The dashed vertical lines indicate the threshold cracking, yielding and ultimate bending moments for the pier and the pier piles respectively. Appendix B shows a worked example of this analysis.

6.2.1.10 Uncertainties in the analysis

Significant uncertainties associated with the model parameters in the PSA should be considered. An important question that needs to be answered is not ‘what is the most appropriate value for a given model parameter?’, but rather ‘how big is the effect of variation (uncertainty) in a given model parameter on the predicted pile response?’ This consideration will enable the user to focus on critical uncertainties in the analysis and develop a suitable strategy for robust implementation of the simplified PSA.

In the case of large ground displacements of a thick unliquefiable crust layer, the large ground displacements and spring properties of the crust layer may completely control the pile response. In such cases, the properties and uncertainties of the soil springs for the liquefied layers are irrelevant and can be ignored. In fact, one may find that in many cases only two or three critical parameters control the pile response in the PSA. Magnitude of ground displacements and properties of the crust layer (load from the crust) are often identified as critical parameters in PSA.
Uncertainties in the analysis

1. Identify the range of variation for soil spring parameters, ground displacements and equivalent static inertia load.
2. Conduct parametric study and identify key parameters controlling the pile response.
3. Focus on examining the effect of uncertainties in critical parameters on the pile response.

6.2.1.11 Summary of the analysis procedure

Step 1: Site and soil characterisation

Site characterisation should include interpretation of local geology, review of historical records with respect to liquefaction, and analysis of an appropriate combination of CPT or SPT investigation and laboratory test data. Shear wave velocity data can also be used and is especially valuable for gravelly soils. Detailed cross sections and soil profiles (including depth to the water table and data for simplified liquefaction triggering analysis) should be developed at each abutment and pier along the bridge alignment.

The soil characterisation should include liquefaction susceptibility evaluation and identification of non-liquefied layers based on plasticity criteria based on Idriss and Boulanger (2008) and Bray and Sancio (2006) and CPT-based \( I_c \)-criteria in addition to other generic criteria.

Step 2: Determine earthquake load at bridge site

The earthquake load parameters required for liquefaction triggering analysis (moment magnitude, \( M_w \) and horizontal peak ground acceleration, PGA) and inertia loads from the bridge superstructure (ie spectral accelerations) should be determined at the bridge site either using regional seismic hazard parameters or site specific analysis.

Step 3: Liquefaction triggering analysis

Conventional liquefaction triggering analysis is then conducted using CPT: (Idriss and Boulanger 2008; Youd et al 2001), SPT: (Idriss and Boulanger 2008) or \( V_s \)-based (Youd et al 2001) procedures to identify the layers that will liquefy including their factors of safety against liquefaction triggering. The water table and presence of non-liquefiable soils should be used to determine the thickness of the crust of non-liquefiable soils at the ground surface.

Step 4: Formulate beam-spring model

The beam-spring model is defined based on the geometry of the bridge, bridge components and simplified soil profile derived in steps 1 and 3. The length of the beam elements or spring spacing should be preferably 0.1m and not larger than 0.2m. Appropriate boundary conditions should be adopted for a single-pile (at the top and tip of the pile) or a global bridge model including constraints imposed by the structure.

Step 5: Estimate soil spring parameters

Stiffness and strength of the springs are estimated for the non-liquefiable crust layers, liquefied layers and non-liquefiable layers throughout the depth of the profile based on detailed procedures described in section 6.2.1 and expressions given in equations 6.1 to 6.9. Best-estimate (reference), upper-bound and lower-bound values should be estimated for stiffness and strength (ultimate capacity) of soil springs. Separate set of spring values should be defined for the cyclic phase and lateral spreading phase (analysis) of the bridge.
Step 6: Estimate pile $M-\phi$ parameters

The bending stiffness and moment curvature relationships for the piles, abutments, piers and deck should be defined. Bi-linear or tri-linear relationships are preferred. $M-\phi$ relationships should be defined for an appropriate range of axial loads, pre-stress levels, pile geometry, strength and threshold strain characteristics of the pile.

Step 7: Estimate free-field ground displacements

Magnitude and distribution of ground displacements throughout the soil profile are estimated for free-field conditions (excluding any interaction with the piles or bridge structure), using the methods listed in section 6.2.1. Cyclic liquefaction and lateral spreading displacements should be considered and estimated separately. Given the uncertainties in the assessment of lateral spreading displacements and due to sensitivity of cyclic displacements in liquefied soils to site response and earthquake motion characteristics, a range of ground displacements (ie best-estimate, upper bound and lower-bound values) should be considered in the analyses.

Step 8: Estimate inertia loads

Inertia loads should be estimated for the cyclic phase of the response, from both the superstructure and the pile cap. Inertia forces can be calculated using spectral accelerations, and applied as static forces at the top of the pile (from pile cap) or at the deck (from the superstructure). For the cyclic phase of the response maximum ground displacement and a portion of the maximum inertia force should be applied simultaneously to the pile or bridge model. In the lateral spreading analysis none or a small portion of the inertia load should be applied.

The designers should also consider negative skin friction on the piles resulting from settlement of liquefied soil and non-liquefied crust. Appropriate down-drag loads should be considered in the design if required.

Step 9: Conduct PSA with best-estimate parameters

PSA is conducted using best-fit values for the parameters of the beam-spring model and loads.

Step 10: Conduct parametric (sensitivity) analyses

In order to consider uncertainties in the assessment of liquefaction and lateral spreading and in the analysis procedures, PSA should be conducted using upper-bound and lower-bound values for the parameters of the beam-spring model and loads.

Step 11: Estimate pile group effects

Pile group effects due to overlapping zones, shadowing and cross-interaction should be evaluated separately in the case of single-pile analysis. It is recommended to employ a global bridge analysis in order to capture the interaction of the soil-pile-pier-abutment-deck system.

Step 12: Consider SFSI and 3-D effects

P-delta effects and potential buckling (O’Rourke et al 1994; Bhattacharya et al 2004) as well as effects of soil-foundation-structure interaction (SFSI) and 3-D effects should be considered by separate checks and analyses, if potentially significant.

6.2.2 PEER method

The Recommended design practice for pile foundations in laterally spreading soil ground by PEER (Ashford et al 2011) provides a summary of recommended procedures and practices for analysis and design in the
US. In this method, the equivalent static analysis or PSA has been identified as one of the principal methods for the analysis of bridge pile foundations. In this report we refer to this PSA analysis as the PEER method.

The PEER method of analysis is very similar in concept to the Cubrinovski et al method and can be summarised as follows:

- A beam-spring model is used (figure 6.15) where nonlinear soil-springs and nonlinear moment-curvature relationships are employed for the soil and the pile. Lateral, vertical and bearing soil springs are defined in the model. However Ashford et al (2011) stated that guidance for the vertical springs and bearing springs could not be provided.

- The method can be applied to a single pile, pile group or the whole bridge. The analysis of a pile foundation may be directly coupled to, or separated from the analysis of the superstructure. Analyses in both transverse and longitudinal directions and separate analyses for non-liquefaction and liquefaction cases are recommended.

- The displacement based approach is adopted where the free-field ground displacements are applied at the end of the soil springs. A number of different methods suggested for estimating the free-field displacements, including integration of shear strain profiles in conjunction with SPT- and CPT-based liquefaction analyses (eg Ishihara and Yoshimine 1992; Tokimatsu and Asaka 1998; Idriss and Boulanger 2008), LDI method (Zhang et al 2004), empirical relationships based on regression analysis (Youd et al 2002) and the Newmark sliding block analysis (either regression models or site specific time history analysis). Considering the uncertainties in estimating lateral spreading displacements based on the currently available methods, it is recommended to make a number of independent estimates and quantify a range of anticipated displacements.

**Figure 6.15  Pile-group model in the PEER equivalent static analysis with imposed soil displacements**

- The PEER method suggests that the shape of the ground displacement profile is not an important factor for laterally stiff and strong piles. Therefore, a simple linear distribution of ground displacements can be adopted across layers. For flexible piles, however, the shape of the ground displacement profile can control bending moments and curvature demands. Therefore, alternative soil displacement profiles may need to be considered.
The restraining or pinning effect of the pile foundation can significantly reduce the lateral spreading displacements of the soil near the pile foundations.

Effects of liquefaction on the soil springs are accounted for by two separate methods. In the first method, scaling factors, or so-called p-multipliers \( (m_p) \) are applied to the spring (p-y) resistance. Figure 6.16 summarises the p-multipliers accounting for liquefaction effects as a function of the clean-sand normalised SPT blow count. Figure 6.17 summarises some other published recommendations for p-multipliers.

It is recommended to use the middle of the range of p-multipliers recommended by Brandenburg (2005) and check the sensitivity of the foundation response to a factor of two increase or decrease in p-multipliers. Pile performance can be insensitive to the p-multipliers when a strong non-liquefiable crust is present.

While the PEER method uses nonlinear p-y curves (concave downward), the shape of these curves can be very different from those of liquefying soils observed in experiments (the actual curves are concave upward due to cyclic mobility).

The second recommended method to account for the effects of liquefaction on the soil springs is the use of the residual post-liquefaction soil strength (\( S_r \)).

Residual soil strength can be estimated from empirical correlations to SPT or CPT data and both \( S_r \) based or normalised relationships (\( S_r/\sigma'_{vc} \)) can be applied.
• The Rankine pressure theory is the most appropriate for calculating the passive pressure in non-liquefiable crust layers. When free-field ground displacements (not accounting for pinning-effects) are specified as an input, the amount of displacement required to mobilise the ultimate crust load can be approximated as being 25% (for stiff crust soils) to 70% (for soft or loose crust soil) of the wall (or pile cap) height.

• For design purposes it is prudent to assume that enough lateral spreading displacement occurs during strong ground shaking to consider the lateral spreading displacements and a fraction of the inertia demands as additive. In other words, lateral spreading displacements and inertial loads should be applied simultaneously (figure 6.18).

• The inertia force is given by:

\[
I_{liq} = C_{cc} \cdot C_{liq} \cdot I_{nonliq}
\]  
(Equation 6.10)

in which \(I_{liq}\) - inertia force accounting for effects of liquefaction, \(C_{cc}\) - the fraction of the maximum displacement demand with liquefaction that occurs at the critical cycle, \(C_{liq}\) - ratio of maximum displacement demand with liquefaction to that without liquefaction, and \(I_{nonliq}\) - peak inertia force for a linear-elastic bridge superstructure in the absence of liquefaction (\(I_{nonliq} = m \cdot S_a\) where \(m\) is mass and \(S_a\) is spectral acceleration). The variation of the coefficients in equation 6.10 with the frequency characteristics of the motion for the pile cap and superstructure inertia forces is given in figure 6.19.

Figure 6.18 Combined displacement demands from lateral spreading and inertial loading in the longitudinal direction for an individual single-column bent (Ashford et al 2011)
The stiffness and capacity of soil springs are often reduced to account for pile group interaction effects by applying group p-multipliers. Group effects should not be applied in liquefied soils because available case studies and research data indicate they do not exist in liquefied soils. Also, group effects should not be applied in laterally spreading non-liquefiable crust layers, because this would constitute non-conservative reduction in lateral spreading forces.

Global bridge analyses are recommended particularly when the subsurface conditions and expected ground displacements vary substantially along the bridge alignment (figure 6.20). Global analyses can provide additional insights into the pinning effects at abutments, where axial loads in the superstructure can pin back the spreading abutment. A number of possible loading combinations should be examined in the global bridge analyses.

Parametric and sensitivity analyses are recommended to assess the uncertainties and check the design for a range of soil spring parameters, ground displacements and loading conditions using best estimates, upper and lower bound design values.

The AIJ method (AIJ 2001) specifically addresses piles for building foundations. It is one of the well-developed and widely used methods for analysis of pile foundations in Japan. It is therefore useful for geotechnical designers to understand its basics. The AIJ method of analysis is similar in concept to the Cubrinovski et al method. Key features of the AIJ method of analyses are as follows:

- It adopts the displacement-based approach using a beam-spring model and uses Bi-linear soil springs and tri-linear (or similar) moment-curvature relationships for the pile. Free field ground displacements...
6 Methods of analysis

are applied at the end of the springs to simulate effects of transient ground displacement and spreading displacements.

- The stiffness of soil springs is defined using the subgrade reaction approach. Equation 6.2 is used for sandy soils.

**Figure 6.21** Stiffness reduction factor for liquefied soils adopted in AIJ method (AIJ 2001)

- Effects of liquefaction on the soil springs are accounted for through a degradation factor $\beta$ which is a function of the SPT blow count $N$ and depth, as shown in figure 6.21. In the figure, $N_a$ is equivalent to a normalised SPT blow count.

- The ultimate soil pressure or spring strength in non-liquefied soils is defined using the Rankine passive pressure and an expression identical to that given in equation 6.3 with $\alpha_\ell = 3.0$ based on the well-known early study of Broms (1964).

- Uchida and Tokimatsu (2005) recommended the use of $\beta$ as defined in figure 6.21 also for the degradation of soil pressure in liquefied soils.

- Three separate analyses are recommended for the pile foundations: non-liquefaction analysis (Case I), liquefaction analysis (Case II) and lateral spreading analysis (Case III), as illustrated in figure 6.22 (Tokimatsu and Asaka 1998; Tokimatsu et al 2005).

**Figure 6.22** Separate analyses and loading conditions (inertia and kinematic loads) for three different stages of the response: no-liquefaction (Case I), liquefaction (Case II) and lateral spreading (Case III) (Tokimatsu and Asaka 1998; Tokimatsu et al 2005)
• Ground displacements for both liquefaction and lateral spreading analyses are estimated based on the respective procedures recommended in Tokimatsu and Asaka (1998) using estimates of maximum shear strains and their integration throughout the depth of the profile.
• Effects of ground displacements are neglected in non-liquefaction analysis (Case I) with the inertia force being the only applied load in this analysis.
• In the liquefaction analysis (Case II), effects of inertia and ground displacement demands are combined by assuming either that the inertia and kinematic forces are in phase (method 1, when the natural period of the superstructure is smaller than that of the ground) or that the inertia and kinematic forces are out of phase (method 2, when the natural period of the superstructure is larger than that of the ground. In the latter case, the maximum pile bending moment may be estimated by the square root of the maximum moments computed in decoupled analyses in which maximum inertia force and maximum ground displacement (kinematic load) are applied respectively, as illustrated in figure 6.23.

Figure 6.23 Approximation of combined effects of inertia and kinematic loads on pile in liquefaction analysis – Case II (Tokimatsu et al 2005)

6.2.4 Japan Road Association (JRA) method
The JRA method (JRA 1996; Tamura 2013) was developed specifically for highway bridges. Highway bridges in Japan are very large and massive structures and large diameter piles (shafts) in a group are typically used for these bridge foundations. The piles are very stiff and strong, and hence generally resist the ground movement and show stiff pile behaviour as depicted in figure 6.5. This feature is reflected in the design and analysis philosophy of the JRA method.

Key features of the JRA method of analyses can be summarised as follows:
• The JRA method considers three cases for: non-liquefaction, liquefied soils and laterally spreading soils.
• The analytical model for non-liquefaction and liquefaction analyses of a pier-pile structure using a beam-spring model is shown in figure 6.24. Bi-linear springs and tri-linear relationships are used for the soil and pile respectively.
• Effects of liquefaction are accounted for by multiplying the stiffness (subgrade reaction coefficient), ultimate soil reaction (strength of soil spring) and skin friction capacity by a degradation coefficient $D_e$. The coefficient $D_e$ is defined as a function of the factor of safety against liquefaction triggering ($F_L = F_s$) and depth from the ground surface (figure 6.25).

**Figure 6.24** Analytical model and load deformation relationships for liquefaction analysis of a pier pile foundation (Tamura 2013)

- Force-based approach, with prescribed lateral loads on the pile corresponding to the ultimate loads from the soil on the pile, is used for lateral spreading analysis.

<table>
<thead>
<tr>
<th>Range of $F_L$</th>
<th>Depth from ground surface $x (m)$</th>
<th>Dynamic shear strength ratio $R$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_L \leq 1/3$</td>
<td>$0 \leq x \leq 10$</td>
<td>$R \leq 0.3$</td>
</tr>
<tr>
<td></td>
<td>$10 \leq x \leq 20$</td>
<td>$1/3$</td>
</tr>
<tr>
<td>$1/3 &lt; F_L \leq 2/3$</td>
<td>$0 \leq x \leq 10$</td>
<td>$1/3$</td>
</tr>
<tr>
<td></td>
<td>$10 \leq x \leq 20$</td>
<td>$2/3$</td>
</tr>
<tr>
<td>$2/3 &lt; F_L \leq 1$</td>
<td>$0 \leq x \leq 10$</td>
<td>$2/3$</td>
</tr>
<tr>
<td></td>
<td>$10 \leq x \leq 20$</td>
<td>$1$</td>
</tr>
</tbody>
</table>
Rankine passive pressure is specified for the non-liquefied layer, while 30% of the overburden effective stress is applied to the underlying liquefied layer, resulting in linear distribution of these pressures with depth, as illustrated in figure 6.26. Details in the calculation of the lateral pressures are given below:

\[ q_{NL} = C_s C_{NL} K_p \gamma_{NL} x \quad (0 \leq x \leq H_{NL}) \]  \hspace{1cm} \text{(Equation 6.11)}

\[ q_L = C_s C_L \left( \gamma_{NL} H_{NL} + \gamma_L (x - H_{NL}) \right) \quad (H_{NL} < x \leq H_{NL} + H_L) \]  \hspace{1cm} \text{(Equation 6.12)}

In which \( K_p \) - coefficient of passive earth pressure, \( x \) - depth measured from the ground surface, \( \gamma_{NL} \) and \( \gamma_L \) - unit weights of non-liquefied and liquefied layers respectively, and the constants are given below. \( C_s \) is the correction factor for distance, \( S \), from the waterfront, ie

\[ C_s = \begin{cases} 1.0 & \text{for } S \leq 50\text{m} \\ 0.5 & \text{for } 50\text{m} < S \leq 100\text{m} \end{cases} \]  \hspace{1cm} \text{(Equation 6.13)}

\( C_s \) is the correction factor in the liquefied layer:

\[ C_L = 0.3 \]  \hspace{1cm} \text{(Equation 6.14)}

\( C_{NL} \) is the correction factor in the non-liquefied layer:

\[ C_{NL} = \begin{cases} 0.0 & \text{for } P_L \leq 5 \\ (0.2P_L - 1)/3 & \text{for } 5 < P_L \leq 20 \\ 1.0 & \text{for } P_L > 20 \end{cases} \]  \hspace{1cm} \text{(Equation 6.15)}

In equation 6.15, \( P_L \) represents the index of liquefaction potential (Iwasaki et al 1982), which is used to express the severity of liquefaction.

**Figure 6.26** Definition of lateral loads in the force-based approach for analysis of lateral spreading (‘ground flow’) adopted in the JRA method
6.2.5 Consideration of PSA methods

The Cubrinovski et al. method focuses on a simplified, but sufficiently accurate, modelling of the soil-pile-bridge system where uncertainties in the applied loads and characteristics of liquefying soils are addressed through modelling considerations and parametric studies. Special attention and guidance is given to the determination of model parameters and also to the identification of the key parameters controlling the pile/bridge response in order to focus on critical performance parameters.

The non-linear p-y curves of the PEER method do not provide any advantage in the modelling of the soil-pile interaction in liquefied soils, but potentially introduce difficulties in the determination of soil springs. The AIJ method on the other hand, does not provide guidance on how to treat the uncertainties associated with liquefaction and lateral spreading, and how to perform parametric evaluations.

The PEER and AIJ methods provide a relatively simple guidance for the evaluation of inertial loads from the superstructure (and pile cap) and on how to combine the inertial and kinematic loads in PSA addressing the cyclic phase of liquefaction analysis. It is important to recognise that the estimate of inertial loads as well as the combination of inertial and kinematic loads in an equivalent static analysis will always be burdened by substantial uncertainties. Therefore emergence of well-established criteria for the combination of these loads is highly unlikely. For this reason, it is essential to perform parametric evaluation within reasonable range of assumed inertial loads and inertial-kinematic load combinations.

The JRA method suffers from the key anomaly of the forced-based approach where compatibility between the pile displacement and the soil pressure cannot be ensured. The method is clearly inappropriate for any pile behaviour except for very stiff pile behaviour (figure 6.5), and therefore is very limited in its application.

6.3 Time history (dynamic) analysis

The dynamic response of the bridge is highly nonlinear and changes dramatically as it goes through the different stages from the initiation of strong shaking, through rapid build-up of excess pore pressures and consequent reduction in stiffness and strength of soils, development of liquefaction and post-liquefaction large ground deformation associated with earthquake-induced but gravity driven spreading. A nonlinear time history analysis enables the designers to investigate the dynamic response of the bridge taking into account complex soil-pile-pier-abutment-deck interaction of the bridge system in liquefying and laterally spreading soils (figure 6.27). There is no doubt that a capable numerical (effective stress) analysis that is well-calibrated and executed provides the most realistic simulation of the actual bridge behaviour. While the use of nonlinear time history analysis is beyond the scope of this report, it is important to emphasise the unique capability and value that such analysis provides, and hence it is recommended for use whenever viable and justifiable. The dynamic effective stress analyses are becoming more common for significant engineering projects, and it is anticipated that their use will further increase in the near future. Key features, advantages, shortcomings and requirements of the time history analysis are summarised in table 6.1. A more detailed consideration of modelling issues and applications of the effective stress analysis is given in Cubrinovski (2011).

6.3.1 Effective stress analysis (ESA)

A rigorous ESA permits evaluation of seismic soil-pile interaction while considering the effects of excess pore pressure and eventual soil liquefaction on the pile response. The predictive capacity of such analysis has been verified in many studies. However its application in engineering practice is constrained by two requirements:
6.3.2 Total stress analysis (TSA)

The total stress dynamic analysis has the same attributes and requirements as the ESA except that it cannot accurately simulate effects of excess pore pressures and liquefaction. The soil models in TSA should reflect substantial reduction of stiffness and strength of liquefied material.

Figure 6.27 Analytical model for effective stress analysis of a bridge in liquefying soils

6.4 Substructure approach

The Multidisciplinary Center for Earthquake Engineering Research (MCEER) method (MCEER 2001; Martin et al 2002) provides guidelines for the seismic design of highway bridges in the US including recommendations for design against liquefaction and lateral spreading. The MCEER method considers a subsystem of the bridge and focuses on the design of piles in approach abutments. The MCEER method can be summarised as follows:

- The design for vibration (cyclic phase of the response) and lateral spreading is considered in a decoupled manner, using two separate analyses.
- The cyclic phase is considered using nonlinear static or pushover analysis where the effect of liquefaction is included through a reduced soil resistance adjacent to the foundation and the alteration of the input seismic spectra is due to softening and energy dissipation in the soil.
- The rationale behind the lateral spreading design approach is to determine the likely magnitude of lateral soil movement and assess the structure’s ability to accommodate and/or limit this movement. The flowchart of the methodology is given in figure 6.28.
The method can be summarised as follows:

- The soil layers likely to liquefy are identified.
- Pseudo-static stability analyses are conducted to back-calculate the yield acceleration or acceleration triggering instability. In the stability analyses, residual strength is used for the liquefied layers.
- Newmark sliding block analysis is used to estimate the ground displacements due to lateral spreading.
Two scenarios are considered for the pile response: flow of soil around the pile (stiff pile behaviour), and displacement of the foundation together with the soil (flexible pile behaviour). These cases are shown in figure 6.29. If the flow of soil around the structure is indicated in the assessment, the foundation is designed to withstand passive pressures from the soil (the maximum lateral loads from the soil). If on the other hand, the assessment indicates flexible pile behaviour, the structural behaviour of the piles must be evaluated at the maximum expected displacement.

The plastic deformation of the foundation is determined using PSA. The likely shear resistance of the foundation is assessed and then a stability analysis is conducted where additional resistance provided by the bridge foundation is included.

Ground displacements are recalculated using the revised stability calculations, and the response of the structure is re-evaluated. Structural strengthening or ground improvement is adopted if the assessed seismic performance of the bridge is not acceptable.

The PEER guidelines also consider the design of piles in approach embankments in a similar way as the MCEER:

- The PEER procedure for piles in approach abutments consists of three parts:
  - estimation of longitudinal displacement of the embankment for a range of restraining forces from the foundation and bridge superstructure
  - estimation of the longitudinal restraining force exerted on the embankment by the pile and bridge superstructure for a range of spreading displacements
  - determination of compatible displacement and the interaction forces between the embankment, the piles and the bridge superstructure.

- A range of possible failure surfaces is considered in the slope stability analyses (figure 6.30), in which foundation shear forces are distributed or represented by an increase in soil shear strength along some portion of the failure surface. When estimating the loads on the piled abutment, it is recommended to limit the distance to which the critical surface extends behind the abutment to about four times the height of the embankment. In this step of the analysis embankment displacements are estimated for a range of restraining forces based on the computed yield acceleration and adopted design ground motion parameters.
- The restraining force from the pile foundation is determined using an equivalent static pushover analysis. Global bridge analysis can be used to estimate the development of resisting forces from the bridge superstructure and load transfer to either the intermediate bends or to the opposite abutment. In this analysis, the restraining forces from the pile foundation and bridge superstructure are estimated for a range of possible embankment displacements.

- The interaction diagram is eventually constructed (figure 6.31) to estimate the compatible displacement and interaction force between the embankment sliding mass and the pile foundation-bridge superstructure. The intersection of the curves in the force-displacement relationship determines the compatible displacements and forces.

**Figure 6.30** Critical slope stability failure surfaces for different values of pile restraining force (Ashford et al 2011)

**Figure 6.31** Compatibility between computed embankment slide mass displacements and equivalent constant restraining force from the pile foundation (Ashford et al 2011)
7 Structural mitigation approaches to liquefaction induced lateral spreading

Mitigation measures/design philosophy depends on the size and type of the structure and the extent of liquefaction and liquefaction induced movements (settlements and lateral displacement), as well as the interaction between the soil and the proposed structure. At least three approaches can be followed.

Approach 1 (structural): minimise effect of lateral spreading on vulnerable parts of the structure.

The focus of this approach is to minimise the effect of lateral spreading load on the most vulnerable parts of the structure (the abutments) and utilise the superstructure and substructural elements less exposed to lateral spread loading to support these parts as follows:

At the abutments:

- Minimise the size and number of piles to minimise the lateral spread loading being attracted to the structure. This arrangement, however, minimises the pile pinning effect on the moving soil which can be conservatively ignored in the design. The piles should be designed to resist lateral spread load elastically.
- Create a void below the abutment, bridged by a simply supported ‘landspan’ supported on a shallow spread footing on the embankment, to minimise the depth of the abutment structure directly loaded by spreading or rafting of the embankment material. This void can also be used as a zone in which services carried on the bridge can be provided with flexibility to accommodate relative movement between the bridge and the approaches.
- Consider using ground improvement techniques to further minimise the effects of liquefaction, if necessary or desirable.

At the piers:

- Position piers as far out and away from lateral spreading embankments as practical to minimise lateral spread loading from acting directly on pier piles and for loading from embankment spreading from one end of the bridge to be counterbalanced by that from the other end of the bridge. This allows the number and size of the piles to be increased and the bridge superstructure to be used to prop lateral spread loading acting on the abutments and their piles across to the larger, stronger and more numerous pier piles. This applies particularly to a two-span arrangement at a generally liquefiable site where the loading on the central pier can be counter-balanced. Piles at the pier(s) need to be designed to be able to resist any out-of-balance lateral spreading induced forces, combined with the seismic inertial loads if required.
- Use of permanent steel casing for the piles to provide additional stiffness and/or strength and confinement can be beneficial. Use of steel encased piles offers the benefit of providing a high level of confinement to the concrete core enhancing the ductility of the pile. The steel casing, with an appropriate allowance made for section loss due to corrosion, can also be utilised to provide some of the pile flexural capacity, though it will generally be necessary to keep the inner surface of the casing free of protrusions (eg shear connectors) to facilitate pile driving and construction. Design of the steel casing should consider constructability and resistance to buckling.

Approach 1 was the approach used in the design of the Ferrymead Bridge (Kirkcaldie 2013).
Approach 2 (structural): resist lateral spread loads at the abutments, as follows:

At abutments:

- Provide strong and stiff foundations (piles). These can be either anchored (cantilevering) from the non-liquefiable underlying layers or racking, supported by the non-liquefiable layers.
- Include in the design any pinning effect of the piles on the lateral spreading induced movements in the design (use soil structure interaction).
- Large movement (rotations) of the piles is likely to occur. Check that the piles (and the rest of the structure) are capable of accommodating these.
- If deflections are excessive either accept or resist them. Consider using ‘passive’ piles (piles not connected to the superstructure) to increase the pinning effect and ‘shield’ active abutment piles.
- Consider using permanent steel casing for the piles to provide additional stiffness and/or strength and confinement. Use of steel encased piles offers the benefit of providing a high level of confinement to the concrete core enhancing the ductility of the pile. The steel casing, with an appropriate allowance made for section loss due to corrosion, can also be utilised to provide some of the pile flexural capacity, though it will generally be necessary to keep the inner surface of the casing free of protrusions (eg shear connectors) to facilitate pile driving and construction. Design of the steel casing should consider constructability and resistance to buckling.
- Consider using soil improvement techniques to improve performance of the bridge structure if necessary.

At piers:

- Position these as far out and away from the lateral spreading embankments as practical to minimise lateral spread loading from acting directly on pier piles. The piles should be considered as part of the overall lateral load resisting system in the bridge longitudinal direction, as well as in the bridge transverse direction.

Superstructure:

- Superstructure should be designed and detailed to be able to resist imposed loads elastically. Connection with the abutments and pier should be designed and detailed to be able to accommodate expected movements and does not restrain and cause damage to either the superstructure or the supports.

In the design of foundations under the effect of lateral spreading loads in approaches 1 or 2, soil structure interaction (eg soil lateral spread loads on the structure due to both unliquefied and liquefied soils, pile pinning effects) should be considered. This may involve iterative analysis.

Approach 3 (geotechnical): ground improvement

The focus of this approach is to strengthen and stabilise the ground that is prone to lateral spreading under the onset of liquefaction, to limit the ground displacement and loading imposed on the bridge to tolerable levels. With lateral spreading generally arising from approach embankments settling, ground improvement mitigation efforts are generally focused around the abutments and the zone of the embankment immediately behind the abutments. Approaches that have been applied include:

- Installation of stone columns through the layers of liquefiable material to provide a drainage path for water, relieving the buildup of pore water pressure that causes soil liquefaction, and increasing the shear strength of the block of soil supporting the embankment in the vicinity of the abutment.
drainage blanket should also be installed across the top of the stone columns, beneath the embankment, to drain the ejected water out to the sides of the embankment.

- As a retrofit solution at existing bridge abutments, arrangement of stone columns in a triangle behind the abutment has been used to strengthen the ground immediately behind the abutment and to deflect any lateral spreading from further back along the embankment out to the sides and away from the bridge.

- Where liquefiable materials are in close proximity to the ground surface (e.g., <3m deep), ground replacement of foundation materials beneath embankments and in the zone immediately in front of abutments may be a practical option. This approach may be particularly appropriate as a retrofit option when headroom constraints make it impractical to install stone columns in front of the abutments of an existing bridge.

- Reinforcement of embankments at bridge abutments with geogrid to reinforce the embankments against slip circle failure and against being able to spread laterally.

- Construction of embankments using geofoam materials (e.g., polystyrene) to reduce the weight of the embankment and therefore the weight of material driving slip circle failures penetrating down into the foundation material underlying the embankment.

- Jet grouting of the ground in the vicinity of the abutment to form a block of competent founding material beneath the abutment and adjacent approach that will not liquefy.

- Utilisation of piles to restrain the uppermost soil materials that would otherwise slide on a slip circle surface by pinning them to stronger underlying material. These may be either the piles used to support the bridge abutments or additional piles that are not part of the bridge structure.

Ground improvement may limit ground displacement due to lateral spreading, but not totally eliminate it. Confirmation that the bridge structure and its supporting piles can sustain the residual displacements will commonly be necessary. Again, as for approach 1, the use of permanent steel casing to provide both additional flexural capacity and enhance the ductility of piles loaded by the lateral spreading can be beneficial.

The seismic strengthening of the SH3 Cobham Bridge at Wanganui (Brabhaharan and Kirkcaldie 2009) is an example of application of this second approach, in which:

- stone columns and wick drains were installed in a triangular shaped arrangement behind and to the sides of the abutment to strengthen the embankment, relieve the build-up of pore water pressure inducing liquefaction, and to deflect laterally spreading embankment from further behind the abutment around the abutment and away from the bridge

- constrained by low headroom in front of the abutment making the installation of stone columns impractical, ground replacement of shallow liquefiable soils in front of the abutment was also undertaken, providing buttressing to the embankment.

Single span bridges supported on spread footings on MSE wall retained embankments have been designed employing:

- strengthening and drainage of the foundation soils using stone columns overlain with a drainage blanket at the base of the supporting embankments

- transverse reinforcement of the embankments with geogrid to provide restraint against lateral spreading of the embankment.
At the Cobham Bridge in Wanganui, approach 3 was applied through strengthening the plastic hinge regions of the piers for shear and installing ground improvements at the abutments (Brabhaharan and Kirkcaldie 2009).

Situations in which one of the three approaches may be more appropriate to adopt are as follows:

Approach 1 or 2: Structural mitigation is more likely to be favourable when:

- the structure is a new bridge to be designed for which a structural arrangement applying the principles outlined above can be adopted
- the depth of potentially liquefiable material materials is very deep, making the effectiveness of a ground improvement approach questionable and costly
- numerous services are present at the site and are to be carried on the bridge, resulting in the protection or relocation of the services being costly should a ground improvement approach be adopted.

Approach 2 can be used for either a new bridge or for retrofitting an existing bridge. Retrofitting can be carried out by installing large diameter piles with a new capping beam behind the existing abutment. A particular advantage is that it does not eliminate passive resistance at the abutments which can be very effective at providing damping and reserve strength under strong shaking that may precede the lateral spreading phase.

Approach 3: Ground improvement is more likely to be favourable when:

- retrofit of an existing bridge for seismic resistance is required, the structural form of which will not generally be amenable to radical alteration
- the depth of liquefiable ground required to be improved is not excessive
- there is an absence of buried services at the site, although a construction technique has been developed for stone column installation that minimises the potential for damage to services as described in the Cobham Bridge seismic retrofit paper (Brabhaharan and Kirkcaldie 2009).

A paper presented by Poulos (2013) gave three categories of liquefaction mitigation measures. These can be divided into treatment of liquefiable soil to strengthen it, treatment of soil to accelerate the dissipation of seismically induced excess pore pressures and measures to reduce liquefaction induced damage to the structure or facility.
8 Conclusions and recommendations

The design methods described in this report to address liquefaction and lateral spreading effects are based on observed seismic behaviour of bridges and on the most recent research findings.

The report has discussed a large number of issues associated with liquefaction and lateral spreading and their effect on bridge structures and requirements for geotechnical investigations, evaluation techniques for liquefaction and lateral spreading, methods of ground improvements, methods of liquefaction analysis, structural mitigation solutions, and construction and monitoring issues.

Design of bridges for liquefaction and lateral spreading effects is a complex technical problem and a large number of issues associated with the design process require further research and refinement. Additional work will be required to summarise the findings in a form of a technical memorandum which can be later incorporated into NZ Transport Agency’s Bridge manual and disseminated to the wider New Zealand engineering community.

There are several areas where further development and refinement of investigation, assessment and design processes will be of value:

• Update the Bridge manual by implementing the key investigation, assessment and design guidelines presented in this report.

• Standardise field and laboratory testing procedures, sampling and reporting. Recent work in Christchurch has highlighted the need for consistency in CPT testing procedures and SPT hammer calibration. Other methods such as shear wave velocity and cyclic triaxial testing are becoming more commonly used in practice but the quality of testing can be variable. Standardisation of sampling and testing methods would provide greater confidence in the results and comparison between results from different sources. Standardisation should also improve efficiency with investigation scoping, briefing of investigation contractors and assessment of results.

• Undertake detailed investigation of the liquefaction susceptibility and post liquefaction behaviour of local New Zealand soils. The geology of New Zealand is diverse, comprising areas of young alluvial, marine, aeolian and tephra sand and non-plastic silt deposits with a variety of chemical compositions and mechanical properties. Recent research on pumice soils indicates conventional liquefaction triggering analysis methods may under-predict their resistance to liquefaction and this may be the case for other New Zealand soils. Post-liquefaction strength, strain magnitude and how strain develops during shaking is important for estimating lateral spread displacements and consequences of liquefaction for bridges. The results of these detailed investigations should be used to complement conventional techniques to estimate triggering using CPT or shear wave velocity test data for example.

• Undertake research to improve prediction of lateral spread displacements and pile pinning effects. Lateral spread displacement is an uncertain but often a sensitive input to pseudo-static displacement based analysis of bridge piles. Limitations with current methods to calculate lateral spread displacements are described in this report. Improved estimation of lateral spread displacement and the pinning effects of piles will reduce uncertainty in bridge performance and therefore reduce the need for expensive mitigation measures.

• Develop a (GIS) database of investigation results, laboratory testing and construction data. This database will be useful in a number of ways and as the database grows, may reduce the amount of investigation required on successive projects. For example, comparison of ground improvement trials
will be useful for comparing the effectiveness and relative cost of different improvement techniques. Cyclic triaxial testing can be used to continually update liquefaction resistance charts.

- Develop standard specifications for the construction of ground improvement methods. These should detail minimum quality control and assurance methods for ground improvement techniques including requirements for field trials to confirm the design.

- Perform a detailed analysis of soil structure interaction for typical New Zealand bridge forms. Time history effective stress analysis of typical structures will help understand which forms and pile types perform better and what existing bridge forms are more susceptible to liquefaction.

- Undertake research to assess the relative performance and optimise the design of ground improvement.

- Undertake instrumentation of bridges in liquefiable areas. Instrumentation may include inclinometer tubes in piles, accelerometers on the superstructure and ground-based instruments to record the ground motions. Pore-water pressures monitoring would also provide valuable information. Instrumentation installed on the ANZAC Bridge (or a SH bridge located at some other liquefaction prone site in a high seismic zone) as part of a research project would provide a better understanding of the performance of bridges on sites prone to liquefaction. Further possible instrumentation may include inclinometer tubes in piles for example or rapid assessment of damage to piles following an earthquake and to gain better understanding of the behaviour of bridges on liquefiable sites. Select bridges may include accelerometers or electronic inclinometers for detailed post-disaster assessment of bridge response.

- Consider further design issues associated with liquefaction at large depths (more than 20m below the ground surface level), the settlement of spread footings (shear deformations within liquefiable layers) and the effect of negative skin friction on pile foundations.
9 Bibliography


American Association of State Highway and Transportation Officials (2011a) AASHTO guide specifications for LRFD seismic bridge design – section 3.2 Performance criteria. Washington DC: AASHTO.

American Association of State Highway and Transportation Officials (2011b) AASHTO guide specifications for LRFD seismic bridge design – section 3.4.3 Performance criteria. Washington DC: AASHTO.

American Association of State Highway and Transportation Officials (2011c) AASHTO guide specifications for LRFD seismic bridge design – section 3.5 Selection of seismic design category. Washington DC: AASHTO.

American Association of State Highway and Transportation Officials (2011d) AASHTO LRFD bridge design specifications – section 10.5.4 Extreme events limit states. Washington DC: AASHTO.


California Department of Transportation (2011) *Guidelines on foundation loading and deformation due to liquefaction induced lateral spreading.* Los Angeles: California Department of Transportation.


Design guidance for bridges in New Zealand for liquefaction and lateral spreading effects


Appendix A: Mechanism and effects of liquefaction and lateral spreading

A1 Soil liquefaction and lateral spreading

Liquefaction is a phenomenon in which the strength and stiffness of a soil are reduced by earthquake shaking or other rapid cyclic loading. Liquefaction and related phenomena have been responsible for tremendous amounts of damage in historical earthquakes around the world.

A1.1 Mechanism of soil liquefaction

It is widely recognised that the basic mechanism of liquefaction in a deposit of loose saturated sand during earthquakes is the progressive build-up of excess pore water pressure due to application of cyclic shear stresses induced by the upward propagation of shear waves from the underlying rock formation (Terzaghi and Peck 1948; Seed and Lee 1966; Ghabousi and Wilson 1973; Marcuson 1978).

Soil liquefaction is a process in which over a very short period of time (several seconds or tens of seconds) during strong ground shaking, the soil transforms from its normal solid state into a heavy liquid mass. As a consequence of liquefaction, the soil essentially loses its strength and bearing capacity (i.e., the capacity to support gravity loads of heavy structures), causing sinking of heavy structures into the ground and/or slope movement. Conversely, light and buoyant structures (that have smaller mass density than the liquefied soil mass) will be uplifted and float above the surface.

Ground deformation associated with liquefaction takes various forms and is often excessive, non-uniform and involves large permanent vertical and lateral displacements commonly resulting in large cracks and fissures in the ground, substantial ground distortion and sand/silt/water ejecta covering the ground surface. The large pressures created in the groundwater during liquefaction are in excess of the equilibrium pressures, thus triggering flow of water towards the ground surface. Since the water pressures are very high, water will carry a significant amount of soil on its way towards the ground surface and eject it on the ground surface. This process inevitably leads to loosening of some parts of the foundation soils and often results in creation of local ‘collapse zones’, ‘sinkholes’ and ‘vents’ for pore pressure dissipation and flow of pore water.

Figure A.1 illustrates some features of the liquefaction process. Before the cyclic loading, the soil element is subjected to a confining stress due to the weight of the overlying soil. When cyclic shear stresses are applied, the element of loose sand tends to reduce in volume. However, if the duration of loading is short compared with the time required for drainage to occur, volume contraction cannot occur immediately. In order to keep the volume of contracting sand constant, some change in the existing stress system must take place. This stress change is generated by an increase in the pore water pressure and consequent reduction in the effective overburden stress. Hence, the contact forces between the individual soil particles are lost, resulting in softening and weakening of the soil particle skeleton.

When the state of sand packing is loose enough and the magnitude of cyclic shear stress is great enough, the pore pressure builds-up to a point where it becomes equal to the initial confining stress (Ishihara 1985). At this state, no effective stress, (i.e., inter-granular stress) is acting on the sand and the individual particles lose contact with each other. Such state is called liquefaction (see figure A.2).

After liquefaction, the individual particles start to sediment, expelling pore water towards the boundary of the deposit. After sedimentation has taken place throughout the depth, the excess pore water pressures reduce to zero, there is positive effective stress in the sand particle skeleton, and a new particle
arrangement is formed which may be denser, looser or similar to the density state of the soils before the occurrence of liquefaction. Figure A.1 illustrates one of the possible outcomes where the soils have densified. In principle, however, the fabric and new structure of the soil skeleton of liquefied soils is very weak and prone to re-liquefaction. The potential of soils to re-liquefy has been demonstrated by the widespread re-liquefaction of soils in the eastern suburbs of Christchurch during the 2010–2011 Canterbury earthquakes.

Figure A.1 Mechanism of liquefaction

As seen above, the process of soil liquefaction generally involves three phases:

1. Pore pressure build-up
2. State of liquefaction with nearly zero effective stress in the soil mass
3. Dissipation of excess pore water pressures.

The liquefaction process is depicted in figure A.2. The first phase in which the pore water pressure rises to the level of the effective overburden stress (and triggers liquefaction) is very short. In the 1995 Kobe earthquake, for example, only two or three seconds of intense ground shaking were required to trigger liquefaction in 15m to 20m thick reclaimed deposits. The rate of pore pressure build-up is primarily influenced by the deformational behaviour of the soil and ground motion characteristics (amplitude and number of intense cycles of ground shaking). The duration of the second phase (during which the effective
stress is nearly zero and the soil is liquefied) is much longer and depends on a number of factors (soil stratification, permeability of soils, presence and thickness of impermeable layers, duration of shaking and ground distortion caused by the shaking). During this phase, significant unbalanced excess pore pressures develop causing the flow of pore water and liquefied soil mass towards the ground surface. Sand boils are a typical consequence of such non-equilibrium pressures. The final phase is quite long and again very complex. It involves dissipation of excess pore water pressures, sedimentation of soil particles, solidification and reconsolidation of the deposit. During liquefaction and dissipation of pore pressures, phenomena such as secondary and progressive liquefaction may occur due to an upward flow of water and redistribution of void ratio (loosening of the soil).

Loose soils have more voids in their inherent structure (since they were not well compacted when deposited). Hence, when shaken, they show a large tendency for densification (contraction) which in turn leads to rapid pore water pressure build-up and eventual liquefaction in only few cycles of strong shaking. Since these soils are loosely packed and are highly deformable (compressible), liquefaction will be severely manifested and will result in very large ground movements and nearly complete loss of load carrying capacity. This is why loose soils are particularly prone to liquefaction and show very severe consequences of liquefaction. Conversely, very dense soils show very limited tendency for densification and hence produce low excess pore water pressures, and therefore they have much higher liquefaction resistance. Clays, clayey soils and plastic soils in general, derive stiffness and strength from an additional mechanism—cohesion, and hence are considered to be non-liquefiable. Softening of these soils and large deformation especially of soft clays and peat can produce severe ground deformation and affect the seismic behaviour of buildings and infrastructure, but their response mechanism is different from the soil liquefaction outlined above.

**A2 Liquefaction effects during earthquakes**

Liquefaction induces very large strains (ie the decrease in the thickness of a soil layer divided by its original thickness, which defines the relative deformation within the soil), typically in the order of several percent. Hence, if for example a 10m thick layer liquefies, the horizontal displacement of the top of the layer (eg at the ground surface) relative to its base (10m depth) could be in the order of 50m to 60cm.

A buried structure, including piled foundations in liquefied soil will be subjected to very large and non-uniform lateral loads from these ground movements and oscillation of the building. There are two particular locations where damage to piles in liquefied soils typically occurs near the pile top and at the interface between the liquefied soil and underlying unliquefied soil. In some cases, this interface is at large depth, and hence, it imposes serious constraints in identifying if there has been damage caused by the earthquake, and also in repairing or strengthening of the piles if required. The large ground distortion and highly non-uniform displacements caused by liquefaction often result in stretching of the ground imposing large loads and damage to foundations and horizontal infrastructure. Substantial total settlements, differential settlements and tilt of structures are common consequences of soil liquefaction. Hence, for engineering purposes, it is not the occurrence of liquefaction that is of prime importance, but its severity and its capability to cause damage to land, buildings and infrastructure. Adverse effects of liquefaction can take many forms (eg Kramer 1996; NRC 1985; Towhata 2008).

**A2.1 Flow failures**

Flow failures are the most catastrophic ground failures caused by liquefaction. These failures commonly displace large masses of soil tens of metres laterally. In some cases large masses of soil have travelled tens of kilometres down long slopes at velocities up to tens of kilometres per hour. Flows may consist of
completely liquefied soil or blocks of intact material riding on a layer of liquefied soil. Flows develop in loose saturated sands or silts on relatively steep slopes, usually with slope angles greater than 3\(^\circ\).

A2.2 Lateral spreads

Lateral spreading is a particular form of land movement associated with liquefaction that produces very large lateral ground displacements from tens of centimetres to several metres, and hence, is very damaging for buildings and infrastructure. Lateral spreading typically occurs in sloping ground or level ground close to waterways (e.g., river banks, streams, in the backfills behind quay walls). Even a very gentle slope in the ground (of several degrees) will create a bias in the cyclic loads acting on the soil mass during earthquakes which will drive the soil to move in the down-slope direction.

If the underlying soils liquefy then the liquefied soil mass (‘heavy liquid’) will naturally move down-slope and will continue this movement until equilibrium is re-established (or resisting forces reach the level of driving forces). Hence, displacement occurs in response to the combination of gravitational forces and inertial forces generated by an earthquake. The displaced ground usually breaks up internally, causing fissures, scarps, horsts and grabens to form on the failure surface.

Lateral spreads commonly disrupt foundations of buildings built on or across the failure, sever pipelines and other utilities in the failure mass, and compress or buckle engineering structures, such as bridges, founded on the toe of the failure (see figure A.3a). The process of spreading in backfills behind retaining walls is similar, with large ground shaking first displacing the retaining structure outwards (e.g., towards a waterway), which is then followed by lateral spreading in the backfills.

A2.3 Ground oscillation

Where the ground is flat or the slope is too gentle to allow lateral displacement, liquefaction at depth may decouple overlying soil layers from the underlying ground, allowing the upper soil to oscillate back and forth and up and down in the form of ground waves. These oscillations are usually accompanied by opening and closing of fissures and fracture of rigid structures such as pavements and pipelines. During the March 2011 earthquake in Japan videos were taken of ground oscillation movements in the Ciba region, near Tokyo, which have been described as ‘ground breathing’ (Towhata 2012).

Transient ground displacements of liquefied soils can be quite significant. One can easily calculate a ballpark figure of such displacements by integrating the shear strains (typically 1\% to 5\%) throughout the depth of the liquefied soil. For example, in the liquefied reclaimed deposits of Kobe harbour, the transient (cyclic) displacements of the liquefied soils during the strong shaking were on the order of ± 0.4m (Cubrinovski et al. 1996; Tokimatsu and Asaka 1998) and these large displacements were sufficient to cause substantial damage to pile foundations of high-rise buildings even in the absence of lateral spreading (Horikoshi et al. 2000). Hence, when analysing the response of bridges to strong ground shaking in potentially liquefiable soils, it is important to consider effects of both inertial loads due to vibration of the superstructure and kinematic loads due to displacements of the liquefying soils.

A2.4 Tilting and settlement of structures

When the soil supporting a building or other structure liquefies and loses strength, large deformations can occur within the soil which may allow the structure to settle and tip. For example, many buildings settled and tipped during the 1964 Niigata, Japan earthquake. The most spectacular bearing failures during that event were in the Kawagishi-cho apartment complex where several four-story buildings tipped as much as 60\(^\circ\). Apparently, liquefaction first developed in a sand layer several metres below ground surface and then
propagated upward through overlying sand layers. The rising wave of liquefaction weakened the soil supporting the buildings and allowed the structures to slowly settle and tip.

Figure A.3  Manifestations of liquefaction in the field: a) lateral spreading observed near Avon River following the 2011 Christchurch earthquake; b) sand boil observed during the 2000 Tottori-ken Seibu earthquake

A2.5  Ground settlement

In many cases, the weight of a structure will not be great enough to cause the large settlements associated with soil bearing capacity failures described above. However, smaller settlements may occur as soil pore-water pressures dissipate and the soil consolidates after the earthquake. These settlements may be damaging, although they would tend to be much less than the large movements accompanying flow failures, lateral spreading, and bearing capacity failures. The eruption of sand boils (fountains of water and sediment emanating from the pressurised, liquefied sand) is a common manifestation of liquefaction that can also lead to localised differential settlements.

A2.6  Buoyant rise of buried structures

Soil liquefaction can also induce buoyant rise of underground structures such as empty or partially filled pipelines and manholes. Normally, the uplift of the buried structure is prevented by resistance from the adjacent soil. However, when soil liquefies, the soil loses its resistance and starts to behave like liquid with a unit weight almost twice that of water. When the unit weight of the buried structure is less than that of the liquefied soil, floating of underground structures can occur.

A2.7  Increased lateral pressure on retaining walls

If the soil behind a retaining wall liquefies, the lateral pressures on the wall may greatly increase. As a result, retaining walls may be laterally displaced, tilt, or structurally fail, as has been observed for waterfront walls retaining loose saturated sand in a number of earthquakes.

A2.8  Sand boils

Sand boils are diagnostic evidence of elevated pore water pressure at depth and are indications that liquefaction has occurred. During earthquakes, sand boils are formed by water venting to the ground surface from zones of high pressure generated at shallow depth during seismic shaking (Housner 1958; Scott and Zuckerman 1973). The water, which may flow violently, usually transports considerable suspended sediment that settles and forms a conically shaped sand boil deposit around the vent (see figure A.3b). Massive sand boils can be very damaging for shallow foundations and buried lifelines since they often create local ‘collapse zones’, sinkholes and vents for pore water flow that lead to a complete loss of stiffness and bearing capacity in the foundation soils.
A3 Lateral ground deformations

Cyclic and permanent lateral displacements of liquefied soil are among the most troublesome liquefaction hazards for foundations, buried structures and lifeline facilities. Because these types of deformation involve the movement of competent soil, full passive pressure can be mobilised against an underground structure. Pipelines, bridges, pile foundations and other civil engineering structures on or within the extensional zone are typically cracked or torn apart. Almost all the alarming photos of widespread destruction from an earthquake are damage done by large permanent lateral movements of the soil surface.

A3.1 Field observations

Case histories of liquefaction-induced ground deformations during past earthquakes are important for understanding ground failure processes and the factors controlling these processes. Noteworthy is the fact that they provide sufficient data to be used in the verification of predictive models. In addition, the relation between geological and geotechnical conditions and the resulting deformations can be clearly evaluated. The two main techniques employed in measuring permanent lateral ground deformations include ground surveying and processing of aerial photographs and LiDAR.

A3.1.1 1964 Niigata earthquake

On 16 June 1964, an earthquake of M7.5 shook Niigata Prefecture. The earthquake caused extensive damage to various engineering structures such as buildings, bridges, harbours, river dikes and lifeline facilities. Measurements of permanent ground displacements were conducted by Hamada et al (1986) by comparing aerial photographs taken before and after the earthquake. Their studies reveal that large lateral spreading occurred in Niigata City, with displacements as large as 8.5m in the area of Hakusan Power Station and 8.8m on the left bank near Bandai Bridge (see figure A.4).

During the earthquake, Showa Bridge collapsed. According to eye witnesses, the bridge collapsed a few seconds after the earthquake had ended. A similar phenomenon was observed for the revetment at the bank of Showa Bridge (Yoshida et al 2011). These clearly show that the inertia forces associated with the earthquake motion were not the direct cause of the collapse of these structures.

A3.1.2 Nihonkai Chubu earthquake

On 16 May 1983 Nihonkai-Chubu earthquake, with a magnitude of 7.7, caused extensive damage to the coastal area of Tohoku region. One of the most severely damaged areas was Noshiro City, which is built on the sand dunes along the Japanese sea coast and alluvial plain of Yoneshiro River. Numerous cracks on gentle slopes indicated the occurrence of lateral spreading due to liquefaction.
Appendix A: Mechanism and effects of liquefaction and lateral spreading

Figure A.4  Permanent horizontal ground displacements in Niigata City during the 1964 Niigata earthquake (after Hamada et al 1986)

Figure A.5  a) Permanent displacements around Maeyama Hill in Noshiro City (after Hamada et al 1986); and (b) permanent displacements in vertical cross-sections of subsoils (after Towhata et al 1992)
Figures A.5a and A.5b show the permanent ground displacements measured in Noshiro City. Large ground displacements occurred along the gentle slopes of the sand dunes, with the maximum horizontal displacement exceeding 5m and the direction of displacement almost parallel to that of the slope. The observed displacements become smaller near the toe of the slope. The ground surface subsided by about 1m near the top of the slope where lateral displacements started, while the ground heaved at the foot of the slope. The major findings are:

- Many tension cracks are detected near the top of the liquefied slope. They are perpendicular to the direction of ground displacement.
- The permanent displacement is oriented downwards along the slope, suggesting the influence of gravity.
- Displacement is maximum at the top of the slope, while negligible at the bottom of the slope.
- Subsidence is predominant near the top of the slope, while uplift is important in the lower portion of the slope. Note that the vertical displacement is much smaller than the horizontal displacement.

### A3.2 Physical modelling

One of the shortcomings of field observations is that most of the findings reflect the displacement at the ground surface, ie information about sub-surface displacement has been scarce. Such a problem is solved by physical modelling using a 1-G shake table or centrifuge apparatus wherein the sub-surface deformation can be observed through a transparent side wall of a soil container. Some of the results of shaking table tests conducted by Towhata et al (1988; 1992) are presented here.

A model of a liquefied deposit with an embankment (figure A.6a) was shaken laterally. The shaking continued until the lateral displacement was stopped, indicating the maximum possible displacement. The top of the fill sank, while the toe was uplifted. Since the final configuration is almost flat, there seems to be no shear resistance in the liquefied sand. It is reasonable therefore to say that liquefied sand behaves in a similar way to liquid.

The response of a dry fill is investigated in figure A.6b. After shaking, the dry fill maintained its rigidity to some extent. After liquefaction, the top of the fill was still seen above the ground surface.

Figure A.6  a) Deformation of model with liquefied fill; and b) deformation of model with dry fill
Figure A.7a shows a model ground which is inclined and has a gravelly unliquefied crust at the surface.

Figure A.7 Deformation of subsoil with gravelly surface layer, a) before shaking; b) after liquefaction

Water was supplied at the upper lateral boundary and was drained out from the lower end, causing a realistic seepage flow. Upon liquefaction, both liquefied material and the surface gravel layer moved together without slip at the interface. Figure A.7b shows that the gravelly layer was compressed in the lateral direction. Since it did not liquefy, it appears to have some rigidity, resisting against its lateral compression. Hence, the liquefied subsoil cannot flow so freely as in the case without a surface crust.

The major findings of the small-scale shaking table tests are:

- Liquefied sand behaves in a similar way to liquid.
- The lateral displacement in liquefied layer is largest at the surface, while negligible at the base.
- The unsaturated layer at the surface moves together with the liquefied subsoil without slipping at the interface.
- The permanent displacement is caused by gravity force. The cyclic inertia force triggers liquefaction, but does not affect the displacement significantly.

### A4 Evaluation of liquefaction

The conventional method (state-of-the-practice) for liquefaction assessment involves the following evaluation steps.

1. **Liquefaction susceptibility**: In this step, based on the grain-size composition and plasticity of soils, it is determined whether the soils at the site in question are liquefiable or not. If the soils are deemed non-liquefiable, then further liquefaction evaluation is not required (Bray and Sancio 2006; Idriss and Boulanger 2008; NZGS 2010).

2. **Liquefaction triggering**: If the soils (or some of the layers) are liquefiable, then a triggering analysis is conducted to determine whether (and which) soil layers are going to liquefy when shaken by a particular ground motion (the design earthquake) specified in terms of peak ground acceleration (PGA) and earthquake magnitude (Mw). In this analysis step, a factor of safety against triggering of liquefaction is calculated as a ratio of the liquefaction resistance (cyclic strength of the soil, or resistance capacity) and cyclic stresses in the soil induced by the design earthquake (seismic load/demand) (Youd et al 2001; Seed and Idriss 1982; Idriss and Boulanger 2008). In the simplified procedure, the PGA is used as a measure for the amplitude of ground shaking while the earthquake (moment) magnitude (Mw) is used as a proxy for the duration of shaking (ie number of significant stress cycles).
Liquefaction-induced ground deformation: In this step, consequences of liquefaction in terms of ground displacements/deformation are estimated for a free field (land not affected by structures or built environment) level ground or sloping ground conditions. Using the computed factor of safety and estimated thickness of the liquefied soils in the triggering analysis, liquefaction-induced settlements and lateral ground displacements are calculated using empirical methods (e.g., Ishihara and Yoshimine 1992; Tokimatsu and Seed 1987; Tokimatsu and Asaka 1998; Zhang et al. 2002). Similar approaches are used for estimating lateral ground displacements due to spreading (e.g., Hamada et al. 1987; Youd et al. 2002; Tokimatsu and Asaka 1998; Zhang et al. 2004).

Impacts of liquefaction on structures and their seismic performance: Using the ground displacements and loads estimated in the previous step, the impacts of liquefaction on structures are then analysed. This includes calculation of seismic loads acting on the structure, displacements, deformation and damage to the structure (structural members and overall structural system).

Countermeasures against liquefaction: In the final step of the assessment, countermeasures against liquefaction are considered either to prevent the occurrence of liquefaction or to reduce its impacts on ground deformation and structures and bring their seismic performance within tolerable limits. Ground improvement and foundation strengthening are the two principal mechanisms used as countermeasures against liquefaction.

The following sections address the first three evaluation steps given above and refer to some alternative methods.

A4.1 Liquefaction susceptibility

The key question to answer in the assessment of liquefaction susceptibility is whether the soils at the site in question are liquefiable or not. Many factors affect liquefaction susceptibility including grain-size composition, plasticity of soils and age of deposits.

Traditionally, empirical criteria based on the grading curve (compositional criteria) have been used for assessment of liquefaction susceptibility (see figure A.8). While these criteria are easy to implement and hence are quite practical, it is now well established that they are very approximate and essentially of little predictive value.

Figure A.8 Relationship between grain size characteristics and liquefaction potential (after Tsuchida 1971)

It is widely accepted that sands, non-plastic silts, gravels and their mixtures form soils that are susceptible to liquefaction. Clays, on the other hand, do not exhibit typical liquefaction features (even though they may significantly soften and fail under cyclic loading) and therefore are considered non-liquefiable. The key difference in the context of liquefaction is that the pore pressure rise in clayey soils is typically limited to 60%-80% of the overburden stress (whereas liquefiable soils generate 100% rise in the excess pore
water pressure). The largest problem exists in the evaluation of liquefaction susceptibility of fine-grained soils that are in the transition zone between the above mentioned liquefiable soils and non-liquefiable clays. Based on the predominant matrix structure of fines-containing sands, we can distinguish several sub-groups of these soils as below:

- sands (gravelly sands) with up to 10%-20% fines
- sands (gravelly sands) with 20%-40% fines
- fine-grained soils with over 50% fines.

The first group is basically 'controlled' by a sand-matrix with the fines filling the voids in-between sand particles. The third group is a fine-grained matrix structure with large sand particles 'floating' in the fine-grained matrix. Soils of the second group are in the transition zone between those with a sand-matrix and fine-grained matrix (Cubrinovski et al 2010). This classification is useful for further discrimination between liquefiable and non-liquefiable soils based on plasticity criteria. Idriss and Boulanger (2008) recommend a plasticity value of $\Pi = 7$ as a threshold for separating between liquefiable ($\Pi \leq 7$) and non-liquefiable soils ($\Pi > 7$). They have adopted this rule to apply to soils with fines content of up to 50%. The guidelines for the Greater Vancouver area as well as the NZGS (2010) guideline adopt slightly more rigorous criteria as follows: i) $\Pi < 7$ susceptible to liquefaction: soils classified under this category should be considered as ‘sand-like’ and evaluated using the simplified procedure for sands and non-plastic silts presented in these guidelines; ii) $7 < \Pi < 12$ ($30\% < FC < 50\%$) moderately susceptible to liquefaction: soils classified under this category should be considered as ‘sand-like’ and evaluated either using the simplified procedure for sands and non-plastic silts or using site-specific studies including laboratory tests on good-quality soil samples; iii) $\Pi > 12$ ($FC > 30\%$), not susceptible to liquefaction: soils classified under this category are assumed to have ‘clay-like’ behaviour and are evaluated using the procedure for clay-like soils.

The first group of soils are closer to clean sands, and hence rigorous plasticity criteria (higher $\Pi$ value) are needed in order to deem the soil non-liquefiable (especially because the amount of fines is very low, $F_c = 10\%-20\%$). The second group of ‘transitional soils’ is the most difficult to characterise; in the absence of specific data and evidence, these soils should be conservatively evaluated using the same criteria as for the first group. The soils in the third group are fine-grained (silts or clays) and hence should be assessed using different plasticity criteria (lower $\Pi$ value can be justified by a high fines content of over 50%). Recent studies by Boulanger and Idriss (2006) and Bray et al (2004) provide criteria based on fines content and plasticity index for fines-containing sands and fine-grained soils. It is important to point out that:

- there are no widely accepted criteria for liquefaction susceptibility, and
- soils that are deemed non-liquefiable can undergo significant deformation due to cyclic softening (evaluation of seismic deformation should not be limited to liquefiable soils).

The age of the deposit is an important factor to consider when assessing liquefaction susceptibility. Young Holocene sediments and man-made fills in particular are susceptible to liquefaction (Youd and Perkins 1978). It has been generally accepted that aging improves liquefaction resistance of soils, however, these effects are difficult to quantify and are usually not directly addressed in design procedures.

### A4.2 Liquefaction triggering

The evaluation of whether liquefaction will occur or not for a given site is very important in the design of structures. For this purpose, two approaches are currently available:
1  **Semi-empirical methods** where a set of independent procedures is used to estimate the stresses induced by the earthquake together with empirical charts/equations to calculate the liquefaction triggering.

2  **Numerical methods** where a complete evaluation of liquefaction including triggering, ground deformation and effects on structures in a complex time history analysis is performed.

For the semi-empirical or ‘simplified’ methods, calculation or estimation of two variables is required for evaluation of liquefaction resistance of soils: 1) the seismic demand on a soil layer, expressed in terms of the cyclic shear stress ratio (CSR); and 2) the capacity of the soil to resist liquefaction, expressed in terms of the cyclic resistance ratio (CRR).

### A4.2.1 Cyclic shear stress ratio

The most common approach to characterisation of earthquake loading is through the use of cyclic shear stresses. By normalising the cyclic shear stress amplitude by the initial effective vertical stress, a CSR can represent the level of loading induced at different depths in a soil profile by an earthquake. There are, in general, two different procedures for evaluating the cyclic shear stresses:

1. Site response analyses may be performed, using different computer programs such as SHAKE (Schnabel et al 1972), NERA (Bardet and Tobita 2001) and DeepSoil (Hashash and Park 2001).

2. A simplified approach may be used to estimate CSR as a function of peak ground surface acceleration amplitude (eg Seed and Idriss 1971; 1982; Youd et al 2001; Idriss and Boulanger 2008; JRA 1996; AIJ 2001).

### A4.2.2 Cyclic resistance ratio

The cyclic resistance to liquefaction of in-situ deposits is evaluated from the penetration resistance obtained using standard penetration tests (SPT) or cone penetration tests (CPT) or from laboratory testing of high-quality samples (see figure A.9).

**Figure A.9 Methods of estimating the cyclic resistance ratio**

In North America, for example, charts have been proposed by correlating the SPT $N$-value (Seed and Idriss 1971; Seed et al 1985), CPT $q_c$-value (Robertson and Wride 1998; Suzuki et al 1995; Moss et al 2006),
shear wave velocity (Andrus and Stokoe 1997; 2000) and seismic dilatometer parameters (Monaco et al 2005; Marchetti et al 2008) and the estimates of the CSR of a number sites which had or had not manifested evidence of liquefaction during major earthquakes in the past (eg Youd et al 2001; Seed et al 2003). By plotting the \( CSR(N)_1 \) (or \( CSR-q \)) pairs for cases in which liquefaction was and was not observed, a curve that bounds the conditions at which liquefaction has historically been observed can be drawn. This curve, when interpreted as the maximum CSR for which liquefaction of a soil with a given penetration resistance can resist liquefaction, can be thought of as a curve of CRR.

In Japan, on the other hand, the results of cyclic shear tests on high-quality undisturbed samples from in-situ sand deposits are correlated with the penetration resistance obtained at nearby sites to establish the chart (eg Ishihara 1993; 1996; JRA 1996).

### A4.2.3 Factor of safety against liquefaction, \( F_L \)

The liquefaction potential is usually expressed in terms of factor of safety against liquefaction, \( F_L \), and is given by:

\[
F_L = \frac{CRR}{CSR}
\]  
(Equation A.1)

If \( F_L < 1.0 \), the shear stress induced by the earthquake exceeds the liquefaction resistance of the soil and liquefaction will occur. Otherwise, when \( F_L \geq 1.0 \), liquefaction will not occur.

### A4.2.4 Effective stress analyses

A more detailed investigation of the response of soils to cyclic loading can be performed using effective stress analyses (ESA). These involve seismic response and liquefaction process modelling using fully coupled equations for the granular solid and the pore fluid the response of soils (as obtained from laboratory testing) in terms of generation and dissipation of excess pore water pressure and the associated development of ground deformation. These are typically implemented through finite element or finite difference method. Some of the more popular computer programs used are FLAC (Itasca 1998), PLAXIS (Plaxis bv 2011), DIANA (Diana Analysis 2001).

### A4.3 Estimating cyclic ground displacements

As mentioned in section 2.2.2, liquefaction at depth may decouple overlying soil layers from the underlying ground and allow the upper soil to oscillate back and forth and up and down in the form of ground waves. This deformation typically occurs in flat ground or gentle slope where lateral permanent displacement would not occur. These oscillations are usually accompanied by opening and closing of fissures and fracture of rigid structures such as pavements and pipelines. Such back and forth movement of the liquefied soil, with the surface crust riding on top, is also a major hazard to pile foundations; hence estimation of the magnitude of the cyclic component is necessary for efficient design of underground structures.

However, very few studies have been done to date to estimate the magnitude of cyclic ground displacements during liquefaction. The only available approach is based on the studies of Tokimatsu and Asaka (1998) following the 1995 Kobe earthquake. In this method, the peak cyclic displacements are expressed in terms of simplified charts correlating the maximum cyclic shear strain that develop in the liquefied layer with the cyclic stress ratio and SPT blow count, as shown in figure A.10. In the figure, \( N_a \) is the normalised SPT N-value adjusted for the effect of fines fine content, ie this is the equivalent SPT N-value for clean sand. That is, \( N_a = (N)_{\text{tot,cr}} \).
In order to determine the peak cyclic deformation, the adjusted SPT N-values, \( N_a \), and equivalent CSRs during earthquake, \( \tau_{av}/\sigma_{v0}^{'} \) at various depths are evaluated, from which the cyclic shear strain \( \gamma_{cy} \) is estimated for each depth. Then, the cyclic ground displacement profile \( f_c(z) \) is determined by integrating \( \gamma_{cy} \) upwards from the bottom of the liquefied layer, assuming \( \gamma_{cy} \) develops in the same direction. A schematic diagram showing this procedure is shown in figure A.11.

A4.4 Estimating permanent lateral displacements

Evaluation of permanent lateral ground displacements is a difficult non-linear problem. However, it is important as the evaluation of the damaging effects of liquefaction at a site requires the ability to predict the magnitude and spatial distribution of lateral ground displacements. It is worth mentioning that even
though the prediction of whether a site will liquefy can be done with reasonable degree of confidence, there is no generally accepted method for evaluating lateral displacements. Current methods can be generally classified as follows:

A4.4.1 Empirical approach

1. The most straightforward approach to estimating horizontal displacements due to liquefaction is to compile a database of known displacements and to correlate those displacements with measurable parameters. Note that choosing the parameters which should be considered is a formidable task since there are many geotechnical, topographical and seismological factors affecting the results. Moreover, the accurate measurement and compilation of in-situ measurements, and the relevant parameters, is also difficult.

2. Multiple linear regression analysis was conducted by Bartlett and Youd (1995) to take into account a great number of variables in the predictive equation. They analysed 43 detailed factors from eight different earthquakes to account of seismological, geological, topographical and geotechnical effects on lateral ground displacements due to liquefaction. Youd et al (2002) later corrected and updated the original analysis, and gave two equations for lateral ground displacement, $D_H$, one for movement down a gentle slope and another towards a free face, as follows:

For sloping ground relation:

$$\log D_H = -16.213 + 1.532M - 1.406 \log R^* - 0.012R + 0.338 \log S + 0.540 \log T_{15} + 3.413 \log(100 - F_{15}) - 0.795 \log(DS_{015} + 0.1)$$

(Equation A.2a)

For free-face relation:

$$\log D_H = -16.713 + 1.532M - 1.406 \log R^* - 0.012R + 0.592 \log W + 0.540 \log T_{15} + 3.413 \log(100 - F_{15}) - 0.795 \log(DS_{015} + 0.1)$$

(Equation A.2b)

where $M$ is the earthquake moment magnitude, $R$ is the horizontal distance from the site in question to the nearest bound of seismic energy source (km), $R^*$ is a modified source distance ($R^* = R + 10^{0.89M - 5.64}$), $W$ is the ratio of free face height to distance to free face (%), $S$ is ground slope (%), $T_{15}$ is the cumulative thickness (m) of saturated sandy layers with normalised SPT N-value ($N_{15} < 15$, $F_{15}$ is the average fines content of saturated granular layers within $T_{15}$, $S_{015}$ is the average mean grain size (in mm) of layers included in $T_{15}$. The above formulas give results comparable to those of observed displacements within a factor of plus or minus two.

Bardet et al (2002) and Rauch and Martin (2000) also developed empirical models for lateral spreading displacements based on regression techniques using compiled data from lateral spreading case histories. Note that these empirical methods of estimating lateral spreading are based on databases that do not cover the full range of conditions encountered in practice. Their use therefore requires full awareness of the limits of the supporting case history database. The key shortcoming of these methods is that they have little physical basis, and for this reason Ashford et al (2011) state that these methods cannot be extended to approach embankments.

A4.4.2 Semi-empirical approach

Another approach is to estimate the permanent strains that are expected within the liquefied zones and then integrate those strains over the depth to obtain an estimate of the potential lateral displacement at
the ground surface. Then, the lateral displacement is estimated by calibrating the potential displacement with case history observations.

Thus, the first step in this method is integration of shear strain profiles estimated in conjunction with SPT and CPT based liquefaction analyses. The maximum potential shear strains may be estimated using existing relationships, such as the three SPT-based correlations compared in figure A.12. The computed ground surface displacement is known as the lateral displacement index, or simply LDI. Based on calibration with case histories, two equations have been proposed for the lateral displacement, LD (Zhang et al 2004).

For sloping ground:

\[
LD = (S + 0.2) \cdot LDI \quad \text{for } 0.2\% < S < 3.5\%
\]  
(Equation A.3a)

For free face:

\[
LD = 6 \cdot (L/H)^{0.8} \cdot LDI \quad \text{for } 4 < L/H < 40
\]  
(Equation A.3b)

In the above equation, \( H \) is the free-face height, \( L \) is the distance of the target point to free face, and \( S \) is ground slope (%). This method does not account for two- or three-dimensional effects; therefore, the results for individual borings can be misleading on their own. A benefit of the integration of strain method is that an estimate of the soil displacement profile is obtained over the depth of the foundation, which can in turn be used as an analysis input.

Figure A.12  Comparison of the relationship among CSR, SPT, \( (N_{l})_{max} \), and maximum shear strain for three levels of maximum shear strain (Idriss and Boulanger 2008)

A4.4.3  Direct computation

The direct computation of seismically induced ground displacements has been a topic of interest in the past few years. Numerous analytical and numerical techniques have been developed, most of which are based on limit equilibrium, ie if the driving stress is greater than the available strength, the structure
becomes unstable and some form of displacement will occur until enough resistance is mobilised to counteract the driving stresses.

One of the earliest and probably the most widely used type of analysis is that proposed by Newmark (1965). The ground displacement is calculated in this method based on a single degree of freedom system and rigid plastic soil. The earthquake load is represented by a pseudo-static load. When the earthquake-induced acceleration is less than a certain critical value, no sliding will occur. However, when the critical value is exceeded, permanent ground displacement will take place. The displacement is then derived by doubly integrating the acceleration-time history in excess of the critical value (see figure A.13). Although the procedure is quite simple, the determination of critical value is complicated and the calculated displacements depend on the accuracy of this critical acceleration.

Note that the above method is based on rigid body movement of soil. When considering liquefied soil, however, the absence of rigid soil makes the application of the model difficult. Moreover, in its present form, the model cannot account for the large strains and displacements that occur within the zone of liquefaction.

An approach based on the Newmark sliding block model was proposed by Byrne (1990) to incorporate a more thorough description of post-liquefaction behaviour of sand. In his model, the rigid-plastic spring was replaced by a non-linear one representing the stiffness of the liquefied layer with its residual strength incorporated. In this approach, the permanent displacement $D$ is calculated from:
where $G_L$ is the shear modulus of the liquefied soil, $S_r$ is the residual strength of the liquefied soil, $\gamma_{\text{lim}}$ is the limiting shear strain, $T_L$ is the thickness of liquefied layer, $\tau_{st}$ is the average shear stress required for static equilibrium, $m$ is the mass of soil above the failure surface and $v_0$ is the velocity of the mass at the instant of liquefaction. The first part of equation A.4 is a cubic equation which can be solved using Newton’s equation.

**A4.4.4 Finite element method (FEM) based approach**

Recent trends in computing liquefaction-induced ground deformations involve representing the behaviour of liquefied soil through constitutive models and applying them through finite element-based numerical techniques. One early technique proposed by Lee (1974) is based on the assumption that the deformation is due to softening of the soil as a result of seismic shaking so that after the earthquake, the deposit will deform to a new condition compatible with the new softened stiffness of the soil. The softened parameters are based on laboratory tests in which the in-situ stress conditions before and during the earthquake are simulated. Finite element analyses are then performed using the normal and reduced/softened moduli to calculate the liquefaction-induced ground displacement.

However, many of the present available techniques in evaluating permanent displacements employ non-linear dynamic stress-strain behaviour of soil in conjunction with plasticity theory. At present, a number of numerical codes (with appropriate constitutive models for soils) exist to model the post-liquefaction behavior of soils, eg DIANA, FLIP, TARA, ADINA. An exhaustive compilation of the state-of-the-art work in this area can be found in the proceedings of the VELACS meeting (Arulanandan and Scott 1993). A typical FEM-based result is shown in figure A.14.

**Figure A.14** Calculating for ground displacements by finite element analysis
Appendix A: Mechanism and effects of liquefaction and lateral spreading

A5 Impact of liquefaction and lateral spreading on bridges: review of case histories

A5.1 Niigata earthquake

During the 1964 Niigata earthquake ($M=7.5$), several bridges were damaged by liquefaction-induced ground displacements. An example of damage is the collapse of Showa Bridge, shown in figure A.15a. Five simple steel girders of about 28m span collapsed between piers P2 and P7. Measurements after the earthquake indicated ground displacements in the order of 5m in the left bank, and the liquefied layer was estimated to be about 10m thick. Figure A.15b shows the deformation of the steel pipe pile of Pier P4, which was extracted after the earthquake. The piles were bent toward the right bank at a position 7m to 8m below the river bed. The damage to the piles can be explained by considering a scenario wherein a 10m thick soil layer liquefies in the left bank area near the Showa Bridge, causing large ground displacement toward the river. Anecdotal evidence suggests that the bridge failed approximately 70 seconds after the strong shaking (Yoshida et al 2011).

Figure A.15  a) Collapsed Showa Bridge (photo from EERC Archive); and b) damaged steel pipe pile of Pier P4 of Showa Bridge (after Hamada et al 1987)

A5.2 1995 Hyogoken-Nambu earthquake

Nishinomiya Port Bridge, which links two reclaimed islands – Koshien Beach and Nishinomiya Beach, is a part of Route Bay Shore Line linking Osaka City and Rokko Island. It was completed in 1993 considering a design coefficient $k_h=0.3$. The superstructure consists of Nielsen Lohse girders and simple composite steel box girders, while the foundation is caisson-type.

During the 1995 Hyogoken-Nambu Earthquake, one of the steel box girders set on fixed bearing supports on top of the bridge pier collapsed, as shown in figure A.16. Subsequent analyses showed that the caisson supporting the bridge pier rotated and translated laterally toward the channel as a result of 1m~2m lateral spreading of the liquefied soil adjacent to the quay wall. Moreover, the bridge pier deformed, resulting in
a total lateral displacement of the top of pier by 87cm. Such large lateral displacement caused the collapse of one of the steel box girders.

**Figure A.16  Collapsed girder of Nishinomiya Port Bridge**

Large-diameter piles supporting massive bridge structures and storage tanks in proximity to the revetment line also suffered serious damage due to liquefaction and spreading (Ishihara and Cubrinovski 1998). A typical example of such damage was seen in Pier 211 of the Hanshin Bay Route no. 5 which was located in the southernmost part of Uozakihama Island. Side views of Pier 211 and a plan view of its foundation are shown in figure A.17a (HHA 1996). The pier was supported on 22 cast-in-place RC piles, 1.5m in diameter and 41.5m long. The damage to the piles summarised from borehole camera recordings of two inspected piles is shown in figure A.17b. The damage at the pile head was supposedly caused both by spreading loads and by inertial loads from the superstructure during the intense ground shaking. By and large, however, the cracks were predominantly found at depths corresponding to the interface between the liquefied layer and the underlying non-liquefied layer. This type of damage was typically observed in piles located near the waterfront and it could be attributed solely to the excessive lateral ground movement due to spreading.

**A5.3  1995 Kobe earthquake**

The following summary of typical liquefaction (spreading)-induced damage to pile foundations in the 1995 Kobe earthquake is adapted from Cubrinovski (2006).

A large number of pile foundations of buildings, storage tanks and bridge piers located in the waterfront area of Kobe were damaged in the earthquake (eg Ishihara and Cubrinovski 1998; 2004; JGS 1998; Tokimatsu and Asaka 1998). In order to inspect the damage to piles, detailed field investigations have been conducted on selected piles by means of several inspection techniques. For example, features of the damage were investigated by lowering a borehole video camera down the hole of pre-cast hollow-cylindrical piles to examine the development of cracks around the pile-wall. In the case of cast-in-place RC piles, a hole was first drilled into the piles and then a video camera was lowered into the hole to inspect the distribution of cracks. In addition, a survey of pile deformation was carried out by lowering an inclinometer down the hole; by integrating the measured data on tilts through the depth, the lateral displacement and hence deformation of the pile was obtained. In some cases, the top part of the pile foundation was exposed by excavating the surface soils and visual inspection of the damage to the pile head was then carried out. Characteristic damage features of piles located within the lateral spreading zone are briefly described below by using three representative case histories.
Appendix A: Mechanism and effects of liquefaction and lateral spreading

A5.3.1 Mikagehama tank TA7

The performance of the pile foundation of an oil-storage tank, with a diameter of approximately 15m and capacity of 2450kl, was investigated in detail by Ishihara and Cubrinovski (2004). The tank, which was located about 25m to 40m inland from the quay walls, was supported on 69 pre-stressed high-strength concrete piles, 23m long and 45cm in outer diameter. A cross-sectional view of the tank and its foundation is shown in figure A.17a. During the earthquake, extensive liquefaction developed in the reclaimed soils with a seaward movement of the quay wall of about 1m and consequent lateral spreading in the backfills. It was estimated that the permanent lateral ground displacement, at a distance corresponding to the location of the tank, was about 30cm to 60cm. After the earthquake, two of the piles were investigated using the aforementioned inspection methods. The outcome of the borehole camera recordings is summarised in figure A.17b where the observed distribution of cracks is shown for the inspected piles. The piles developed multiple cracks and suffered the worst damage at a depth of approximately 12m to 14m, which corresponds to the depth at the interface between the liquefied layer and the underlying non-liquefied layer.

Figure A.17 Mikagehama tank TA7: a) side view of the tank and its foundation; b) observed damage to piles

A5.3.2 Uozakihama Bridge Pier 211

Large-diameter piles supporting massive bridge structures and storage tanks in proximity to the revetment line also suffered serious damage due to liquefaction and spreading (Ishihara and Cubrinovski 1998). A typical example of such damage was seen in Pier 211 of the Hanshin Bay Route no. 5 which was
located in the southernmost part of Uozakihama Island. Side views of Pier 211 and a plan view of its foundation are shown in figure A.18a (HHA 1996). The pier was supported on 22 cast-in-place RC piles, 1.5m in diameter and 41.5m long. The damage to the piles summarised from borehole camera recordings of two inspected piles is shown in figure A.18b. The damage at the pile head was supposedly caused both by spreading loads and by inertial loads from the superstructure during the intense ground shaking. By and large, however, the cracks were predominantly found at depths corresponding to the interface between the liquefied layer and the underlying non-liquefied layer. This type of damage was typically observed in piles located near the waterfront and it could be attributed solely to the excessive lateral ground movement due to spreading.

Figure A.18  Uozakihama Bridge Pier 211: a) side view of the pier and plan view of its foundation; b) observed damage to piles (Hanshin Highway Authority 1996)

A5.3.3  Higashi-Nada building

The last case history to be introduced is that of a pile foundation of a three-story building in Higashi-Nada (Tokimatsu and Asaka 1998). The building was located 6m from the quay wall and was supported by 38 prestressed concrete piles, 40cm in diameter and about 20m long. A cross-sectional view of the building and its foundation is shown in figure A.19a while a plan view of the foundation is shown in figure A.19b. The permanent spreading displacements at the site of the building have been estimated at about 80cm to 100cm while detailed inspections of two of the piles revealed serious damage to the piles at the pile head and at a depth corresponding to the interface between the liquefied layer and the underlying non-liquefied layer. The largest damage was found for the pile in proximity to the quay wall, which suffered failure about 3m to 4m below the pile top, as indicated in figure 6a. Tokimatsu and Asaka (1998) have shown that this failure pattern could be induced by pile-group effects or cross-interaction of piles subjected to variable magnitudes of lateral ground displacement.
Cubrinovski et al (2009) summarise the key findings with regard to the damage to the piles as follows:

1. Most of the piles suffered the largest damage at the pile top and in the zone of the interface between the liquefied layer and the underlying non-liquefied layer (figure A.19).

2. Piles in the zone of large lateral spreading displacements were consistently damaged at depths corresponding to the interface between the liquefied layer and the underlying non-liquefied layer. Since this interface was at large depths where inertial effects from the superstructure are known to be less significant, this damage can be attributed to the lateral loads arising from the excessive ground movement due to spreading.

3. Damage at the pile head was encountered both for piles in the free field and piles located within the lateral spreading zone, near the quay walls. Both inertial loads from the superstructure and kinematic loads due to lateral ground displacements contributed to the damage at the pile head.

4. The variation of lateral spreading displacements with the distance from the waterfront may result in different lateral loads being applied to individual piles, depending on their position within the pile-group (Cubrinovski and Ishihara 2004). This in turn may lead to significant cross-interaction effects and consequent bending deformation and damage to piles in accordance with these interaction loads from the pile-cap-pile system. In some cases where these pile-group effects were significant, the piles failed within the liquefied layer or at least several metres below the pile head.

A5.4 2010–2011 Christchurch earthquakes

The 2010–2011 earthquakes triggered widespread liquefaction throughout the eastern suburbs of Christchurch and its CBD (Cubrinovski et al 2014). Figure A.20 indicates areas within Christchurch that liquefied during the 4 September 2010, 22 February 2011 and 13 June 2011 earthquakes. In the 23 December 2011 event the extent of liquefaction was similar to that induced in the 13 June 2011
earthquake. The liquefaction map for the Christchurch earthquake indicates the location and severity of liquefaction manifestation, though the severity was non-uniform and variable even within one colour zone. The Christchurch liquefaction was arguably one of the most extensive and severe liquefaction in native soils on record. Over 400,000 metric tons of silt/sand ejecta was removed in the (partial) clean-up of the streets and properties after the Christchurch earthquake. In the worst-hit areas widespread liquefaction occurred in multiple events, with many sites severely liquefying three or four times during the 2010–2011 earthquake sequence (Cubrinovski et al 2011).

Although structural failure of commercial buildings led to the greatest casualties in the 2011 M6.3 Christchurch earthquake, by far the most significant damage to residential buildings, bridges and other lifelines in the Canterbury earthquakes was the result of liquefaction and associated ground deformations. Liquefaction occurred in areas which are known to have a high potential to liquefy – former river channels, abandoned meanders, wetlands and ponds. Immediately following some of the largest aftershocks from the 2010 M7.1 earthquake, liquefaction re-occurred in some of these areas. During the 2011 M6.3 earthquake, liquefaction was more widespread and vents continued to surge during the aftershocks immediately after the event. The impact of sand boils and cracks caused by lateral spreading was that parts of the suburbs were inundated with sand and silt – in places there were layers of ejected soil that were many tens of centimetres thick.

There are over 800 road, rail and pedestrian bridges in Christchurch and the surrounding region. Road bridges, which are the subject of this paper, are typically two or three span, short- to moderate-length bridges (20m to 70m long). Overall, in the 2010–2011 earthquakes, road bridges performed relatively well compared with other engineering structures (Palermo et al 2011; Wotherspoon et al 2011). They suffered low to moderate damage and all bridges but one were in service almost immediately after each significant event. A general overview of the damage to road bridges (longer than 10m) in the urban area of Christchurch, as judged by visual inspections of Opus engineers for Christchurch City Council (CCC 2011), is depicted in figure A.20.

A5.4.1 Damage to bridges in non-liquefied areas

The Darfield earthquake did not cause any significant damage to bridges in non-liquefied areas (Palermo et al 2010) while a small number of bridges suffered damage in such areas in the Christchurch earthquake. The three-span Horotane Valley Overpass, a twin bridge located ~1.5km from the source of the Christchurch earthquake, suffered abutment damage due to incipient slope failure of the approach embankments and fine cracking on the lower half of all piers. Bolts attaching the deck beams to the abutment seat extension had sheared off, and the ties between spans and at the abutments had elongated and pulled out. There was only minor damage to this bridge during the Darfield earthquake. The six-span Port Hills Overpass, a twin bridge less than 200m from the Horotane Overbridge, developed flexural cracking on the lower half of the majority of its piers due to transverse ground shaking, and the linkages between the span and the abutments had elongated.
Appendix A: Mechanism and effects of liquefaction and lateral spreading

The most significant bridge damage outside liquefied areas in the Christchurch earthquake was to the Moorhouse Avenue Overpass, an 11-span reinforced concrete (RC) structure on the southern edge of the CBD. The structure was constructed in three separate sections, with expansion joints passing down the centre of two sets of piers. Steel rod linkages were later installed across the western expansion joint, tying the central and western sections together. The absence of linkages at the eastern expansion joint resulted in an irregular transverse response during the earthquake and a higher displacement demand, leading to significant shear cracking and buckling of the piers at the eastern expansion joint, affecting vertical and lateral load carrying capacity. The columns had widely spaced transverse reinforcement, making the structure susceptible to a brittle failure mechanism. Deck pounding at the eastern abutment also resulted in spalling and bar buckling in the deck girders. The overpass was closed for more than five weeks following the earthquake while temporary strengthening work was carried out (Wotherspoon et al 2011).

A5.4.2 Structural issues

Although the Canterbury earthquakes did not cause the collapse of any bridges, some structural issues emerged:

- Integral cast-in-place bridges, typically constructed prior to the 1950s performed better than precast concrete bridges. The sturdy configuration of these bridges minimised the transverse column drift demand of the Canterbury earthquakes to less than 0.5%.
- Plastic hinges in the bridge columns have been properly detailed and in many cases the damage was limited to concrete spalling and initiation of yielding of the bars.
- Deck linkages are quite widely adopted in New Zealand as part of the New Zealand Retrofit Program (Chapman et al 2005); their function is limited to prevent deck unseating. Bridges in Christchurch retrofitted with linkages and bolts performed well, even though some failures were recorded between the deck and the abutment due to slope failure or liquefaction-induced displacements.
A5.4.3 Damage to bridges in liquefied areas

Most of the damage to bridges was due to liquefaction of the foundation soils and lateral spreading of the river banks. On the Avon River, practically all road bridges downstream of the Fitzgerald Bridge (figure A.21) were substantially affected by lateral spreading.

Figure A.21 shows an aerial view of the four bridges (case studies) presented herein: a) Fitzgerald Bridge, b) Dallington (Gayhurst) Bridge, c) ANZAC Bridge and d) South Brighton Bridge. The solid lines indicate the locations of the transects along which lateral spreading measurements were conducted by the ground surveying method, with the numbers at the tip of the transects indicating the maximum displacements at/near the river banks measured after the Christchurch earthquake and Darfield earthquake (in brackets). Also shown in the figure in a summary form are ground displacements estimated on the basis of LiDAR data (CERA 2012). There are several important observations from the data in figure A.21. First, the data obtained from the ground surveying and LiDAR are consistent with each other and show similar displacements for all cases. Second, the Darfield earthquake caused spreading displacements of the order of 30cm–60cm and 80cm–100cm at the river banks near the Dallington and South Brighton bridges respectively, but no substantial spreads at Fitzgerald and ANZAC bridges. All four bridges were affected by substantial spreading in the Christchurch earthquake which is consistent with the extreme liquefaction and higher seismic demand generated by this event. Finally, it is apparent in figure A.21 that for both meandering loops at the Fitzgerald Bridge and Dallington Bridge large ground displacements of 50cm–100cm occurred in the point bar deposits on the north banks while much smaller movements of less than 20cm were observed in the cut-banks on the south side of the river. This feature was clearly reflected in the level of damage sustained at the north approach/abutment (heavy) and south approach/abutment (light damage) of these bridges.
Appendix A: Mechanism and effects of liquefaction and lateral spreading

The road bridges of Christchurch are typically two or three span, short- to moderate-length bridges. Older bridges are integral systems while recent bridges are commonly precast concrete bridges with moveable joints. They all have sturdy configurations, and large stiffness and strength in the longitudinal direction provided by a rigid deck-wall or deck-girder superstructure. Hence, when subjected to large spreading displacements and closing of the banks towards the river, the bridge superstructure resisted the ground movement and played a key role in the development of a characteristic mechanism of deformation (damage). Figure A.22 schematically illustrates the spreading-induced damage mechanism which was typically observed for the road bridges of Christchurch. It involves deck-pinning, back-rotation of the abutments and consequent deformation (damage) to the abutment piles, and also slumping of the approaches with large vertical offsets between the approaches and pile-supported deck of the bridge.

It is interesting to note that the bridges on the Heathcote River sustained much less damage despite being in areas of higher accelerations and closer to the causative fault of the most destructive 22 February 2011 earthquake. With the exception of the severely damaged Ferrymead Bridge, which was essentially located on top of the causative fault of the Christchurch earthquake, only three or four bridges on the Heathcote River suffered moderate damage to the approaches and some structural/abutment damage. One may argue that two main factors contributed to the much better performance of the Heathcote River bridges: first and foremost, lateral spreading displacements were much smaller along the Heathcote River, and second, the bridges on Heathcote River have shorter spans/lengths.
A5.4.4 Liquefaction-induced damage to bridges: case studies

For clarity of presentation, the damage to the South Brighton Bridge, at the mouth of the Avon River is first described followed by a description of the spreading-induced damage to Dallington (Gayhurst), Fitzgerald and ANZAC bridges. Even though only a small group of bridges is considered, they cover a wide age span (from 1954 to 2000) and varying structural systems (integral bridges and bridges with movable deck joints). Importantly, they clearly illustrate the typical deformation mechanism and damage associated with lateral spreading.

South Brighton Bridge

The South Brighton Bridge is located at the entry of the Avon River into the estuary (figure A.23). The three span (65m long) RC bridge was constructed in 1980. It runs approximately in the east-west direction. The bridge superstructure consists of cast in-situ RC deck on precast 'I' beams, and is supported through elastomeric bearings on two octagonal 'hammerhead' RC piers and seat-type RC abutments. The foundations of the bridge consist of 44 precast concrete piles, 10 beneath each abutment and 12 beneath each pier (CCC, private communication 2011). The octagonal piles are 450mm wide, either vertical or raked (4 on 1), and are rigidly connected to the abutments or the pile caps at the piers. The abutment piles are 18.7m long while those beneath the piers are 13.3m long.

The bridge site is in a wetland area (figure A.23a), where the thickness of recently deposited soils is ~40m. Approximately 4m high embankments of uncontrolled fill material were constructed at both approaches. At the east abutment/approach, except for the variable top soil of sandy silt, fill and lenses of peat up to 2m depth, the soil profile consists of uniform fine and medium sands, which are relatively loose in the top 5m–6m, and then medium dense at greater depths down to at least 25m depth (Cubrinovski et al 2013). Preliminary analyses based on SPT and CPT procedures indicate that the top 8m of the deposit below the water table liquefied in the Christchurch earthquake with some partial liquefaction and limited shear strains developing at larger depths. As shown in figure A.21, permanent lateral ground displacements of 2.9m were measured approximately 23m to the south of the west abutment of the bridge, after the Christchurch earthquake.

Large ground distortion and slumping of the approaches was evident on both sides of the bridge. The slumping resulted in large settlement of the approaches and vertical offset between the pile-supported bridge deck and embankment approaches resting on soft native soils. The slumping was accompanied by spreading of the approaches both towards the river but also down the slope of the embankments (parallel to the river). Unlike the unconstrained spreading of the river banks, the deformation and movement of the...
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embankment approaches towards the river was significantly affected and restricted by the bridge structure itself.

Figure A.23 depicts the mechanism of spreading-induced damage to the South Brighton Bridge. It involved large spreading-induced movement of the banks towards the river/bridge (as illustrated in figure A.23a, which was resisted by the stiff bridge superstructure. After closing the small gap between the abutment wall and the deck beams, the rigid superstructure effectively prevented any additional movement of the abutment (at the girder level) in the longitudinal direction, and the deck-pinning resulted in a back-rotation of the abutments (figure A.23b) about the beam-abutment point of collision. The abutment back-rotation occurred because the foundation piles could not resist the spreading of the foundation soils towards the river. Figure A.23e shows clear evidence of large distress in the foundation soils surrounding the abutment piles consistent with spreading of the foundation soils towards the river. The permanent backward tilt of the abutments of the South Brighton Bridge was about 7º–8º, after the Christchurch earthquake. This back-rotation forced the top of the abutment piles to displace laterally ~20cm towards the river. These large lateral displacements, in conjunction with the rotational constraints at the pile head imposed by the rigid pile-abutment connection, caused bending of the piles resulting in tensile cracks on the river side (figure A.23c) and concrete crushing/spalling on the land side of the piles (figure A.23d).

There was no serious damage to the bridge superstructure, with only minor pounding damage at the abutments and some relative movement apparent in the dislocated bearings. Following the temporary repair of the approaches and infilling of the offsets between the approaches and the deck, the bridge was back in service almost immediately after each earthquake event.

Figure A.23  South Brighton Bridge: a) aerial view of the bridge towards south; b) permanent tilt of the west abutment due to deck (girder)-pinning; c) bending cracks at the top of abutment pile (river side); d) concrete crushing/spalling on the land side of abutment pile; e) ground distress in the foundation soils due to spreading (Cubrinovski et al 2014)
**Dallington (Gayhurst) Bridge**

The Dallington Bridge is located on the Avon River approximately 1 km to the east of the CBD (figure A.24). It is an integral bridge consisting of a continuous RC deck, RC piers and RC abutment walls with wing walls. The bridge is only 26.8 m long and has three spans (8.2 m, 10.4 m and 8.2 m respectively) without any expansion joints. Both the piers and abutments are supported on square reinforced concrete piles 350 mm in width and 10.4 m in length. Seven piles at 4D spacing are used beneath the piers, while six piles at 6D spacing support each abutment. The bridge was constructed in 1954.

The Dallington Bridge runs approximately in the north-south direction. The bridge spans point bar deposits on the north side and cut-banks on the south side of the bridge. At the north (point bar) side, the soil profile consists of 2.5 m of top soil (brown sandy silt and silt with some peat), overlying a grey fine sand (with occasional gravelly sands) that reaches up to about 15 m depth, sandy silt from 15 m–20 m depth and fine sand from 20 m–24 m depth. The fine sand from 2.5 m to approximately 9 m depth is loose, with consistently low CPT resistance ($q_c \approx 5$ MPa). The bearing stratum of the piles is the underlying dense sand layer at about 13 m–16 m depth. The penetration resistance is much higher at the south side of the bridge, which is consistent with the significant contrast in liquefaction manifestation, lateral spreading effects and bridge damage that was observed between the north and south approaches of the bridge. On the north side (in the suburb of Dallington), severe liquefaction occurred repeatedly during all major 2010–2011 earthquakes with spreading displacements of the river banks of 30 m–70 cm. The spreading was accompanied by large ground distortion and subsidence of the northern approach of the bridge of about 1 m (figure A.24a). Conversely, there was very little evidence of land damage on the south (cut-bank) side and approach of the bridge (figure A.24b).

The bridge suffered the same characteristic damage mechanism outlined above involving spreading, deck-pinning and back-rotation of the abutment walls. The effects of this mechanism are evident in figure A.24c which shows large differential movements and failure of the north wing wall of the bridge. The inward rotation of the north abutment wall was about 1.2° or five times less than the permanent tilt observed for the abutments of the South Brighton Bridge, which reflects the rigidity of the integral bridge structure. Further detailed inspections confirmed a formation of a wide crack at the connection between the deck and the abutment, which led to yielding of the top bars of the deck.
Appendix A: Mechanism and effects of liquefaction and lateral spreading

Figure A.24  Dallington (Gayhurst) Bridge: a) subsidence of ~1m at the north approach (point-bar deposit); b) no visible damage or ground distress at the south approach (cut-banks); c) failure of the north wing wall due to large differential movements between the adjacent river banks and the abutment wall (Cubrinovski et al 2014)

Fitzgerald Bridge
The Fitzgerald Bridge (two span, 28m long, constructed in 1964) was originally of segmental design with expansion joints between the spans and approaches, but was later retrofitted with steel gusset plates rigidly connecting the deck beams to the central pier and abutments in an attempt to create an integral bridge system. As previously discussed, the northern abutment of the bridge is on the inside bank of the river bend where substantial lateral spreading occurred (figure A.25a). As shown in figure A.25b, a permanent inward-tilt of ~7.5º was observed at the northeast abutment. At this abutment, the settlement and lateral movement of the foundation soils towards the river exposed the top of the abutment piles (figure A.25c). The easternmost pile (raked at 1:4) had completely sheared through at the connection with the abutment exposing the reinforcing bars.
Anzac Bridge

The ANZAC Bridge is located in the Burwood-Bexley wetland area on the Woolston-Burwood expressway. The bridge runs approximately in a north-south direction and has a roundabout at the north approach (figure A.26a). The 48m long three-span bridge was constructed in 2000. The superstructure consists of a precast concrete hollow-core (double) deck and precast concrete beams, and is supported on in-situ concrete piers and abutments. The 1m by 1m rhomboid piers are founded on circular reinforced concrete piles, 1.5m in diameter with 8mm thick permanent steel casing (NZ Transport Agency 2011). The piles are 20m long and at a spacing of 4.7D. Each abutment is supported on 16 steel ‘H’ piles (310 x 133). The piles are 22m long (reaching the same depth as the pier piles) and are at 1.5m spacing.

Massive liquefaction occurred in the area of the bridge during the Christchurch earthquake, as illustrated in figure A.26a where large volumes of sand ejecta are seen on the south side of the bridge. There was a clear evidence of substantial lateral spreading towards the river, with large cracks and fissures in the ground running parallel to the river (figure A.26c). Permanent lateral spreading displacements of 0.9m–1.1mm were measured at the river banks adjacent to the south abutment. On the north side, the roundabout affected the spreading both with its stiffness and topographic feature, and hence the magnitude of lateral spreading displacements was inconclusive, but likely to be around 40cm or slightly greater.
Again the same characteristic damage mechanism depicted in figure A.22 was evident at the ANZAC Bridge. Figure A.26b illustrates the movements at the south abutment with the red arrow indicating an inward tilt of the abutment of about 6°. The horizontal arrows and associated displacements indicate permanent lateral displacements at the bottom of the abutment (top of the H-piles) due to back-rotation of the abutment, lateral offset of the precast concrete underpass, and lateral offset of the surrounding soil at the interface between the paved track and the RC underpass. These displacements infer a horizontal displacement at the top of the piles of about 20cm (ie 16cm due to abutment rotation, and 3cm–4cm displacement required to close the gap between the abutment and the deck-girder). Note that the pedestrian underpasses were founded on independent foundations consisting of 1.2m diameter RC piles. These piles are only 6m long, and they effectively floated in the liquefied soils, moving together with the surrounding foundation soils. The lateral displacements of the south underpass relative to the abutment were about 20cm at its edges and 50cm–60cm in its central part (Cubrinovski et al 2013). By superimposing these displacements, one can infer lateral displacements of the foundation soils surrounding the abutment piles of 40cm–80cm, which are substantially less than the 1m displacement of the river banks in the free field.

The spreading-induced damage caused slumping of the approaches which required immediate repair/infilling due to the large vertical offsets between the deck and the approaches (figure A.26d). The superstructure sustained some visible damage with pronounced cracking of the interior beam-pier connection (figure A.26e) and concrete spalling due to excessive compression at exterior beam-pier connections. Rebar in the bridge deck was also exposed due to deck-abutment pounding; however, this structural damage was not serious and the bridge remained in service after each earthquake.

Figure A.26  ANZAC Bridge: a) aerial view towards north (massive sand ejecta on the south banks, and the roundabout at the north approach of the bridge); b) back-rotation of the abutment (red arrow) with permanent lateral displacements of the abutment base, adjacent pedestrian underpass and surrounding foundation, and free-field soils; c) evidence of large lateral spreading displacements towards the river; d) temporary repair of the south approach; e) cracks of interior beam-pier joint (Cubrinovski et al 2014)
A5.4.5  Conclusions from Cubrinovski et al (2014)

The Canterbury earthquakes triggered widespread liquefaction over approximately one third of the Christchurch area. Along the Avon River, the liquefaction was accompanied by substantial lateral spreads which affected practically all bridges downstream from the CBD. The road bridges at river crossings are two-to-three span, short- to moderate-length bridges with rigid superstructure. Thus, when subjected to large spreading displacements of the river banks, the bridge superstructure resisted the ground movement and led to the development of a characteristic damage mechanism involving deck-pinning, abutment back-rotation and damage of the abutment piles. The key findings from the case studies are:

- Both segmental and integral bridges exhibited the same characteristic deformation/damage mechanism. Permanent inward tilts of the abutments of ~6° to 8° were observed for segmental bridges, while the back rotation was smaller for integral bridges. The abutment back-rotation resulted in permanent lateral displacements (as large as 20cm–30cm) and damage at the top of the abutment piles.

- The damage involved slumping of the approaches and large vertical offsets between the approaches and the pile-supported deck. Large spreading displacements and subsidence of the approaches were observed particularly at point bar deposits on the inside bank of meandering river bends.

- Well-documented case studies indicate that lateral movements of the foundation soils were greater than the movements of the abutment piles, but substantially smaller than the free-field displacements of the spreading river banks. Thus, the commonly adopted use of free-field displacements in PSA might be overly conservative for bridges with a sufficient capacity to resist large spreading displacements.

The principal findings from the PSAs are:

- Single pile and global PSAs produced consistent results and accurately simulated the observed deformations and damage of the ANZAC Bridge. The constrained translation at the point of abutment rotation provided a key boundary condition that enabled the use of the single pile PSA for the abutment piles.

- The response of the abutment piles was found to be controlled by the magnitude of lateral ground displacement and lateral load from the crust. Good accuracy in the simulations was obtained using measured ground displacements and typical values for the model parameters. The abutment pile response was virtually insensitive to the variation in the properties of the liquefied soil and deeper non-liquefied layers.

- The global bridge analysis with applied ground displacements at the abutment and pier piles showed an important influence of the latter on the pier response and clearly demonstrated the need to consider the response of the bridge and its components using a global interaction model.

A6  References


Appendix A: Mechanism and effects of liquefaction and lateral spreading


Appendix A: Mechanism and effects of liquefaction and lateral spreading


Marchetti, S, P Monaco, G Totani and D Marchetti (2008) In situ tests by seismic dilatometer (SDMT). ASCE geotechnical special publication no.170. 20pp.


Appendix A: Mechanism and effects of liquefaction and lateral spreading


Appendix B: Example calculation

An example calculation is presented for single-pile and global bridge analyses using the ANZAC Bridge analysis given in Cubrinovski et al (2014). The lateral spreading case only is presented here, though cyclic liquefaction analysis was also conducted for the bridge.

Table B.1 summarises the parameter values for the lateral spreading analyses with reference values based on median values or best estimates for each parameter, and lower bound (LB) and upper bound (UB) values of the parameters based on previous studies (Cubrinovski et al 2006; 2009).

B1 Single pile analyses

Independent single pile PSAs were conducted for the north abutment and south abutment using the subsurface conditions shown in figure B.2.

The soil profile generally consists of a 2m thick fill and then variable top sandy soil to about 4m depth, overlying a uniform fine to medium sand from 4m to 17m depth (with $q_c <5$MPa at shallow depths and $q_c = 10$–20 MPa at larger depths), and slightly coarser and denser sands below 17m depth (with $q_c >20$ MPa).

B1.1 Liquefaction triggering analysis

The shaded layers in figures B.2 and B.3 indicate liquefied layers with factors of safety of $F_S < 1.0$ according to the Robertson and Wride (1998) method applied for the Christchurch earthquake. These analyses show larger thicknesses of liquefied layers at shallow depths (up to 10m depth) for the south abutment profile, where larger lateral spreading displacements were observed. Some details of the liquefaction triggering analysis and subsequent calculations of the lateral ground displacements using the Zhang et al (2004) method are given in figure B.3. Here, the ‘adopted profile’ is simplified for the analysis based on SPT and CPT information, and CSR values are shown for the Darfield and Christchurch earthquakes for an equivalent magnitude 7.5 earthquake (ie CSR 7.5.)

B1.2 Free-field ground displacements

Using the calculated $F_S$ values, the distribution of lateral spreading displacements throughout the depth was then estimated based on the method of Zhang et al (2004). The objective of these calculations was to determine the distribution of ground displacements throughout the depth of the profile, which is shown in figure B.2 as normalised $U_g / U_{g\text{max}}$ displacements, where $U_{g\text{max}}$ is the displacement at the top of the liquefied layer. In the PSAs, this distribution of ground displacement was multiplied by the measured lateral spreading displacements (figure B.2) and applied at the end of the soil springs. Since ground displacements generally need to be predicted, the surface ground displacement due to spreading can be estimated using one of the empirical methods, ie Zhang et al (2004) or Youd et al (2002).

It is important to consider the best-estimate values as well as the LB and UB estimates for the ground displacements. In this example, the best estimate value for the south abutment is $U_{g\text{max}} = 66$cm, while the LB and UB estimates are $U_{g\text{max}} = 40$cm and $U_{g\text{max}} = 100$cm respectively. The Zhang et al (2004) method overestimated the measured lateral spreading displacements at the Anzac Bridge, which clearly points out the uncertainties in these estimates and the need to consider a range of anticipated ground displacements.
Table B.1 Soil spring parameters used in pseudo-static analysis

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<td></td>
<td></td>
<td>$\beta_{liq}$ [\text{\textdegree}]</td>
<td>-</td>
<td>0.01</td>
<td>0.001</td>
<td>0.02</td>
</tr>
<tr>
<td><strong>Non-liquefied layers</strong></td>
<td>Strength</td>
<td>$p_{\text{max}}$ [FL-2]</td>
<td>$p_p$</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\phi'_{nl}$ [\text{\textdegree}}</td>
<td>$20 + \sqrt{20(N_{160})}$</td>
<td>Calc.</td>
<td>33'</td>
<td>37'</td>
</tr>
<tr>
<td></td>
<td>Stiffness</td>
<td>$K$ [FL-1]</td>
<td>$\beta_{nl} I_s D_o 56 N(100 D_o)^{-3/4}$</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\beta_{nl}$ [\text{\textdegree}]</td>
<td>-</td>
<td>1</td>
<td>0.3</td>
<td>1</td>
</tr>
</tbody>
</table>

Parameters:

- $p_{\text{max}}$ | soil spring ultimate strength (pressure)
- $p_p$ | Rankine passive pressure
- $\alpha$ | factor to account for the ‘wedge-effect’ of increased pressure on a single pile in comparison to an equivalent wall
- $\phi'$ | soil friction angle
- $N_{160}$ | SPT blowcount
- $(N_{160})$ | SPT blowcount corrected for overburden pressure and energy ratio
- $S_r$ | residual strength of liquefied soil
- $H_a$ | height of abutment.

The moment curvature relationships for the deck and pile abutment, pier pile, abutment pile and pier are shown in figure B.1. Further structural details of the bridge are given in appendix A, section A5.4.4.
Notes:

- Spring stiffness was assessed by back-calculation from the displacement required to mobilise passive pressures ($\delta_u$) and by forward-calculation of spring stiffness using subgrade reaction coefficient method (eg Tokimatsu and Asaka 1998)
- Relative density ($D_r$) of 70%–80% was assessed for the crust fill ($D_r = 14\sqrt{(N_1)_{60}}$), figure 10 in Cubrinovski et al (2009)
- Residual shear strength, $S_r$, was taken as a function of SPT blowcount (eg Seed and Harder 1990)

Figure B.2 Subsurface conditions at the bridge (north and south abutments) showing layers with FS <1.0 for the ‘design earthquake’ liquefaction triggering analysis (Robertson and Wride 1998); normalised spreading displacement profile computed based on Zhang et al (2004) method is also shown (Cubrinovski et al 2014)
Figure B.3. Details of the liquefaction triggering analysis (Robertson and Wride 1998) and computed normalised spreading displacements for the south abutment (Zhang et al 2004) method is also shown (Winkley 2013).

Figure B.4 summarises some of the results of the single pile PSAs in which peak ground displacements of $U_{g\text{max}} = 40\text{cm}, 66\text{cm}$ and $100\text{cm}$ were applied at the south abutment. Horizontal displacements and bending moments along the abutment piles are shown in figure B.4 for six independent analyses. Note that three different ground displacement profiles were applied (three separate analyses), shown with black solid lines: then two sets of analyses were conducted (six analyses in total) using two different soil spring models: reference model (RM) analyses with reference properties, shown with red solid lines, and a model with RM properties for all parameters except for the crust strength, for which LB values are used (shown with blue dashed lines). In the single pile analyses, the abutment is modelled by a rigid beam element (ie as an elastic member with very large stiffness) which is constrained laterally at the point of abutment rotation. Therefore displacements at the top of the piles are zero.
There is a significant influence of the magnitude of the applied ground displacement on the response of the abutment piles, both in terms of the pile displacements and the level of damage to the piles (i.e., whether bending moments reach yield ($M_y$) and ultimate levels ($M_u$) shown on figure B.1). It should be noted that for the maximum applied ground displacement of 100 cm, which corresponds to the observed free-field lateral spreading displacements at the south river banks, the computed pile-head displacements are much greater than the observed displacements. This indicates that the use of free-field lateral spreading ground displacements as an input in the PSA might be conservative for short-span bridges with stiff and strong superstructure.

B1.3 Soil spring parameters: crust layer

The stiffness of the soil spring is based on the subgrade reaction approach using an SPT-based empirical correlation given in Tokimatsu and Asaka (1998). The stiffness was degraded using a degradation factor $\beta$ accounting for stiffness reduction due to soil nonlinearity ($\beta_{nl}$) or liquefaction ($\beta_{liq}$). Alternatively, the stiffness of the crust could be determined using empirical charts for the relative displacement $\delta_u$ required to fully mobilise the ultimate pressure (Cubrinovski et al 2009b). The stiffness of the soil spring is summarised in Table B.1.

A series of analyses was first performed for each abutment using the reference model parameters, followed by a sensitivity study in which the value of one parameter was set first at its lower bound (LB) and then at its upper bound (UB) value with all other parameters kept at their reference model values. In this way, the sensitivity of the pile response to each particular parameter was examined. Figure B.4 presents the results of the analyses investigating the effects of the crust parameters on the pile response ($\phi_{cr}$, $\alpha_{cr}$, $\beta_{cr}$, and $\delta_u$). The reference model response, shown in red solid lines, indicates horizontal displacement at the top of the south abutment pile (figure B.4a, note that the pile top is at the bottom of the shaded area in the figure which indicates the abutment) of ~35 cm which is greater than the observed displacement of ~16 cm (associated with abutment rotation. When varying the stiffness parameters of the crust ($\beta_{cr}$ or $\delta_u$) and $\phi_{cr}$, the pile response only changed slightly and remained within the shaded area along the RM

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**Figure B.4** Computed pile displacements and bending moments using RM (reference model) spring parameters (red lines) and lower bound crust layer parameters (dashed blue lines) for three levels of ground surface displacements of 40 cm, 66 cm and 100 cm (Cubrinovski et al 2014)
response, shown in figure B.3a. However, the pile response substantially changed and approached the measured displacements when $\alpha_{cr-LB}=3$ was used with reference model values for all other parameters, indicating the large sensitivity of the pile response to this crust strength parameter. Recognising this sensitivity, an additional analysis was conducted using the LB values for all the crust strength parameters (i.e. $\alpha_{cr-LB}=3$, $\phi'_{cr-LB}=33^\circ$), which reduced the pile head displacements to the values slightly below the measured ones. This demonstrates that the modelling of the crust governs the abutment pile response. The bending moments (figure B.4b) indicate that the south abutment piles exceeded the yield level and approached the ultimate moment at $\sim0.5$m to 2m below the pile head, and also at the interface of the liquefied and non-liquefied layers at $\sim15$m depth.

B1.4 Soil spring parameters: liquefied layers and deeper non-liquefied layers

Sensitivity analyses were also performed where parameters of the liquefied and non-liquefied layers were varied between their LB and UB values, given in table B.1. The influence of the liquefied and non-liquefied layer parameters on the abutment pile response was insignificant. The results of all of these analyses varied within a few percent from the RM response of the abutment piles shown in figure B.4.

B.2 Global bridge analyses

A series of global bridge analyses was also conducted to account for the substantial variation in the liquefaction-induced ground displacements acting on the abutment and pier piles, and for the effects of soil-pile-pier/abutment-superstructure interaction. A schematic view of the global bridge model, including a summary of the applied ground displacements and computed bridge displacements and bending moments for the piers and pier piles is shown in figure B.5.

First, analyses were performed in which lateral ground displacements were applied only to the abutments and abutment piles (A-analysis). The results from the global A-analyses were practically identical to those of the single pile analyses presented in figure B.4. For reference, figure B.5 shows the displaced shape of the A-analysis using LB values for crust strength parameters and RM values for all other parameters, and ground displacements of 36cm and 66cm at the north and south abutments respectively.

Next, ground displacements were also applied to the pier piles (i.e. in addition to the ground displacements at the abutments and abutment piles), as indicated schematically in figure B.5 (referred to as AP-analyses). The ground displacement at the top of the pier piles was assumed to be 50% of that at the respective elevation for the abutment piles while its distribution with depth was evaluated using the triggering and normalised displacement calculation, as previously discussed. The results of AP-analyses in figure B.4 show that the inclusion of a lateral ground displacement at the pier piles significantly increased the pier displacements and created bending moments close to the ultimate moment at the top of the piers.

Given the significant uncertainties associated with the ground displacements at the piers and effects of liquefaction, two additional AP-analyses were conducted. First, the applied ground displacements at the pier piles were reduced to 20% of the initial value (0.2AP analysis), and second, the strength of the non-liquefied layers (springs) was reduced to 50% of its initial value to assess the effects of strength reduction (due to excess pore pressures) in the non-liquefied layers sandwiched between liquefied layers (AP-$\alpha_{nl-0.5}$ analysis).

Results from all three AP-type analyses indicated that the pier piles did not suffer substantial damage. Only in the case of the AP-analysis, yielding of the steel casing occurred in the south pier piles at $\sim12$m below the pile head. However, all analyses suggest some damage at the top of the piers corresponding to the yield moments, and a similar but smaller level of damage at the base of the piers. The computed
moments at the top of the pier are probably overestimating the actual pier moments because a fully restrained connection between the deck and the pier-cap was adopted in the analysis. The global analysis also indicated that the whole bridge displaced ~7 cm to the north.

Both single pile and global PSAs produced results consistent with the observed displacements and damage of the ANZAC Bridge. The analyses accurately simulated the observed spreading-induced mechanism and provided additional insight into the response of the bridge and its pile foundations.

Figure B.5 Displaced shape of the A-analysis using lower bound values for crust strength parameters and reference model values for all other parameters

B3 References


## Appendix C: Glossary

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>AASHTO</td>
<td>American Association of State Highway and Transportation Officials</td>
</tr>
<tr>
<td>AIJ</td>
<td>Architectural Institute of Japan</td>
</tr>
<tr>
<td>ASCE</td>
<td>American Society of Civil Engineers</td>
</tr>
<tr>
<td>Atterberg limit tests</td>
<td>laboratory tests to determine the liquid and plastic limits of soil</td>
</tr>
<tr>
<td>CCC</td>
<td>Christchurch City Council</td>
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<tr>
<td>CDIT</td>
<td>Coastal Development Institute of Technology, Tokyo</td>
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<tr>
<td>CPT</td>
<td>cone penetration test</td>
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<tr>
<td>CRR</td>
<td>cyclic resistance ratio</td>
</tr>
<tr>
<td>CSR</td>
<td>cyclic stress ratio</td>
</tr>
<tr>
<td>EPOLLS</td>
<td>empirical prediction of liquefaction-induced lateral spreading</td>
</tr>
<tr>
<td>EPWP</td>
<td>excess pore water pressures</td>
</tr>
<tr>
<td>ESA</td>
<td>effective stress analysis</td>
</tr>
<tr>
<td>grabens</td>
<td>a section of earth lying between two faults and displaced downward relative to the blocks either side</td>
</tr>
<tr>
<td>horst</td>
<td>a raised block of earth lying between two faults</td>
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<tr>
<td>JRA</td>
<td>Japan Road Association</td>
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<tr>
<td>LB</td>
<td>lower bound</td>
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<tr>
<td>LDI</td>
<td>lateral replacement index</td>
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<tr>
<td>LiDAR data</td>
<td>data collected by an optical remote sensing technique (usually flyover) which gives points on the surface of the earth</td>
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<tr>
<td>LPI</td>
<td>liquefaction displacement index</td>
</tr>
<tr>
<td>MSF</td>
<td>magnitude linear regression</td>
</tr>
<tr>
<td>NZGS</td>
<td>New Zealand Geotechnical Society</td>
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<tr>
<td>PEER</td>
<td>Pacific Earthquake Engineering Research</td>
</tr>
<tr>
<td>PGA</td>
<td>peak ground acceleration</td>
</tr>
<tr>
<td>PL</td>
<td>probability of liquefaction</td>
</tr>
<tr>
<td>PSA</td>
<td>pseudo-static analysis</td>
</tr>
<tr>
<td>QA</td>
<td>quality assurance</td>
</tr>
<tr>
<td>RC</td>
<td>reinforced concrete</td>
</tr>
<tr>
<td>revetment</td>
<td>a sloping structure placed on river banks or cliffs in such a way as to absorb the energy of incoming water</td>
</tr>
<tr>
<td>SFSI</td>
<td>soil-foundation-structure interaction</td>
</tr>
<tr>
<td>Abbreviation</td>
<td>Definition</td>
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<td>--------------</td>
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<tr>
<td>SPT</td>
<td>standard penetration test</td>
</tr>
<tr>
<td>TSA</td>
<td>total stress analysis</td>
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<tr>
<td>UB</td>
<td>upper bound</td>
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